

Convolutional Neural Networks

Computer Vision

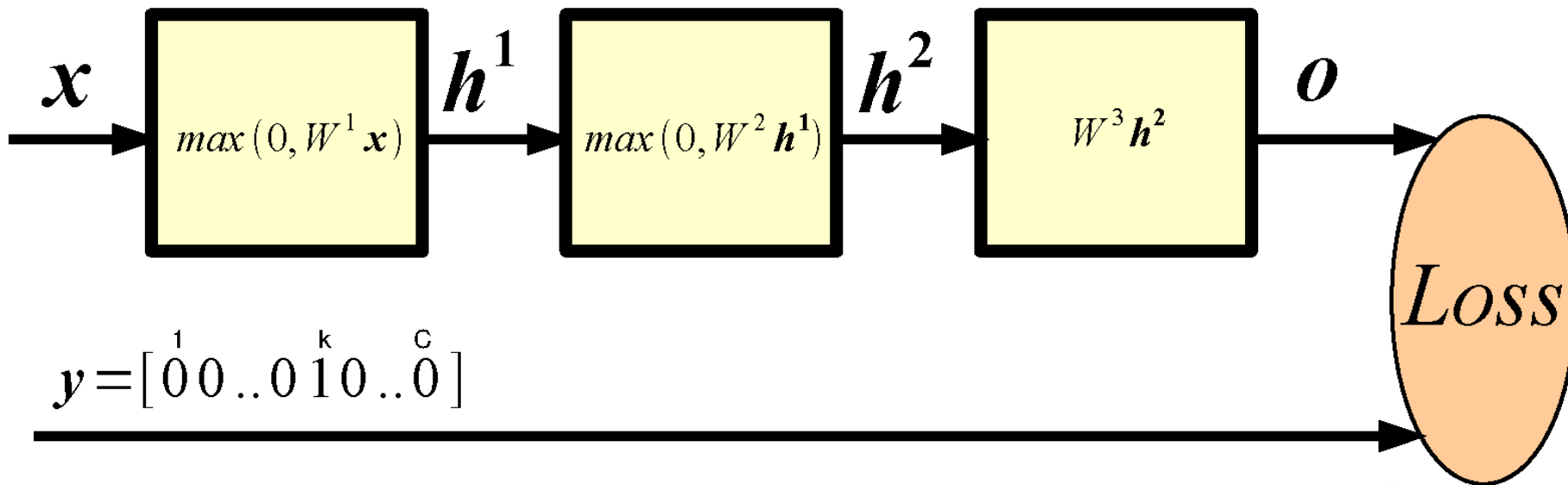
James Hays

Many slides by Marc'Aurelio Ranzato

Outline

- Neural Networks (covered in previous lecture)
- *Convolutional* Neural Networks
- Visualization and interpretation of Deep Networks

How Good is a Network?



Probability of class k given input (softmax):

$$p(c_k = 1 | \mathbf{x}) = \frac{e^{o_k}}{\sum_{j=1}^C e^{o_j}}$$

(Per-sample) **Loss**; e.g., negative log-likelihood (good for classification of small number of classes):

$$L(\mathbf{x}, \mathbf{y}; \boldsymbol{\theta}) = - \sum_j y_j \log p(c_j | \mathbf{x})$$

Training

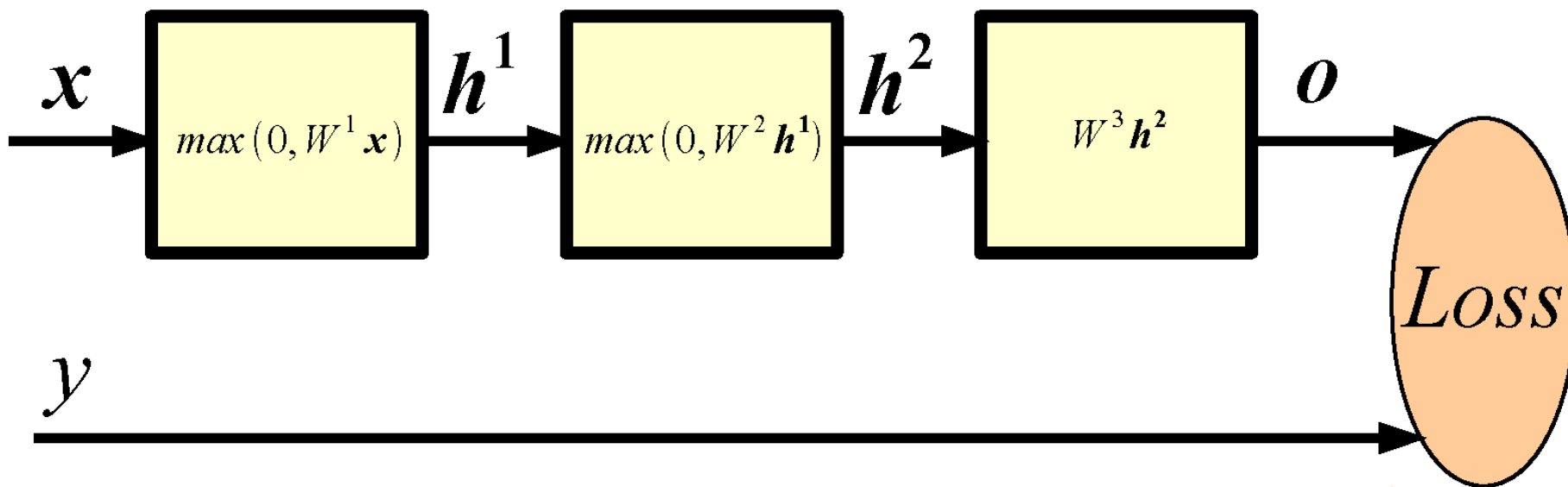
Learning consists of minimizing the loss (plus some regularization term) w.r.t. parameters over the whole training set.

$$\boldsymbol{\theta}^* = \mathit{arg\ min}_{\boldsymbol{\theta}} \sum_{n=1}^P L(\mathbf{x}^n, y^n; \boldsymbol{\theta})$$

Question: How to minimize a complicated function of the parameters?

Answer: Chain rule, a.k.a. **Backpropagation!** That is the procedure to compute gradients of the loss w.r.t. parameters in a multi-layer neural network.

Key Idea: Wiggle To Decrease Loss



Let's say we want to decrease the loss by adjusting $W_{i,j}^1$
We could consider a very small $\epsilon = 1e-6$ and compute:

$$L(\mathbf{x}, y; \boldsymbol{\theta})$$

$$L(\mathbf{x}, y; \boldsymbol{\theta} \setminus W_{i,j}^1, W_{i,j}^1 + \epsilon)$$

Then, update:

$$W_{i,j}^1 \leftarrow W_{i,j}^1 + \epsilon \operatorname{sgn}(L(\mathbf{x}, y; \boldsymbol{\theta}) - L(\mathbf{x}, y; \boldsymbol{\theta} \setminus W_{i,j}^1, W_{i,j}^1 + \epsilon))$$

Derivative w.r.t. Input of Softmax

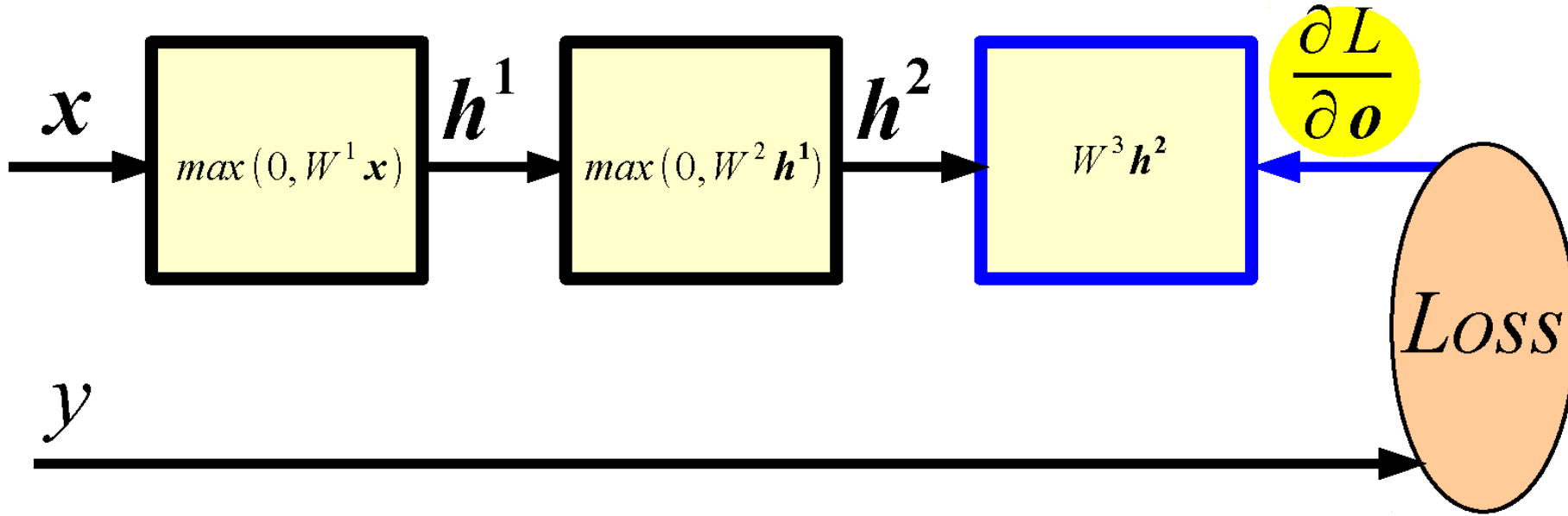
$$p(c_k = 1 | \mathbf{x}) = \frac{e^{o_k}}{\sum_j e^{o_j}}$$

