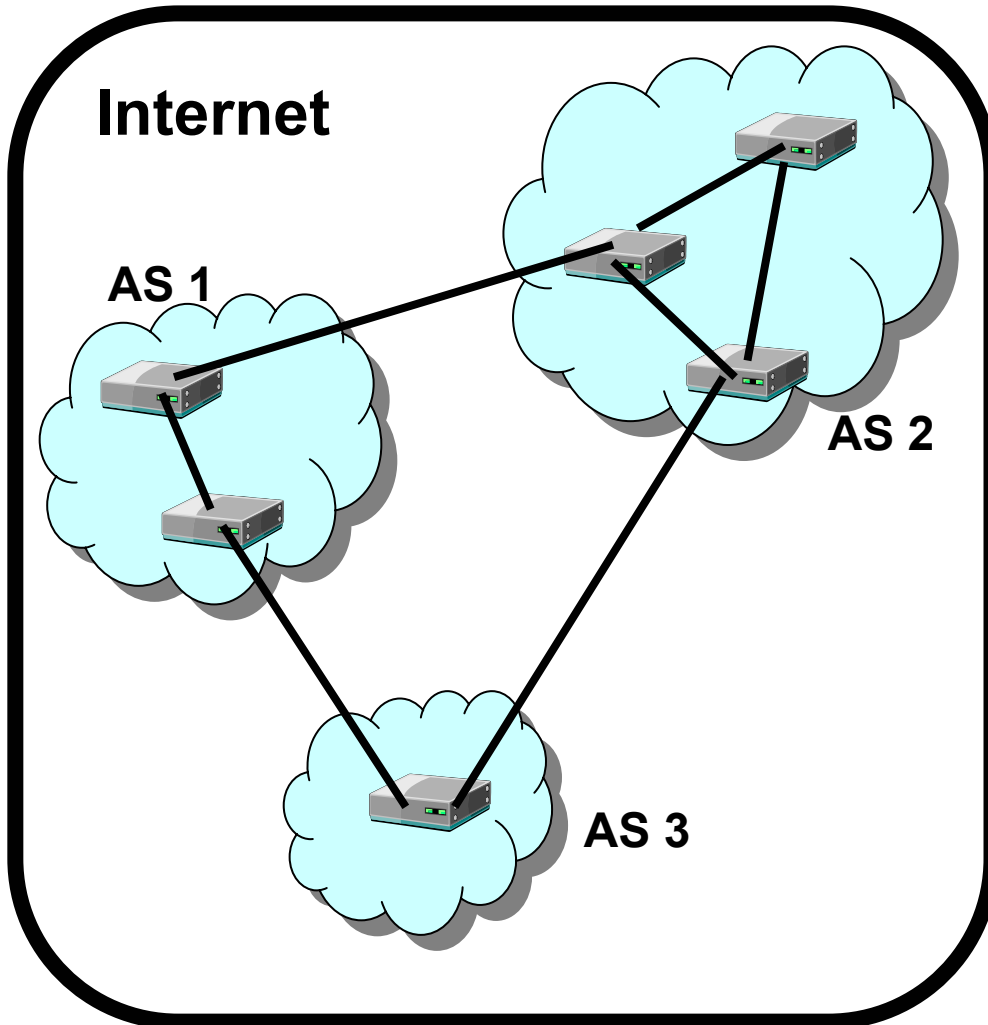


Network Tomography

Christos Gkantsidis

Introduction



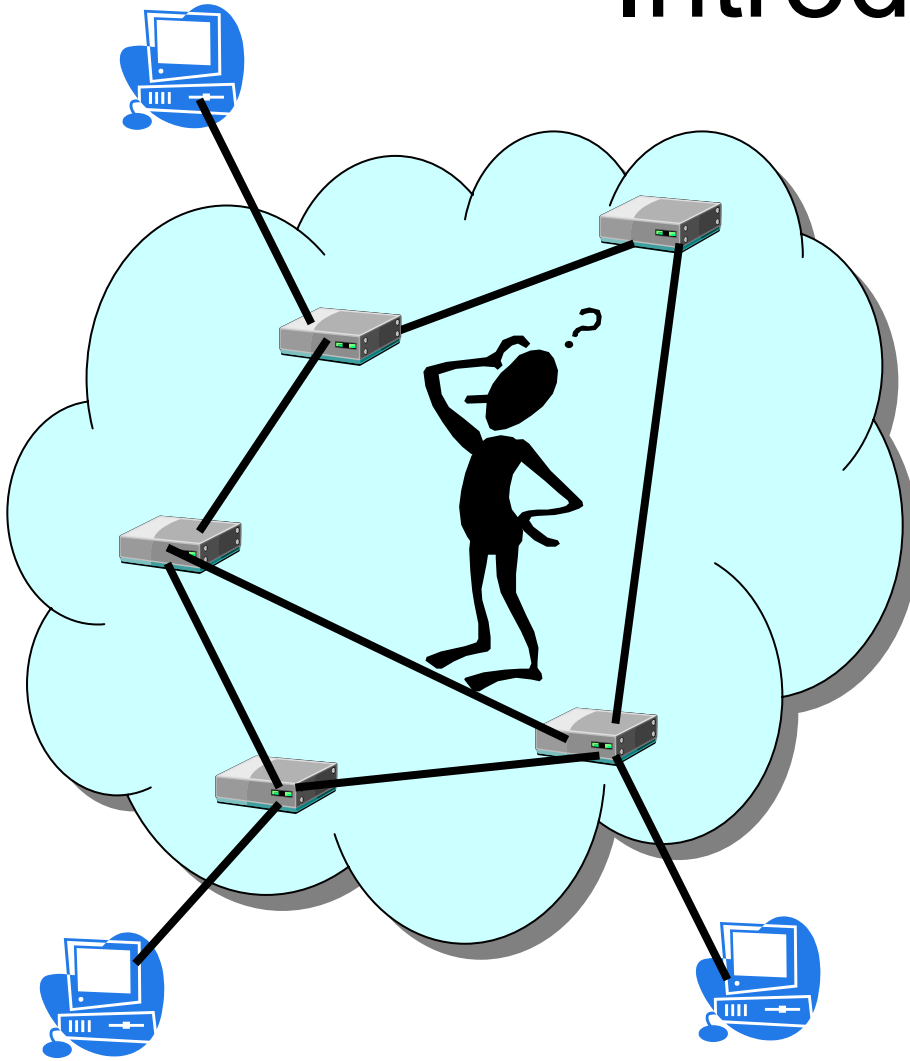
What is the:

- Bandwidth
- Loss Rate
- Connectivity

of the **links** of the network?

Using **only end-to-end** measurements.

Introduction



What is the:

- Traffic demands between **users** of the network?

Using **only limited link** measurements.