$$L(\mathbf{x}, \mathbf{y}; \boldsymbol{\theta}) = - \sum_j y_j \log p(c_j | \mathbf{x}) \quad \mathbf{y} = [0 \overset{1}{0} \dots 0 \overset{k}{1} 0 \dots 0 \overset{c}{0}]$$

By substituting the first formula in the second, and taking the derivative w.r.t. \boldsymbol{o} we get:

$$\frac{\partial L}{\partial \boldsymbol{o}} = p(c | \mathbf{x}) - \mathbf{y}$$

Backward Propagation

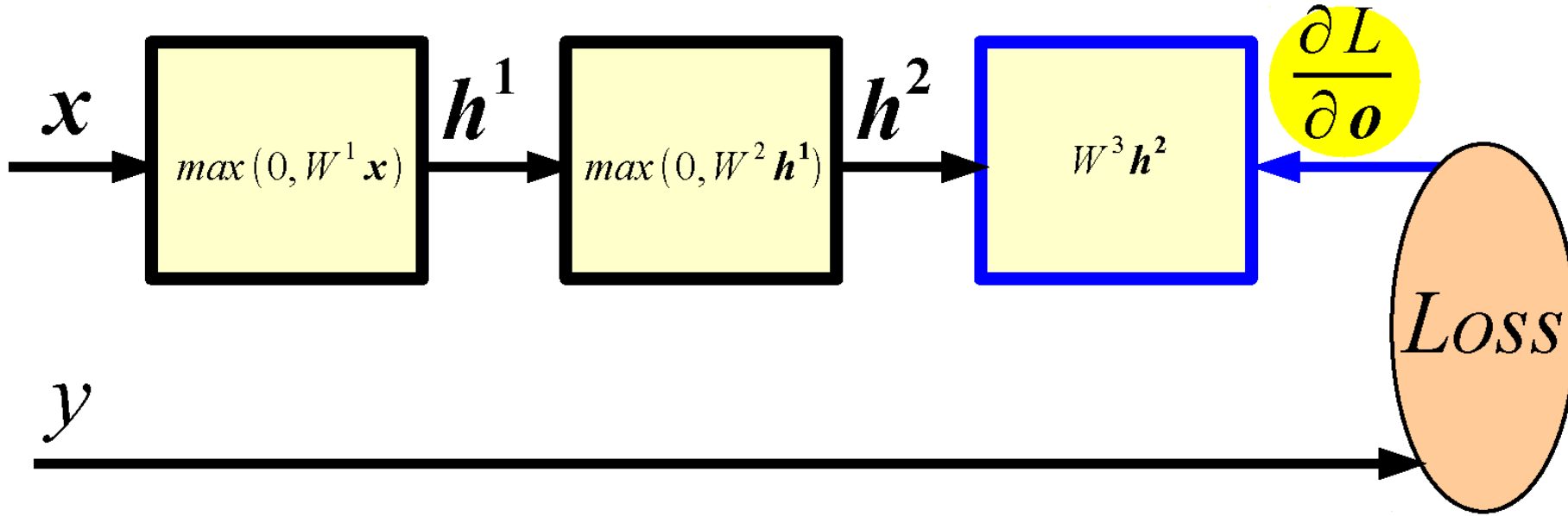


Given $\frac{\partial L}{\partial \mathbf{o}}$ and assuming we can easily compute the Jacobian of each module, we have:

$$\frac{\partial L}{\partial W^3} = \frac{\partial L}{\partial \mathbf{o}} \frac{\partial \mathbf{o}}{\partial W^3}$$

$$\frac{\partial L}{\partial \mathbf{h}^2} = \frac{\partial L}{\partial \mathbf{o}} \frac{\partial \mathbf{o}}{\partial \mathbf{h}^2}$$

Backward Propagation



Given $\frac{\partial L}{\partial o}$ and assuming we can easily compute the Jacobian of each module, we have:

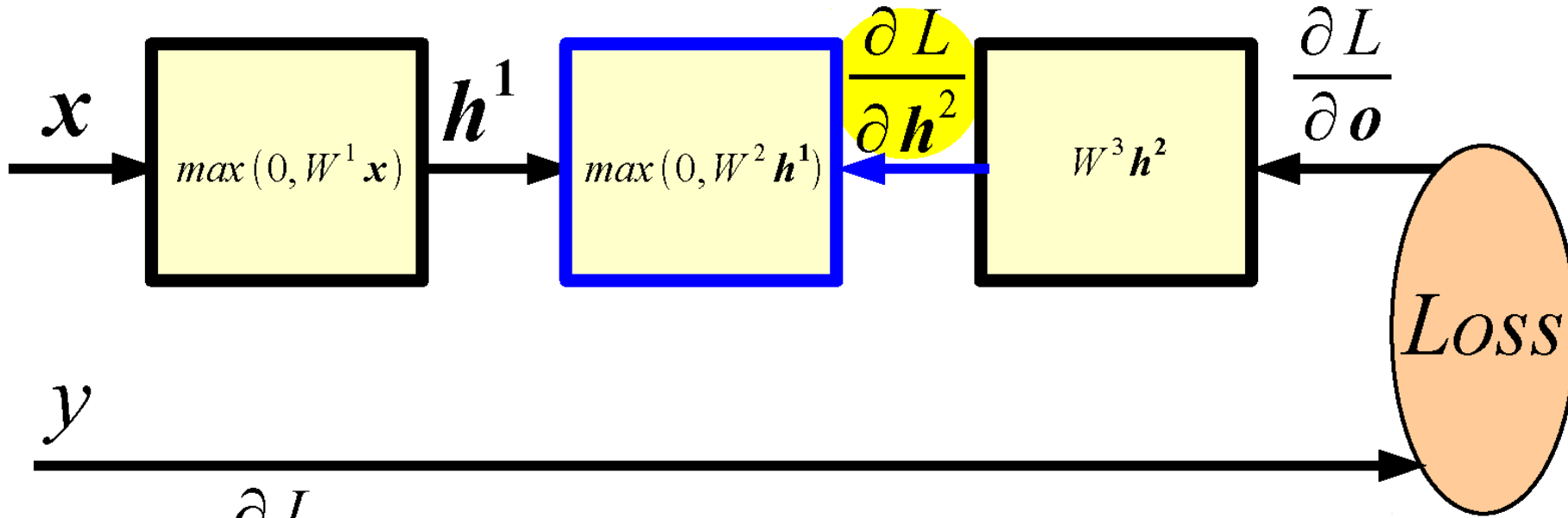
$$\frac{\partial L}{\partial W^3} = \frac{\partial L}{\partial o} \frac{\partial o}{\partial W^3}$$

$$\frac{\partial L}{\partial h^2} = \frac{\partial L}{\partial o} \frac{\partial o}{\partial h^2}$$