Network Tomography

Use a **limited** number of measurements to **infer** network (**link**) performance parameters, using:

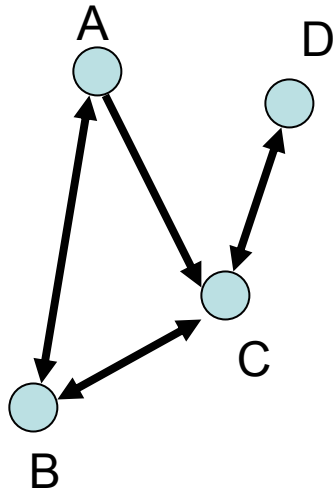
- Maximum Likelihood Estimator.
- Bayesian Inference.

and assuming a **prior model**.

Categories of problems:

- Link level parameter estimation.
- Topology Inference.
- Sender-Receiver traffic intensity.

Sender-Receiver Traffic Intensity



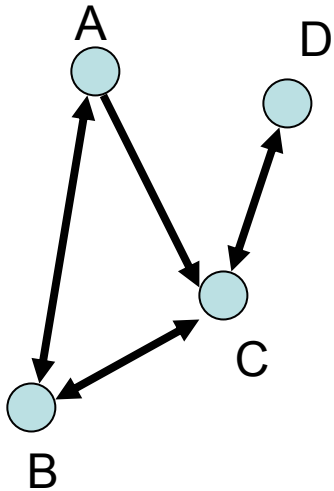
Links

Routing Matrix

	1	2	3	4	5	6	7	8	9	10	11	12
	ab	ac	ad	ba	bc	bd	ca	cb	cd	da	db	dc
1 (a→b)	1	0	0	0	0	0	0	0	0	0	0	0
2 (a→c)	0	1	1	0	0	1	0	0	0	0	0	0
3 (b→a)	0	0	0	1	0	1	1	0	0	1	0	0
4 (b→c)	0	0	0	0	1	0	0	0	0	0	0	0
5 (c→b)	0	0	0	0	0	0	1	1	0	1	1	0
6 (c→d)	0	0	1	0	0	1	0	0	1	0	0	0
7 (d→c)	0	0	0	0	0	0	0	0	0	1	1	1

Source-Destination Pairs

Sender-Receiver Traffic Intensity



Routing Matrix

	1	2	3	4	5	6	7	8	9	10	11	12
	ab	ac	ad	ba	bc	bd	ca	cb	cd	da	db	dc
1 (a→b)	1	0	0	0	0	0	0	0	0	0	0	0
2 (a→c)	0	1	1	0	0	1	0	0	0	0	0	0
3 (b→a)	0	0	0	1	0	1	1	0	0	1	0	0
4 (b→c)	0	0	0	0	1	0	0	0	0	0	0	0
5 (c→b)	0	0	0	0	0	0	1	1	0	1	1	0
6 (c→d)	0	0	1	0	0	1	0	0	1	0	0	0
7 (d→c)	0	0	0	0	0	0	0	0	0	1	1	1

Links

Source-Destination Pairs

$$Y_{rx1} = A_{rxp} * X_{px1} \quad \text{with } p \gg r$$

A = Routing matrix.

X = Source – Destination transmission vector **[Unknown]**.

Y = Link traffic.

Origin-Destination Literature

- **Source-Destination Traffic Estimation.**
[Vardi, J. of the Amer. Statist. Assoc., 1996].
- **Bayesian Inference on Network Traffic Using Link Count Data.**
[Tabaldi and West, J. of the Amer. Statist. Assoc., 1998].
- **Time-Varying Network Tomography.**
[Cao et al., J. of the Amer. Statist. Assoc., 2000].
- **Traffic Matrix Estimation: Existing Techniques and New Directions.**
[Medina et al., ACM SigComm 2002].
- **An Information-Theoretic Approach to Traffic Matrix Estimation.**
[Zhang et al., ACM SigComm 2003].

Link Perf. Inference Literature

- **Multicast-based Inference of Network-internal Characteristics (MINC Project).**
[Caceres, Duffield, LoPresti, Horowitz, Kurose, Towsley, Paxson].
- **Network Loss Inference using Unicast End-to-End Measurement.**
[Coates and Nowak, ITC Seminar on IP Traffic, Measurement and Modelling , 2000].
- **Unicast inference of network link delay distributions from edge measurements**
[Shih and Hero, IEEE Int. Conf. on Acoust. Speech and Sig. Proc., 2001].
- **Nonparametric Internet Tomography.**
[Tsang, Coates, and Nowak, IEEE Intl. Conf. on Acc., Speech and Signal Proc., 2002].
- **Simple Network Performance Tomography.**
[Nick Duffield, ACM IMC 2003].
- **Tomography-based Overlay Network Monitoring.**
[Chen, Bindel, Katz, ACM IMC 2003].

Topology Inference Literature

- Multicast Topology Inference from Measured End-to-End Loss.
[Duffield et al., IEEE Trans. on Info. Theory, 2002]
- **Maximum Likelihood Network Topology Identification from Edge-based Unicast Measurements.**
[Coates et al., ACM Sigmetrics, 2002].
- Merging Logical Topologies Using End-to-end Measurements.
[Coates et al., ACM IMC, 2003].

Outline

- **Origin-Destination.**

Source-Destination Traffic Estimation.

[Vardi, J. of the American Statistical Association, 1996].

- **Link-Level Network Inference.**

Multicast-Based Inference of Network-Internal Loss Characteristics.

[Cáceres, Duffield, Horowitz, Towsley, IEEE Trans. In Information Theory, 1999].

- **Topology Inference.**

Maximum Likelihood Network Topology Identification from Edge-based Unicast Measurements.

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Source-Destination Traffic Estimation

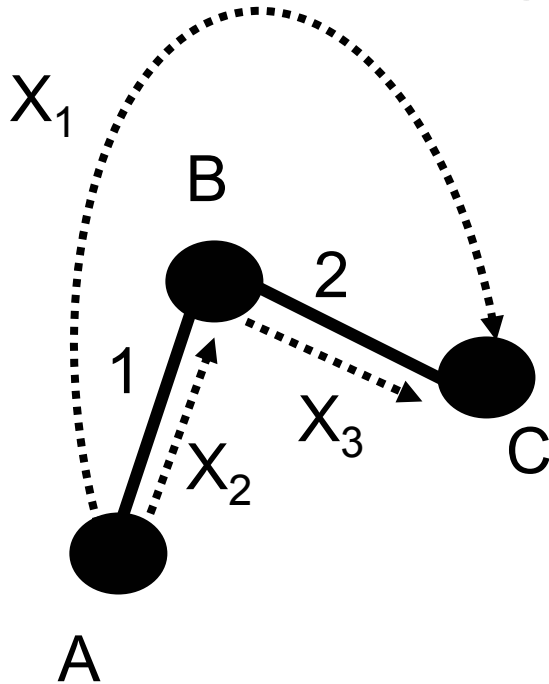
- **Goal:** Given Y_{rx1} , estimate X_{px1} s.t.

$$Y_{rx1} = A_{rxp} * X_{px1}$$

with $r \ll p$.

- **Idea:**
 - Use a model for X_{px1} , eg Poisson with rates λ .
 - Estimate the parameters of the model (λ) that maximize the probability of observing Y_{rx1} .
- **Other Approaches:** Direct measurements with NetFlow, passive monitoring, etc.