$$\frac{\partial L}{\partial W^3} = (p(c|x) - y) h^{2T}$$

$$\frac{\partial L}{\partial h^2} = W^{3T} (p(c|x) - y)_{23}$$

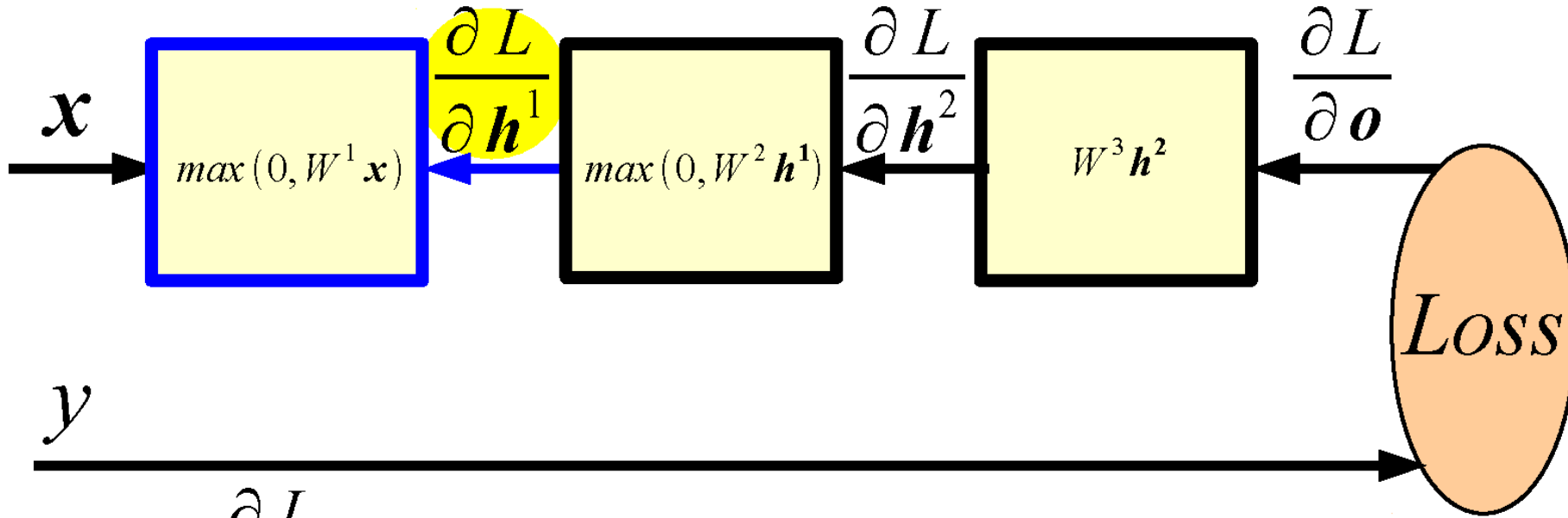
Backward Propagation



Given $\frac{\partial L}{\partial \mathbf{h}^2}$ we can compute now:

$$\frac{\partial L}{\partial W^2} = \frac{\partial L}{\partial \mathbf{h}^2} \frac{\partial \mathbf{h}^2}{\partial W^2} \quad \frac{\partial L}{\partial \mathbf{h}^1} = \frac{\partial L}{\partial \mathbf{h}^2} \frac{\partial \mathbf{h}^2}{\partial \mathbf{h}^1}$$

Backward Propagation



Given $\frac{\partial L}{\partial h^1}$ we can compute now:

$$\frac{\partial L}{\partial W^1} = \frac{\partial L}{\partial h^1} \frac{\partial h^1}{\partial W^1}$$

This all seems pretty complicated. Why are we using Neural Networks? James's rough assessment:

Learning method	Ease of configuration
Neural Network	1
Nearest Neighbor	10
Linear SVM	10
Non-linear SVM	5
Decision Tree or Random Forest	4

This all seems pretty complicated. Why are we using Neural Networks? James's rough assessment:

Learning method	Ease of configuration	Ease of interpretation
Neural Network	1	1
Nearest Neighbor	10	10
Linear SVM	10	9
Non-linear SVM	5	4
Decision Tree or Random Forest	4	4

This all seems pretty complicated. Why are we using Neural Networks? James's rough assessment:

Learning method	Ease of configuration	Ease of interpretation	Speed / memory when training
Neural Network	1	1	1
Nearest Neighbor	10	10	8
Linear SVM	10	9	10
Non-linear SVM	5	4	2
Decision Tree or Random Forest	4	4	4

This all seems pretty complicated. Why are we using Neural Networks? James's rough assessment:

Learning method	Ease of configuration	Ease of interpretation	Speed / memory when training	Speed / memory at test time
Neural Network	1	1	1	6
Nearest Neighbor	10	10	8	4
Linear SVM	10	9	10	10
Non-linear SVM	5	4	2	2
Decision Tree or Random Forest	4	4	4	8

This all seems pretty complicated. Why are we using Neural Networks? James's rough assessment:

Learning method	Ease of configuration	Ease of interpretation	Speed / memory when training	Speed / memory at test time	Accuracy w/ lots of data
Neural Network	1	1	1	6	10
Nearest Neighbor	10	10	8	4	7
Linear SVM	10	9	10	10	5
Non-linear SVM	5	4	2	2	8
Decision Tree or Random Forest	4	4	4	8	7

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Neural Network	1	1	1	6	10
Nearest Neighbor	10	10	8	4	7
Linear SVM	10				
Non-linear SVM	5				
Decision Tree or Random Forest	4				

Representation design matters more for all of these

Outline

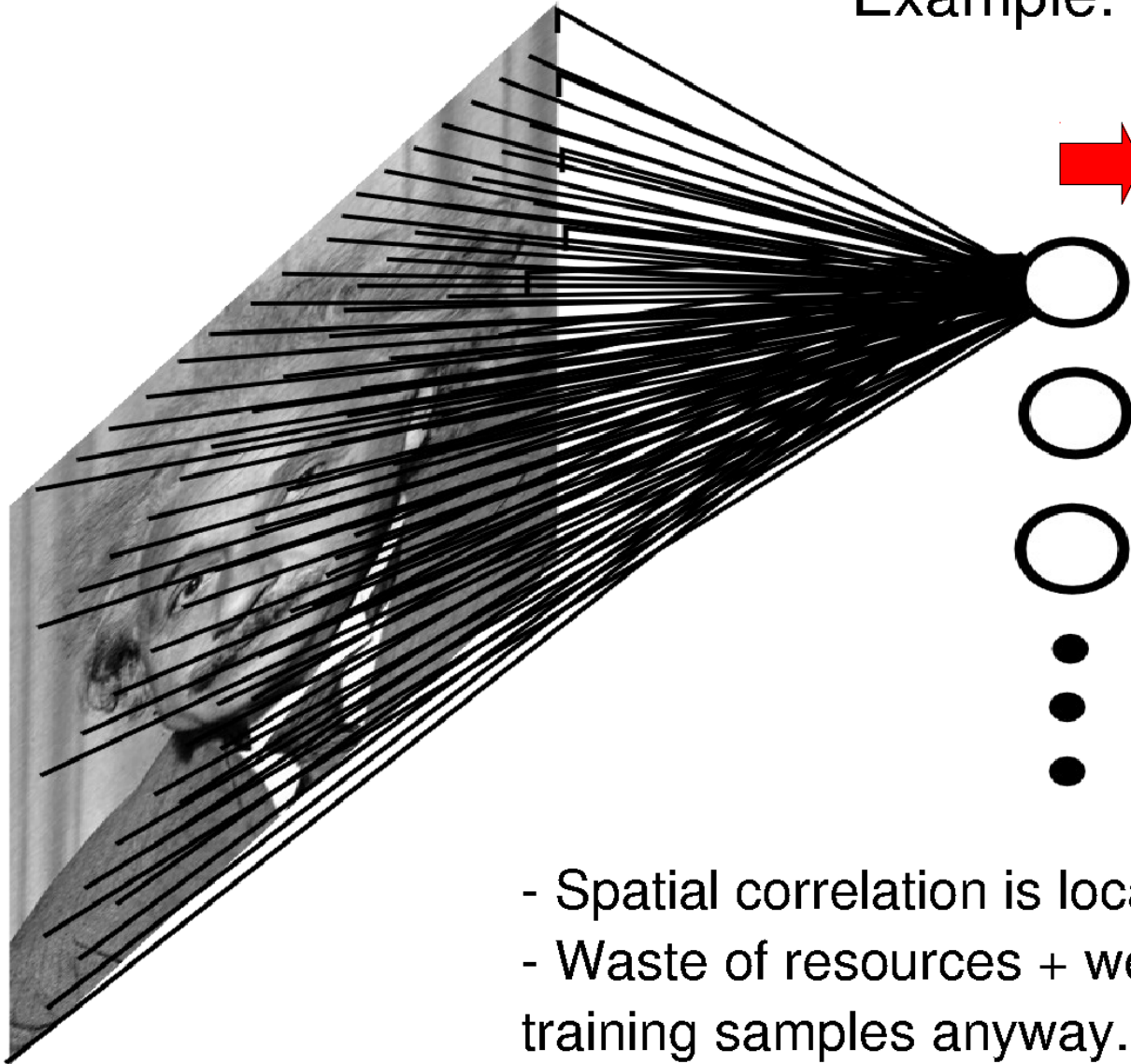
- Supervised Neural Networks
- Convolutional Neural Networks
- Examples
- Tips

Fully Connected Layer

Example: 200x200 image

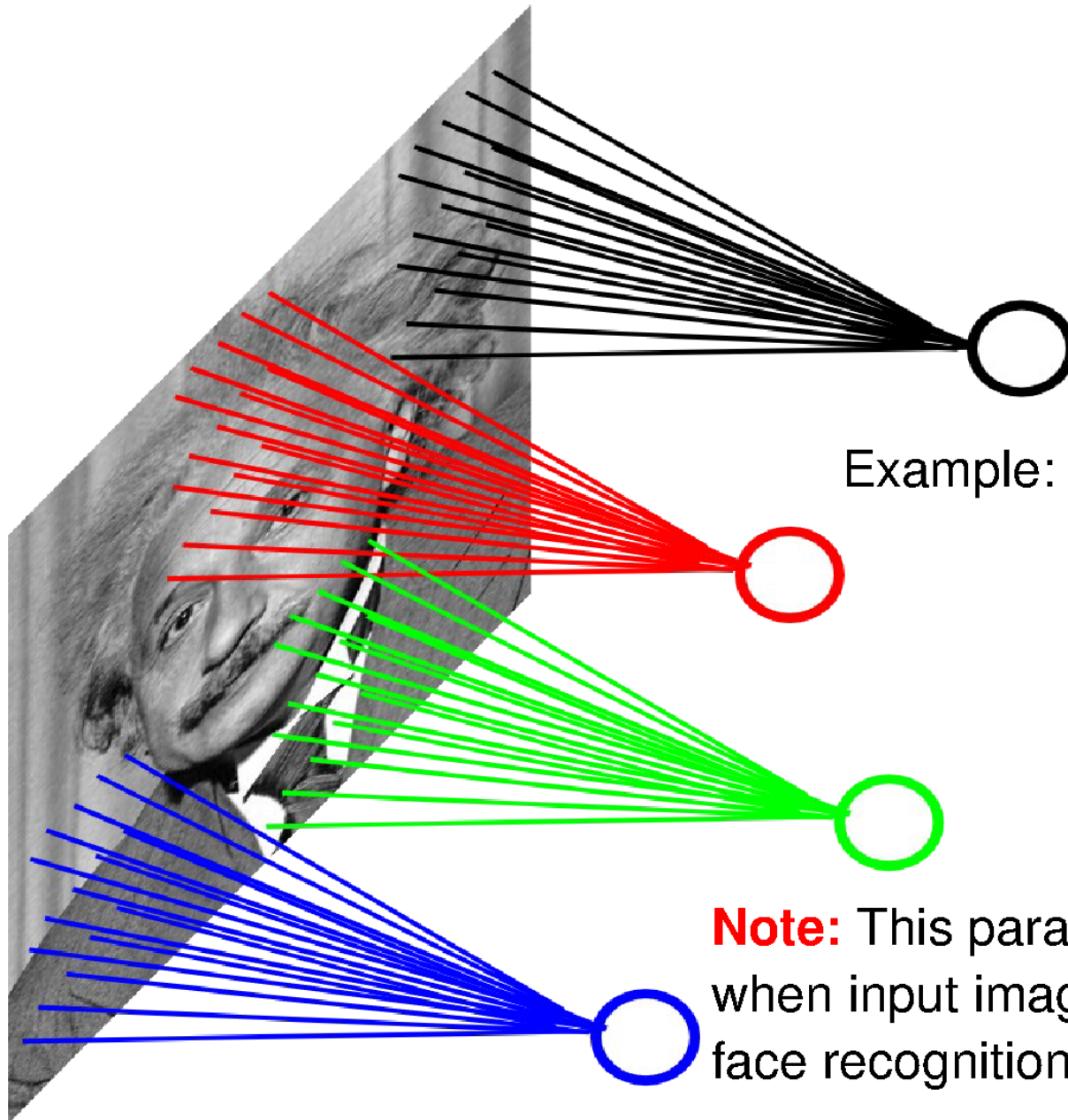
40K hidden units

➔ **~2B parameters!!!**



- Spatial correlation is local
- Waste of resources + we have not enough training samples anyway..