A Simple Example.



$$\mathbf{x} = (X_1, X_2, X_3)^T$$

$$\mathbf{Y} = (Y_1, Y_2)^T = (1, 2)^T$$

$$\mathbf{Y} = \begin{pmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix} \cdot \mathbf{x}$$

Model: $X_i \sim \text{Poisson}(\lambda_i)$

1) Find possible \mathbf{x} : **Very expensive!**

$$\mathbf{x} = (1, 0, 1)' \text{ or } \mathbf{x} = (0, 1, 2)'$$

2) Find likelihood of \mathbf{Y} :

$$L(\lambda) = (\lambda_1 \lambda_3 + \lambda_2 \lambda_3^2 / 2) \exp(-\lambda_1 - \lambda_2 - \lambda_3)$$

3) Find λ : $\max_{\lambda} L(\lambda)$. **Maybe corner solution!**

Expectation-Maximization (EM)

Likelihood maximization when:

$$\lambda = E_{\lambda} [\mathbf{X} | \mathbf{Y} = \mathbf{A}\mathbf{X}]$$

Algorithm for finding λ :

1. Pick initial $\lambda^{(0)}$.
2. $\lambda^{(n+1)} = E[\mathbf{X} | \mathbf{Y}, \lambda^{(n)}]$.

Problems:

1. Difficult to evaluate $E[\mathbf{X} | \mathbf{Y}, \lambda]$.
2. May converge to non-MLE point.

Normal Approximation

1. Measure \mathbf{Y} in K periods.
2. Approximate:
$$\mathbf{Y} \sim N_r(\mathbf{A}\boldsymbol{\lambda}, K^{-1} \mathbf{A}\boldsymbol{\Lambda}\mathbf{A}') \text{ with } \boldsymbol{\Lambda} = \text{diag}(\boldsymbol{\lambda})$$
3. Compute sample average $\bar{\mathbf{Y}}$ and sample covariance \mathbf{S} .
4. Equate sample moments to theoretical moments:
 - $\bar{\mathbf{Y}} = \mathbf{A}\boldsymbol{\lambda}$
 - $\mathbf{S} = K^{-1} \mathbf{A}\boldsymbol{\Lambda}\mathbf{A}'$

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- Origin-Destination.

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- **Link-Level Network Inference.**

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- Topology Inference.

Maximum Likelihood Network Topology Identification from Edge-based Unicast Measurements.

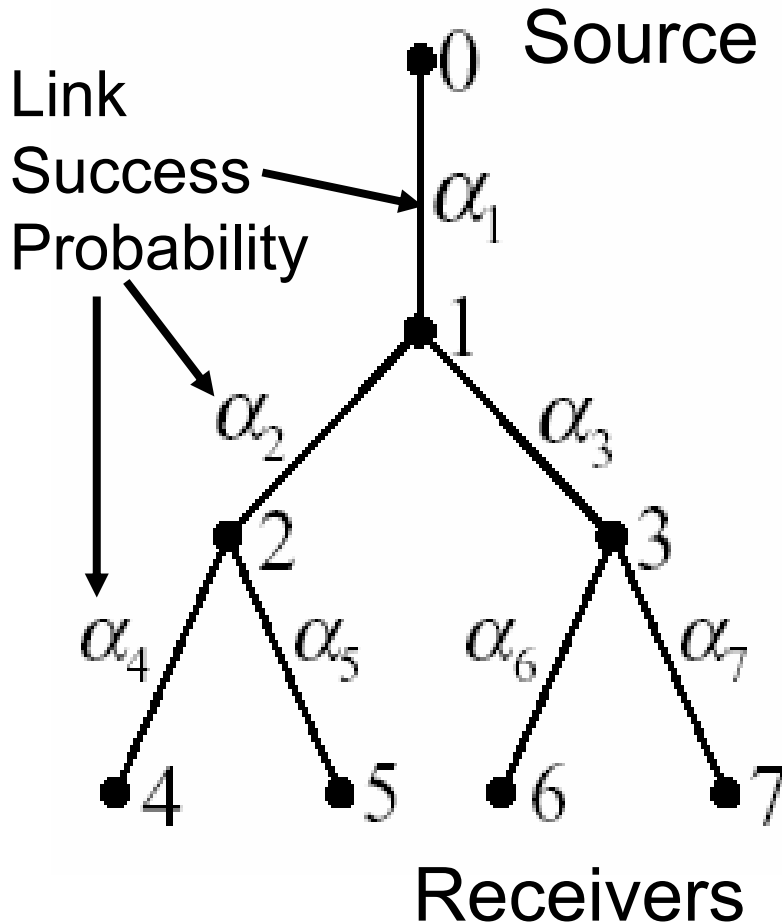
[Coates et al., ACM Sigmetrics, 2002].

Link-Level Network Inference.

- **Goal:** Infer network link characteristics, like loss rate, delay distribution, etc.
- **Idea:**
 - Collect end-to-end measurements.
 - Assume a) known topology, b) **model** for network behavior.
 - Identify *network parameters* that maximize the probability of the observed measurements.
- **Other Approaches:** pathchar, traceroute, clink, etc

Model

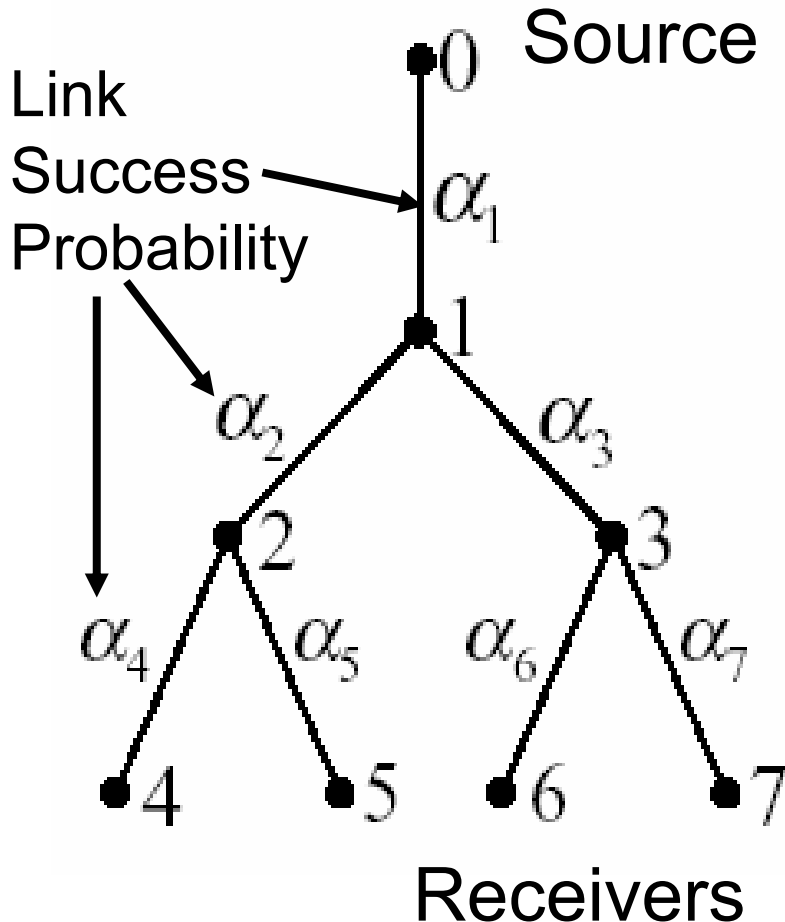
Logical Multicast Tree



- Bernoulli losses with probabilities α :
 - Temporal dependence \Rightarrow Slow convergence.
 - Spatial dependence \Rightarrow Error proportional to dependence.

Model

Logical Multicast Tree



- Ω = set of outcomes, i.e. subsets of receivers received a probe packet.
- n : number of probes.
- $n(\mathbf{x})$: # of probes with outcome $\mathbf{x} \in \Omega$.

Find α to maximize:

$$p(x^1, \dots, x^n; \alpha) = \prod_{x \in \Omega} p(x; \alpha)^{n(x)}$$

Solution Methodology

Compute α to maximize:

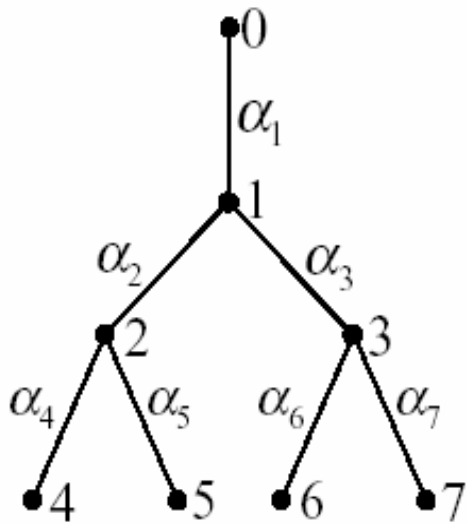
$$p(x^1, \dots, x^n; \alpha) = \prod_{x \in \Omega} p(x; \alpha)^{n(x)}$$

Using Maximum Likelihood Estimators.

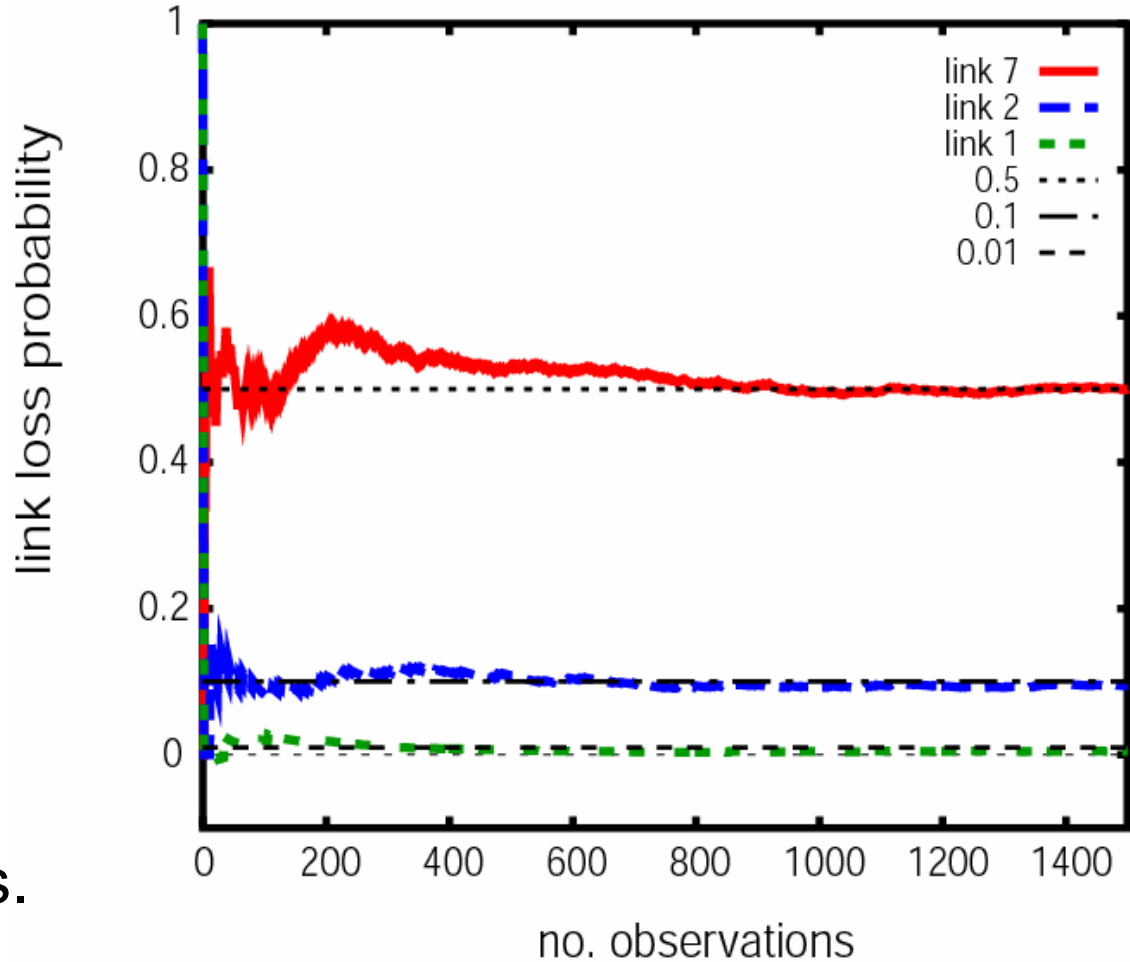
Properties:

- Strong consistency.
- Asymptotic normality.
- Asymptotic unbiasedness.
- Asymptotic efficiency.

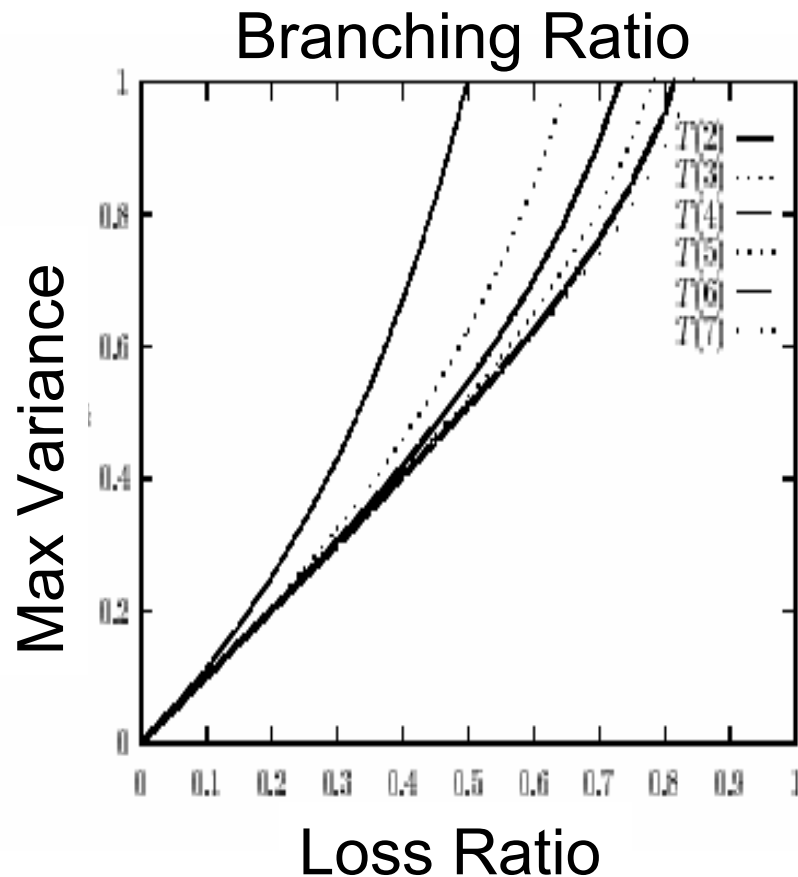
Convergence of Inferred Loss Probabilities