Locally Connected Layer

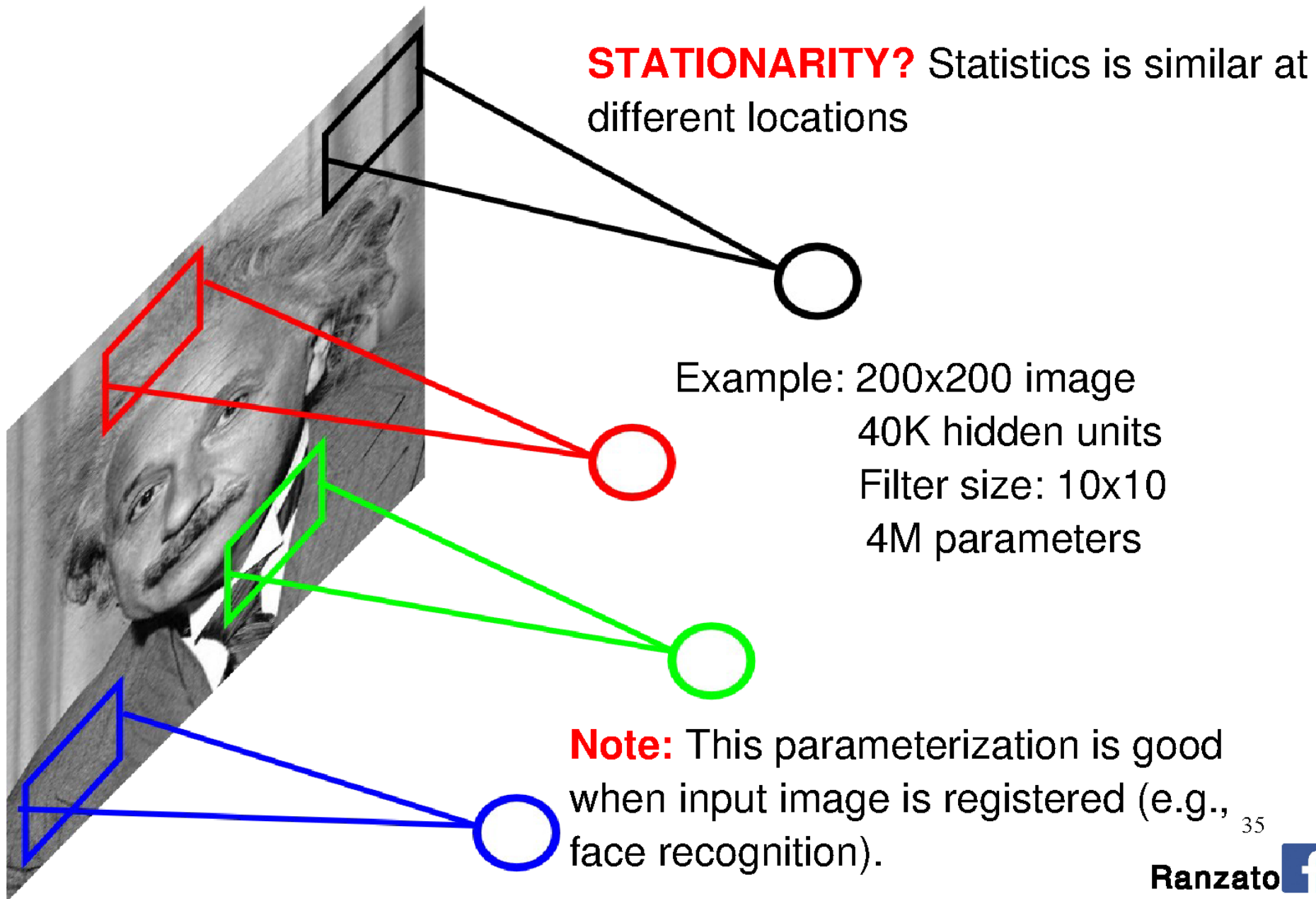


Example: 200x200 image
40K hidden units
Filter size: 10x10
4M parameters

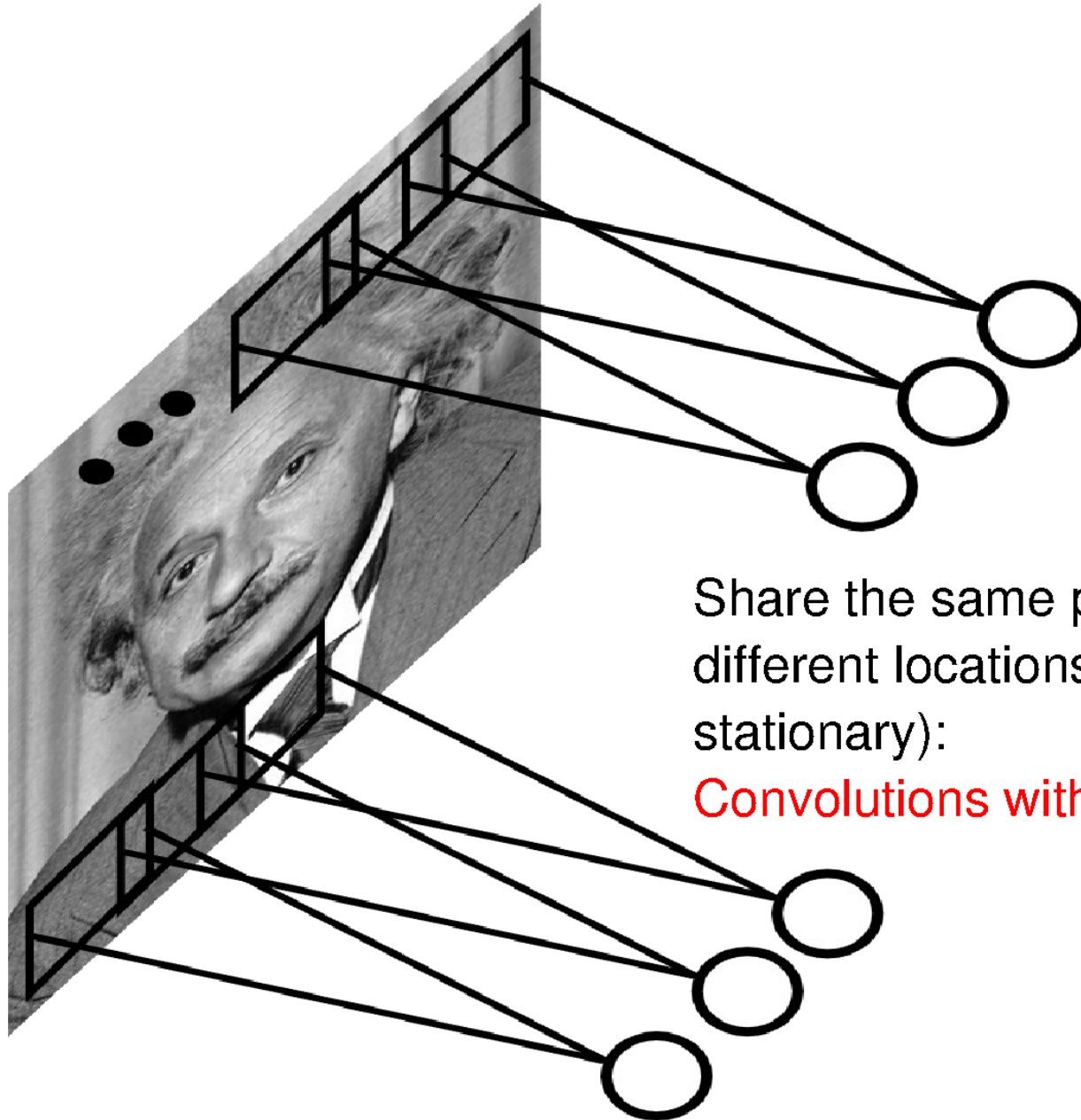
Note: This parameterization is good when input image is registered (e.g., face recognition).

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Locally Connected Layer



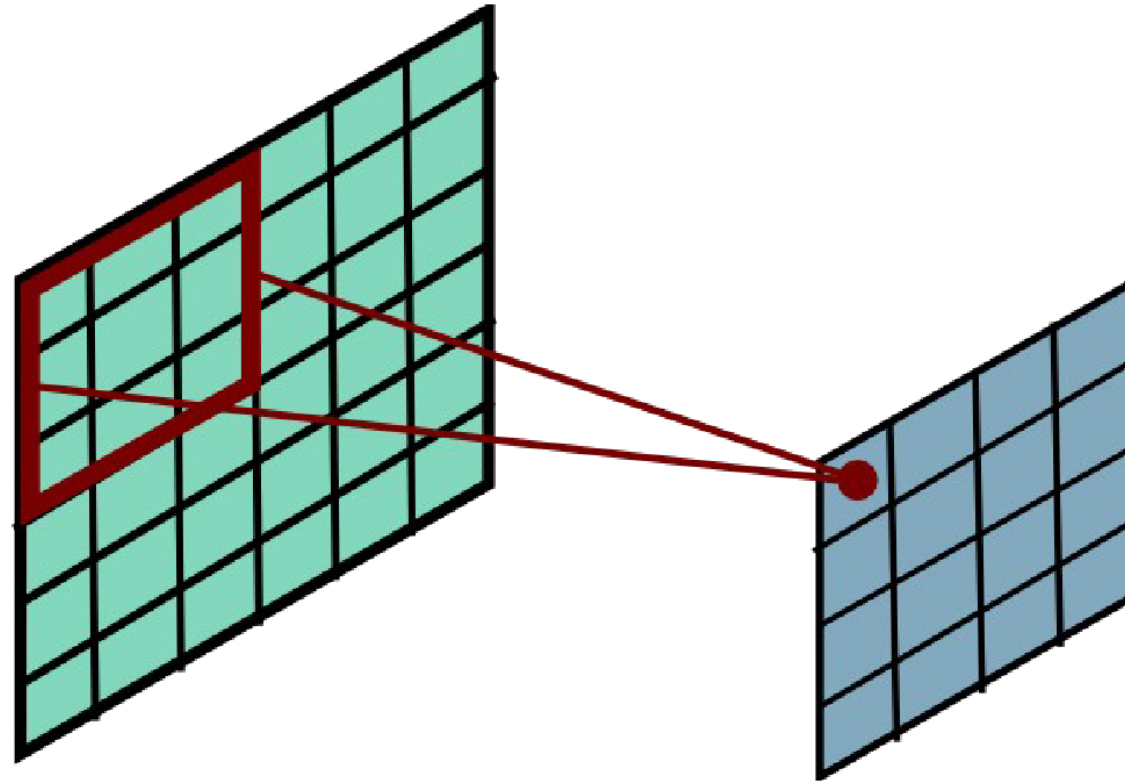
Convolutional Layer



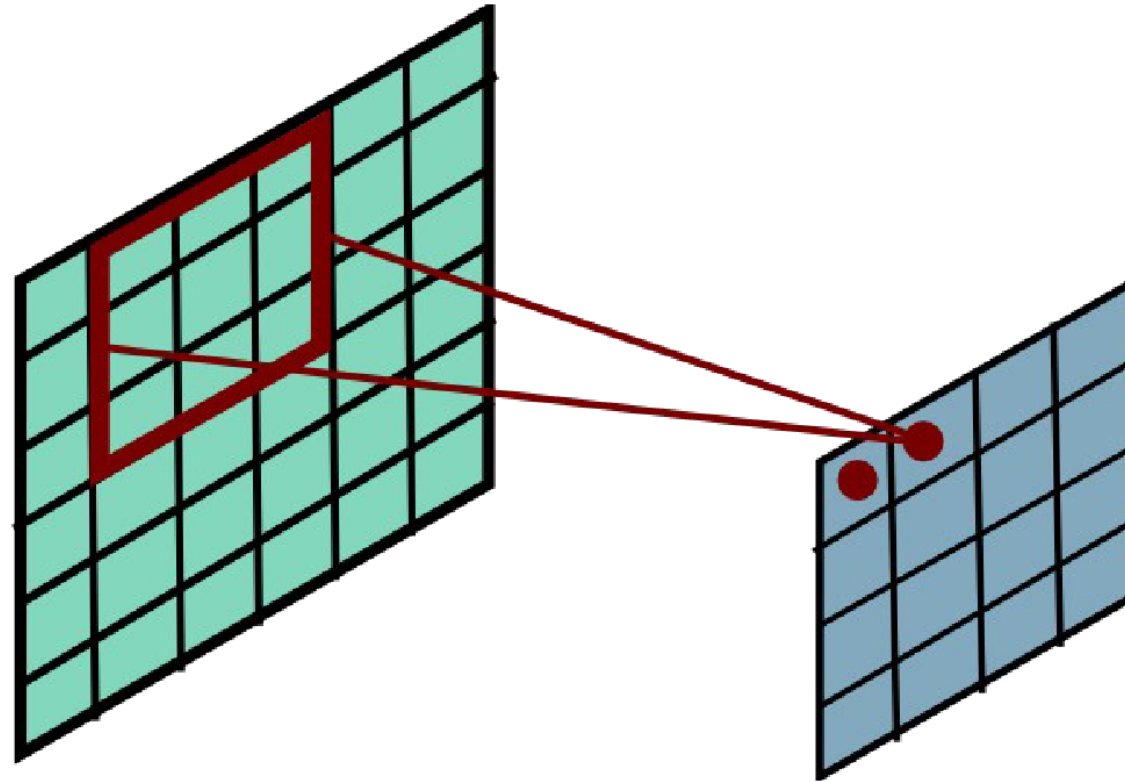
Share the same parameters across different locations (assuming input is stationary):