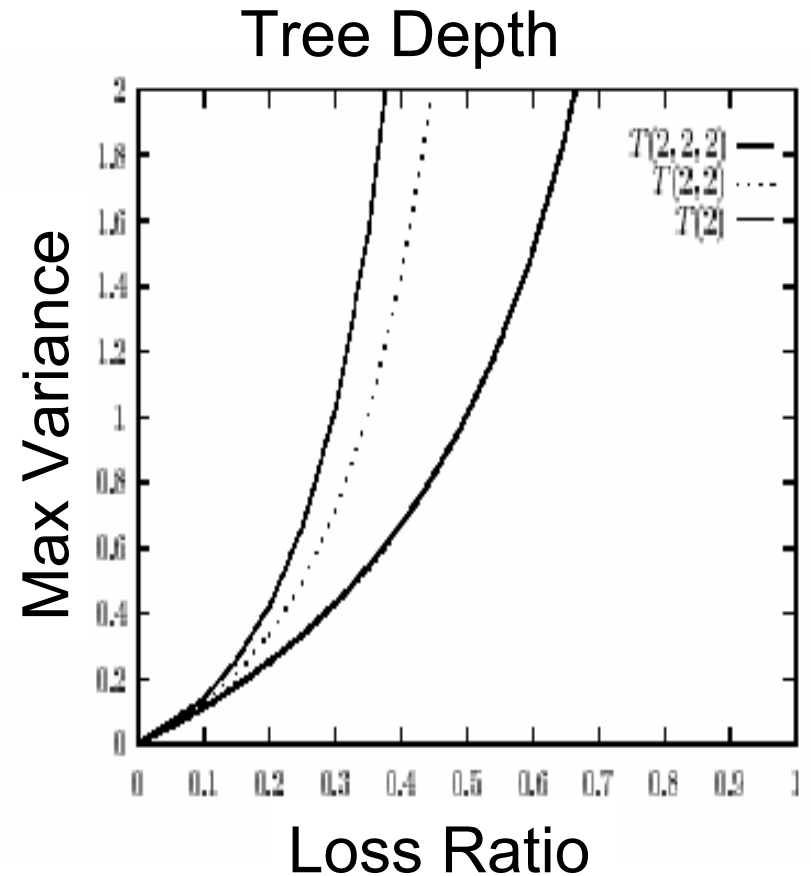
Error ≤ 0.001 after 2000 observations.



Effect of Topology



Variance *decreases* with branching ratio.



Variance *increases* with tree depth.

Outline

- Origin-Destination.

Source-Destination Traffic Estimation.

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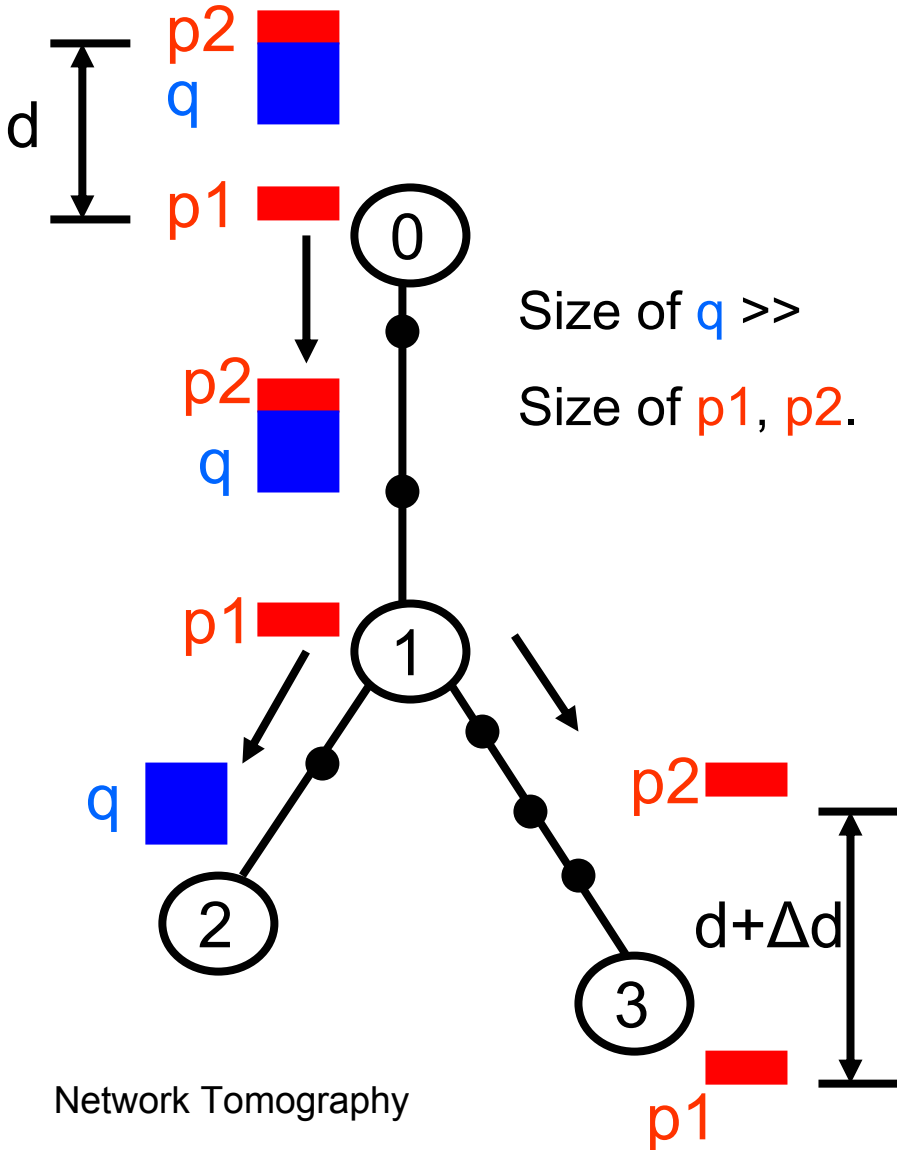
Topology Inference

- **Goal:** Identify the *tree* topology connecting a *single* server to *multiple* receivers.
- **Idea:**
 - Use a monotonic, increasing function of the number of *shared* links to two receivers, e.g. delay, loss, etc.
 - MLE for topology identification:

$$\mathcal{T}^* = \operatorname{argmax}_{\mathcal{T} \in \mathcal{F}} \max_{\gamma \in \mathcal{G}} [p(\mathbf{x} | \gamma, \mathcal{T})]$$

- **Other Approaches:** traceroute, AS map, mtrace, etc.
 - Topology inference more expensive.
 - But, works without router support.
 - “Can” identify **Layer-2** devices.

Sandwich Probe



Idea:

- Packet q introduces delay Δd between $p1$ and $p2$.
- $\Delta d \propto$ shared path $0 \rightarrow 1$.
- Node 3 measures Δd .

Advantages:

- Every measurement is important \Rightarrow Fast.
- No clock synchronization.

Measurement Collection

For each **ordered** pair of nodes (i,j):

- K measurements of delay difference:

$$\Delta d_{i,j}^k \text{ for } k = 1, \dots, K$$

- Compute sample mean and sample variance:

$$x_{i,j} = \frac{1}{K} \sum_{k=1}^K \Delta_{i,j}^k, \quad \sigma_{i,j}^2 = \frac{1}{n} \sum_{k=1}^K \left(\Delta_{i,j}^k - x_{i,j} \right)^2$$

- Asymptotically $x_{i,j}$ is Normal.

Maximum Likelihood Topology Identification.

Find \mathcal{T}^* :

$$\mathcal{T}^* = \operatorname{argmax}_{\mathcal{T} \in \mathcal{F}} [p(\mathbf{x}|\mathcal{T})]$$

Assume delay at link l of \mathcal{T} is μ_l . Maximize:

$$L(x, \mathcal{T}) \equiv \log p(x|\mathcal{T}, \hat{\mu}(\mathcal{T}))$$

Prior model:

$$x_{i,j} \sim \mathcal{N} \left(\sum_{l \in S_{i,j}} \mu_l, \sigma_{i,j}^2 \right)$$

Penalize trees with many links:

$$L_\lambda(x, \mathcal{T}) \equiv \log p(x|\mathcal{T}, \hat{\mu}(\mathcal{T})) - \lambda n(\mathcal{T})$$

with λ a user-defined parameter.

Finding the best tree

Optimize:

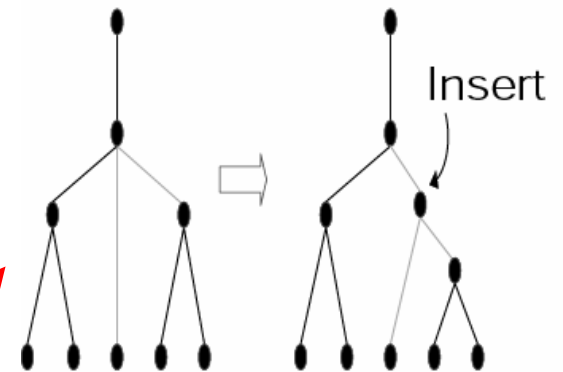
$$L_\lambda(x, \mathcal{T}) \equiv \log p(x|\mathcal{T}, \hat{\mu}(\mathcal{T})) - \lambda n(\mathcal{T})$$

Number of trees \mathcal{T} is HUGE.

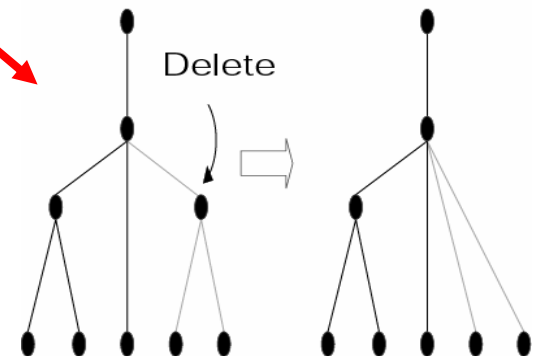
Instead of exhaustive search for \mathcal{T} , use a reversible jump Markov Chain Monte Carlo:

1. Start at state (\mathcal{T}_0, μ_0) .
2. Propose a move to a new state $(\mathcal{T}_i, \mu_{i+1})$.
3. Accept the proposal with probability proportional to the ratio of the likelihoods of the two states.
4. Continue and store for each state visited, its likelihood.