Convolutions with learned kernels

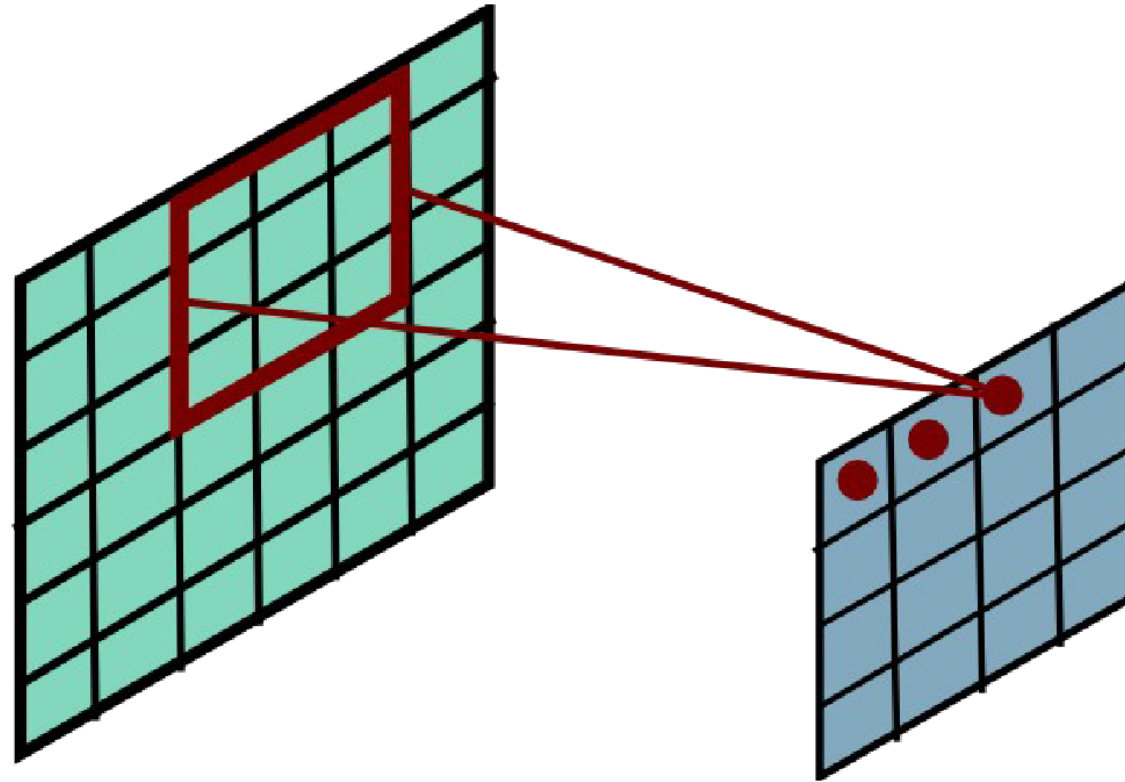
Convolutional Layer



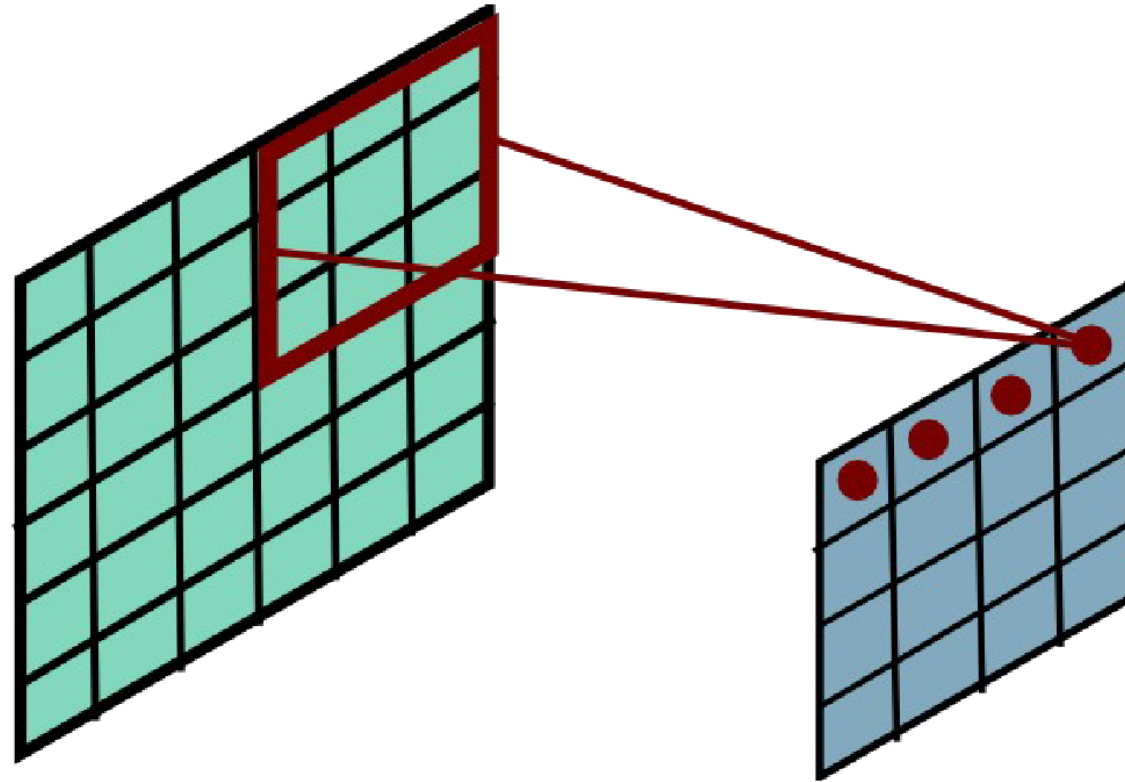
Convolutional Layer



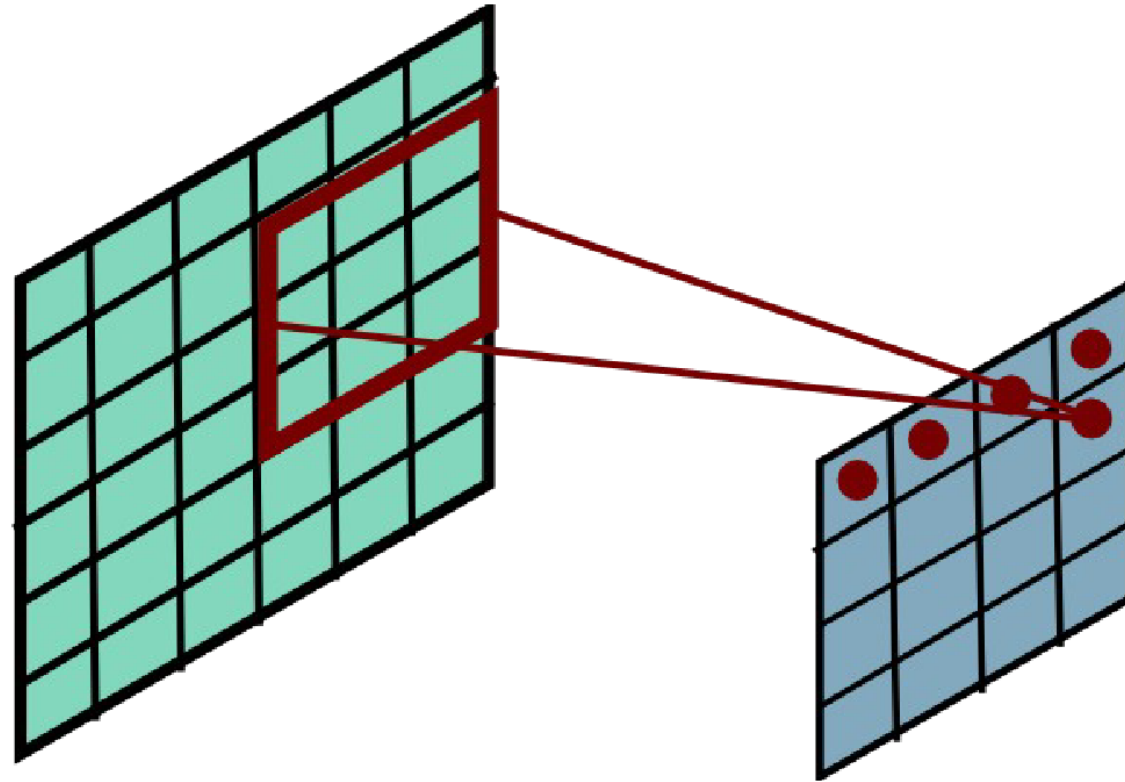