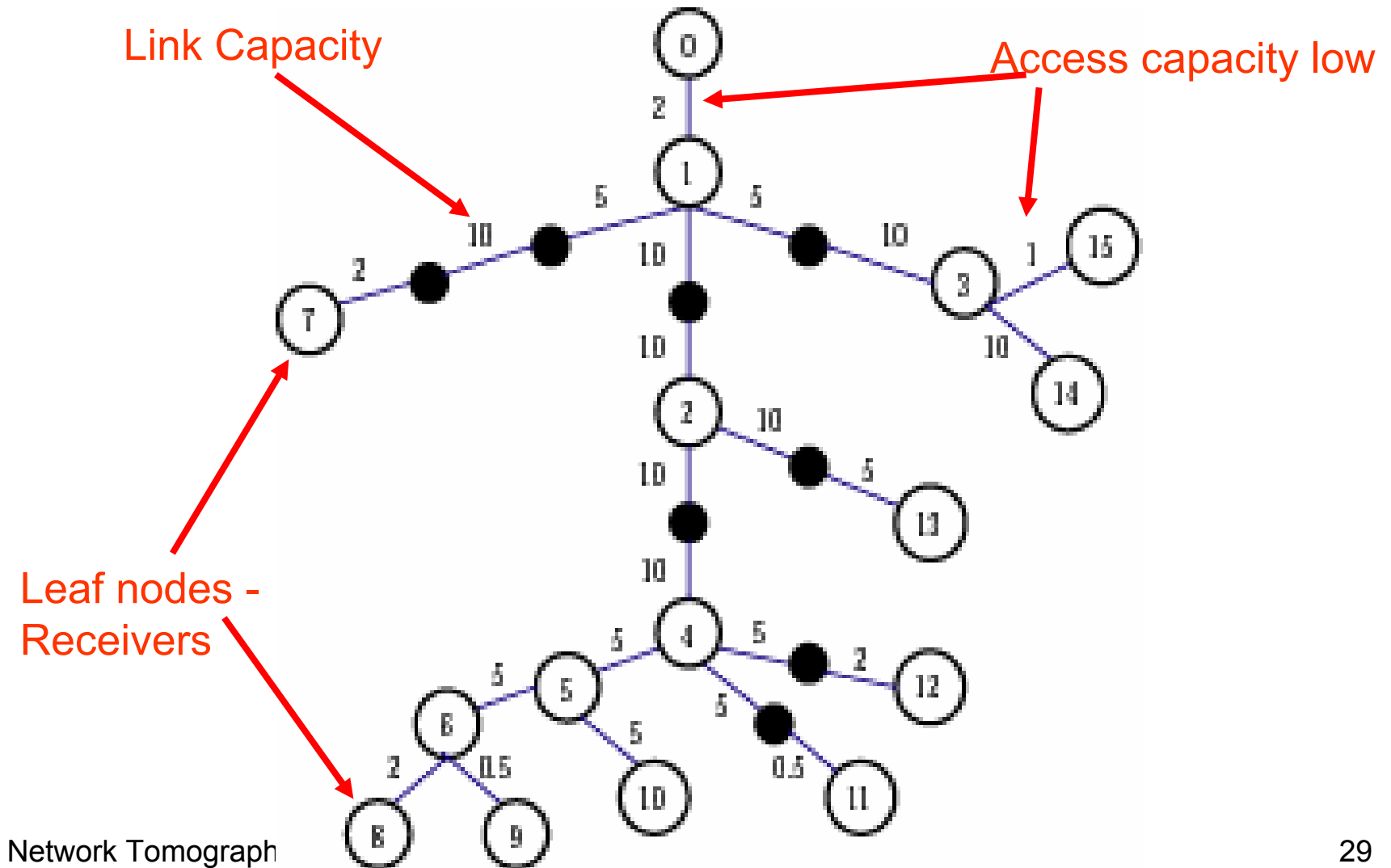
Birth Move



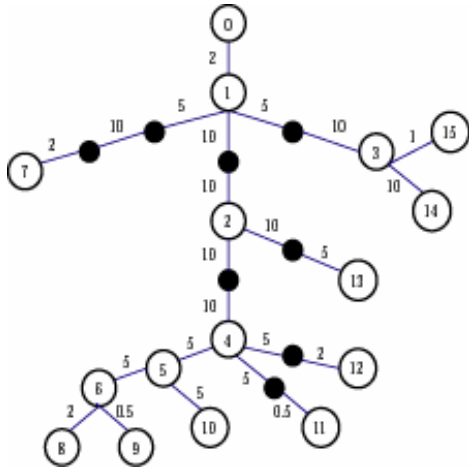
Death Move



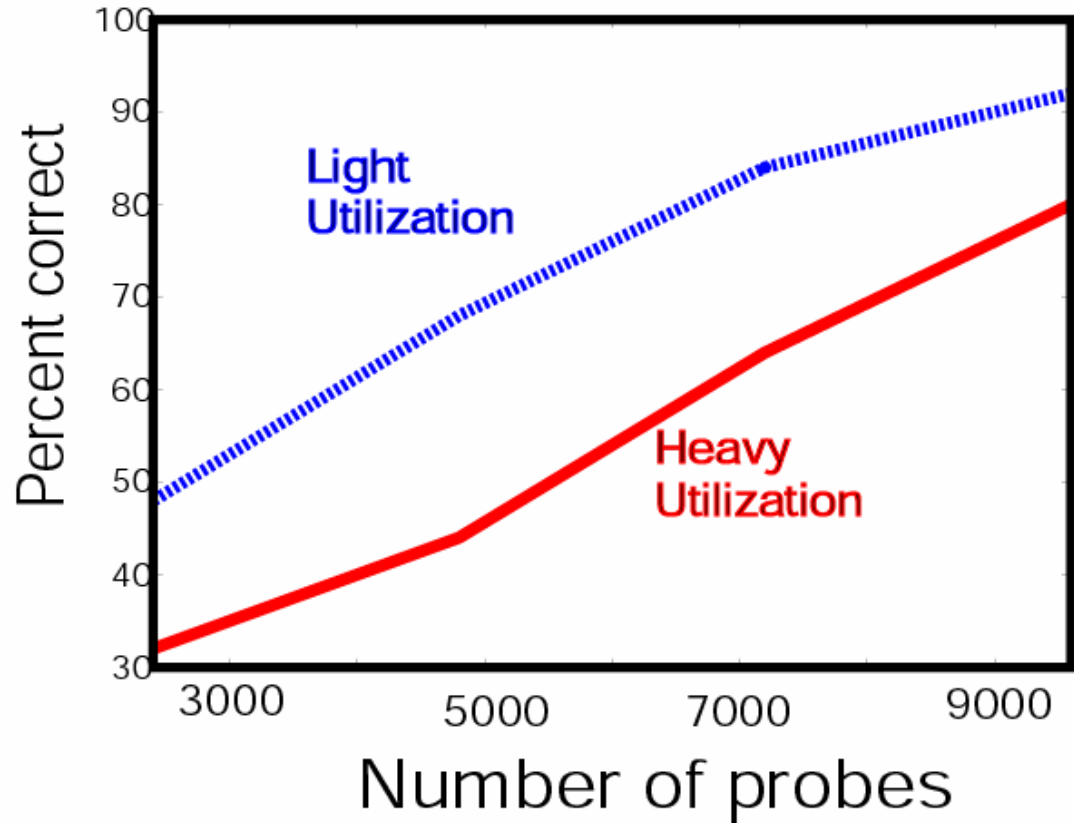
Topology Inference in ns-2



Topology Inference in ns-2

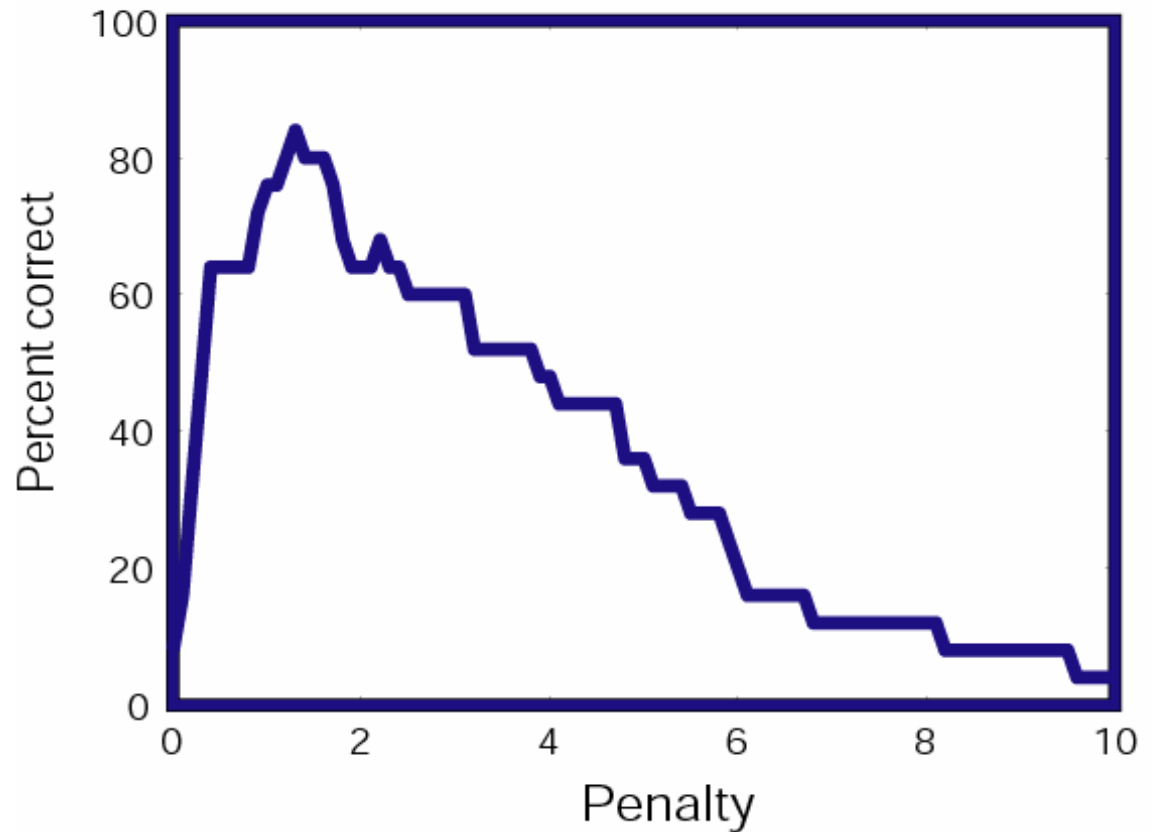
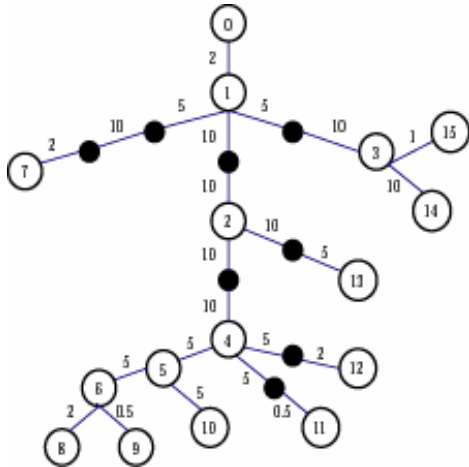