Convolutional Layer



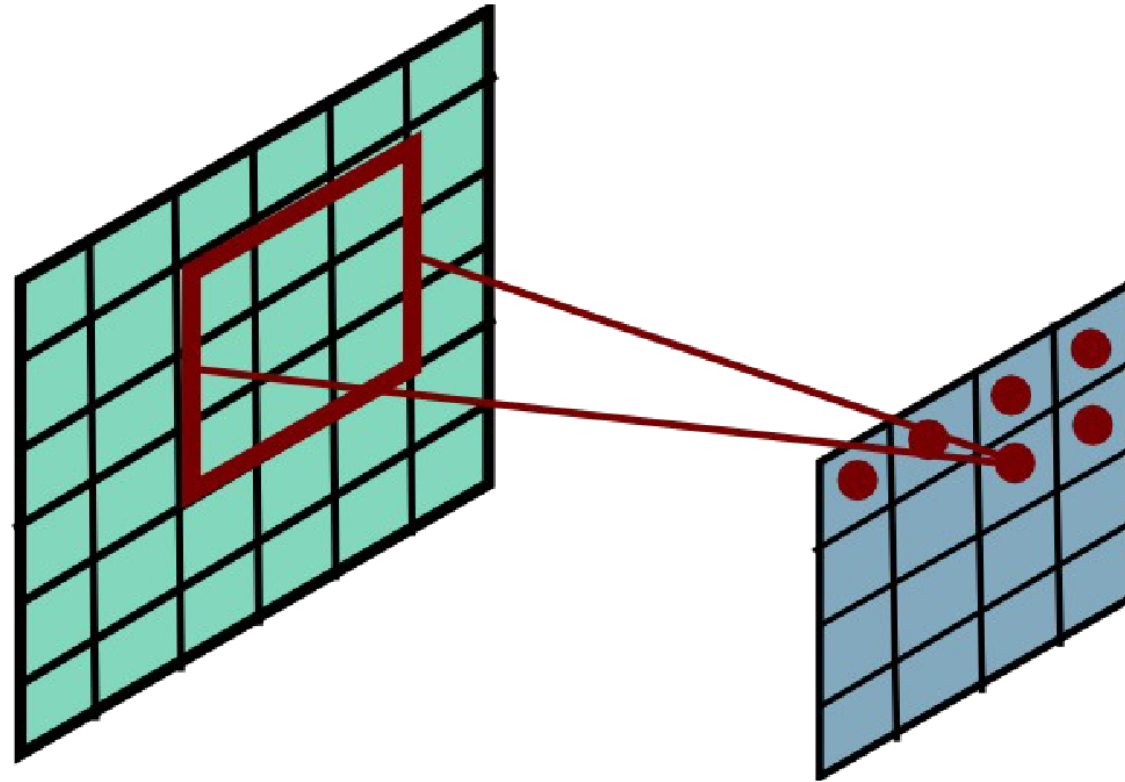
Convolutional Layer



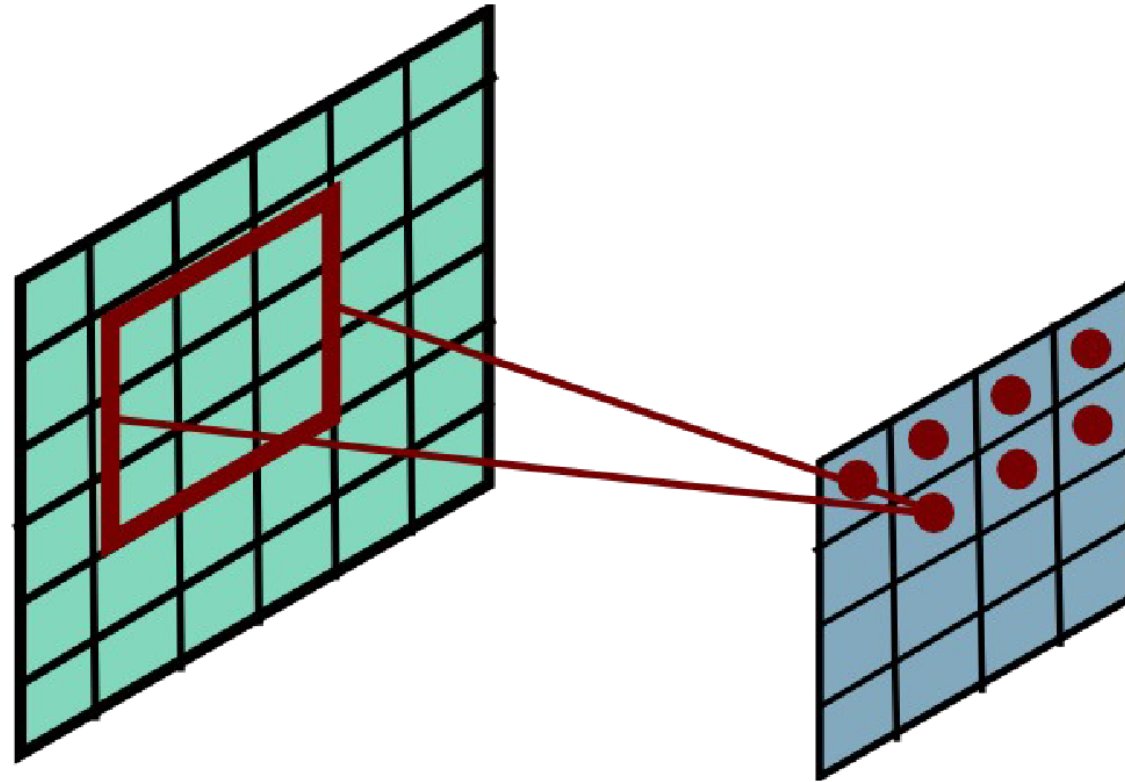
Convolutional Layer



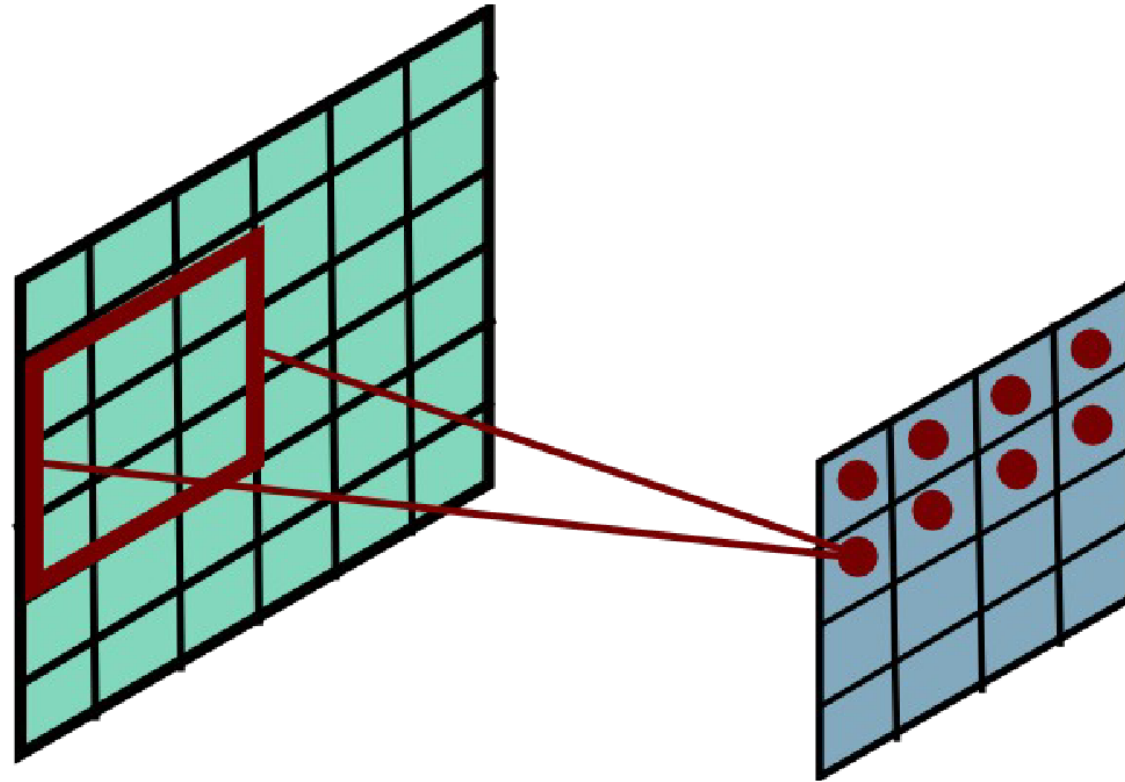