Effect of Number of Probes



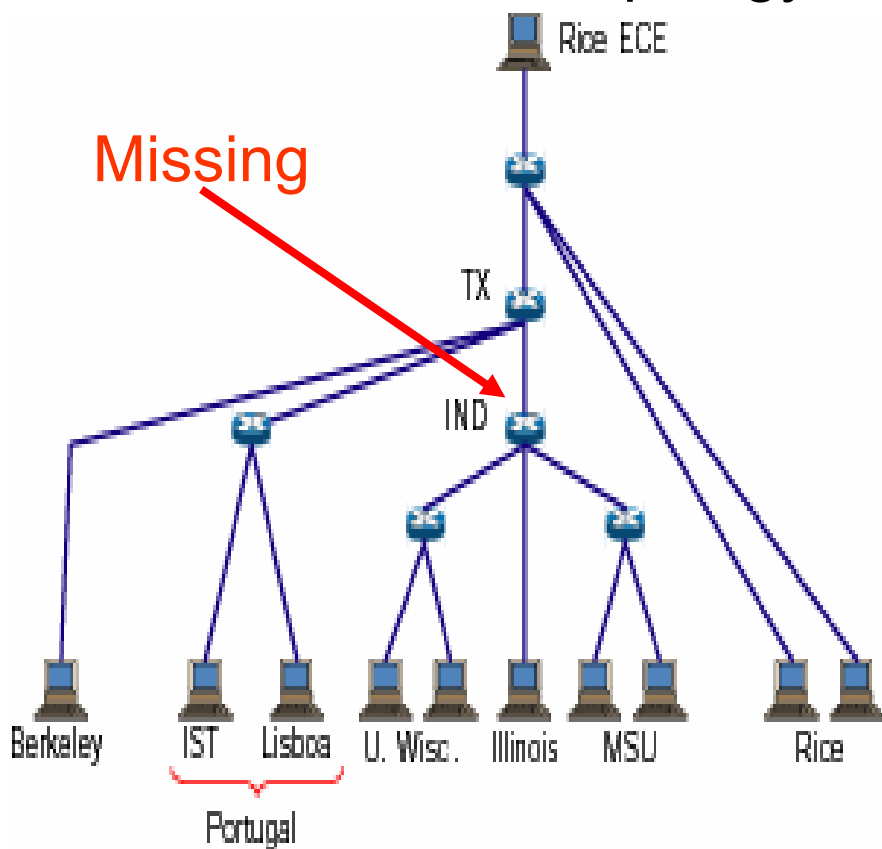
Topology Inference in ns-2

Effect of Penalty λ

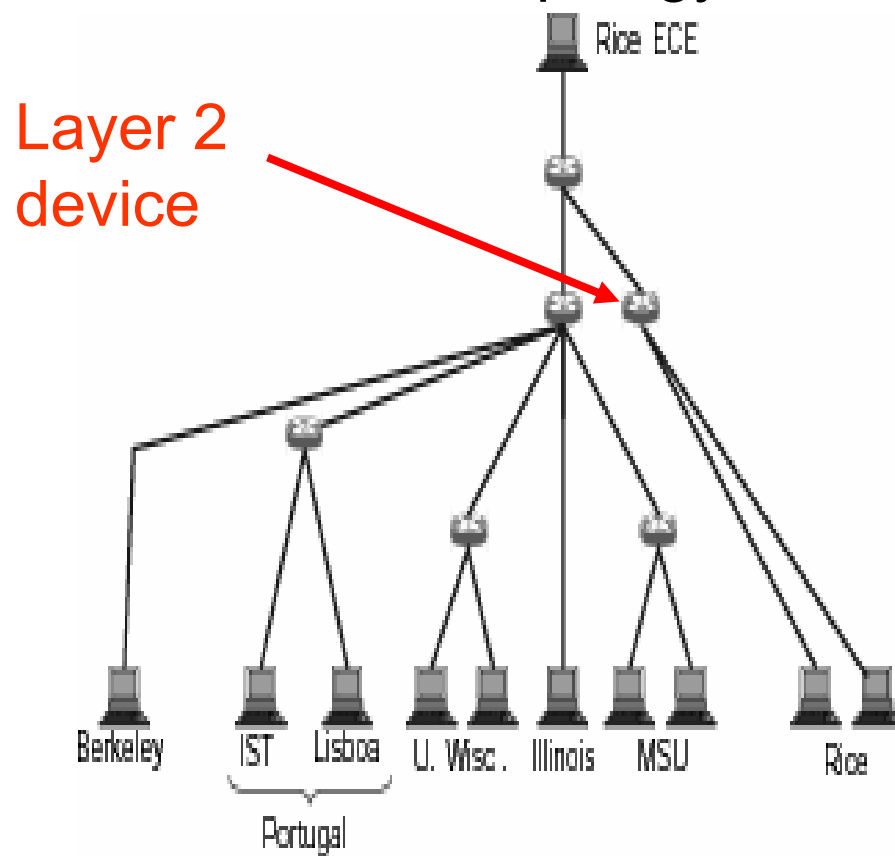


Topology Inference in the Internet

Traceroute Topology



Inferred Topology



Summary

- Areas of interest:
 - Origin-Destination Traffic Matrix.
 - Link-Level Network Inference.
 - Topology Inference.
- Pick solution with **highest likelihood** according to a predefined **model**.
- Numerically difficult problems.
- Standard tools: MLE, Bayesian Inference, EM, MCMC.

Future Work

- Spatial and temporal dependencies.
- Time-varying, non-stationary OD traffic matrices.
- Traffic models with long range dependencies.
- Identification of anomalous behavior, instead of detailed statistics.
- Better passive traffic monitoring.