Convolutional Layer



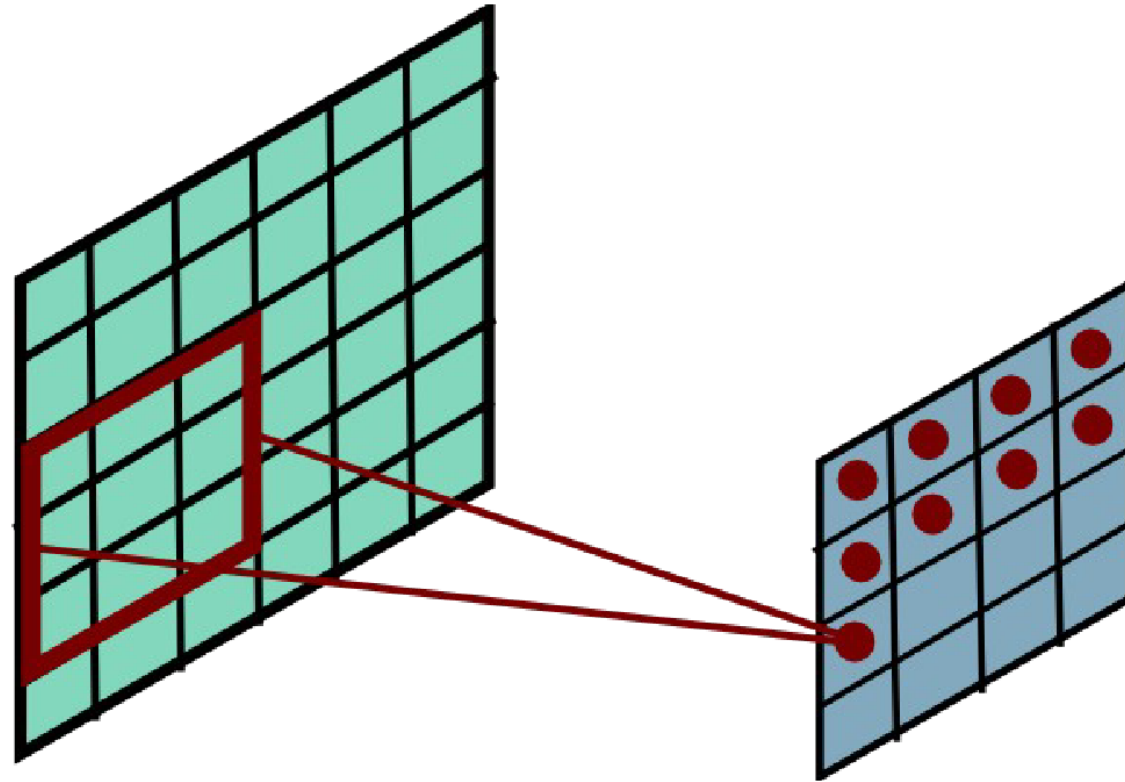
Convolutional Layer



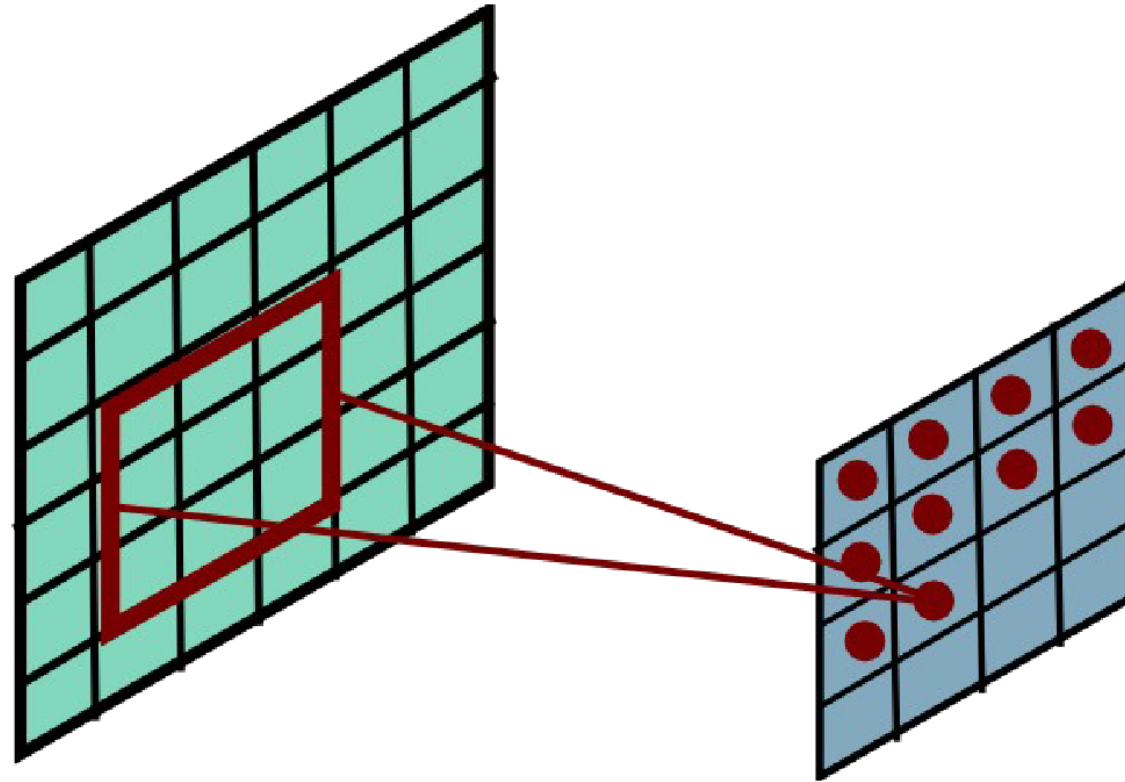
Convolutional Layer



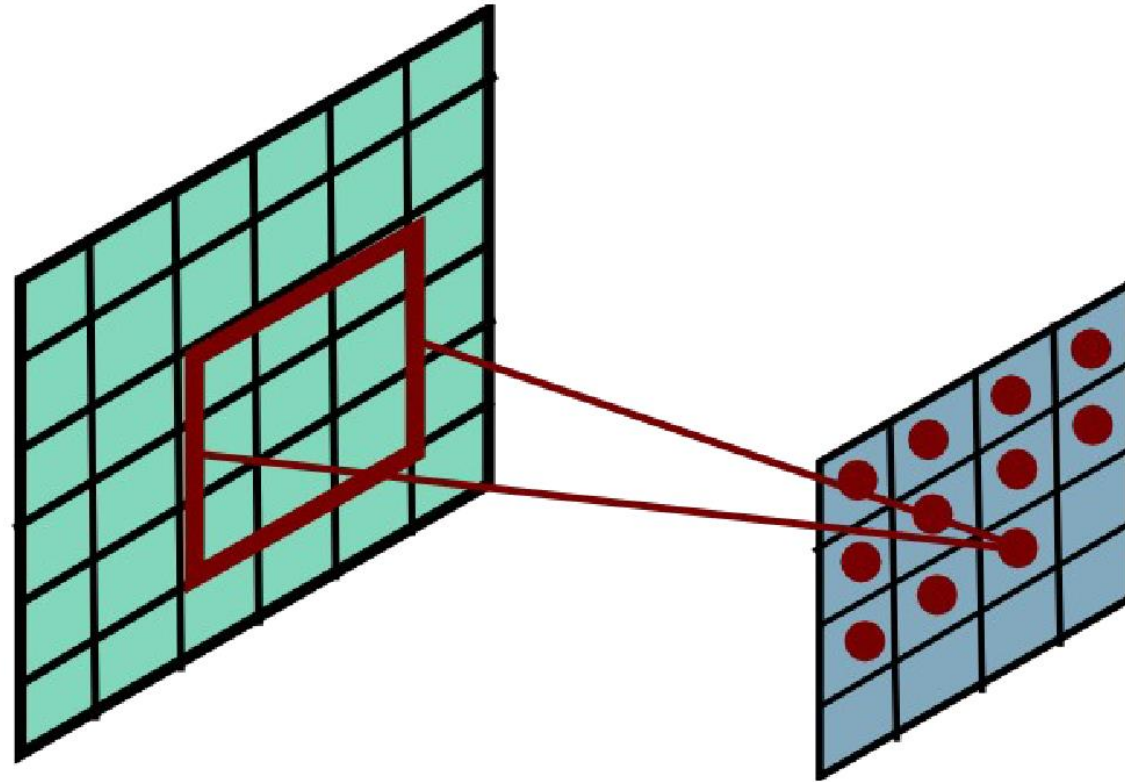
Convolutional Layer



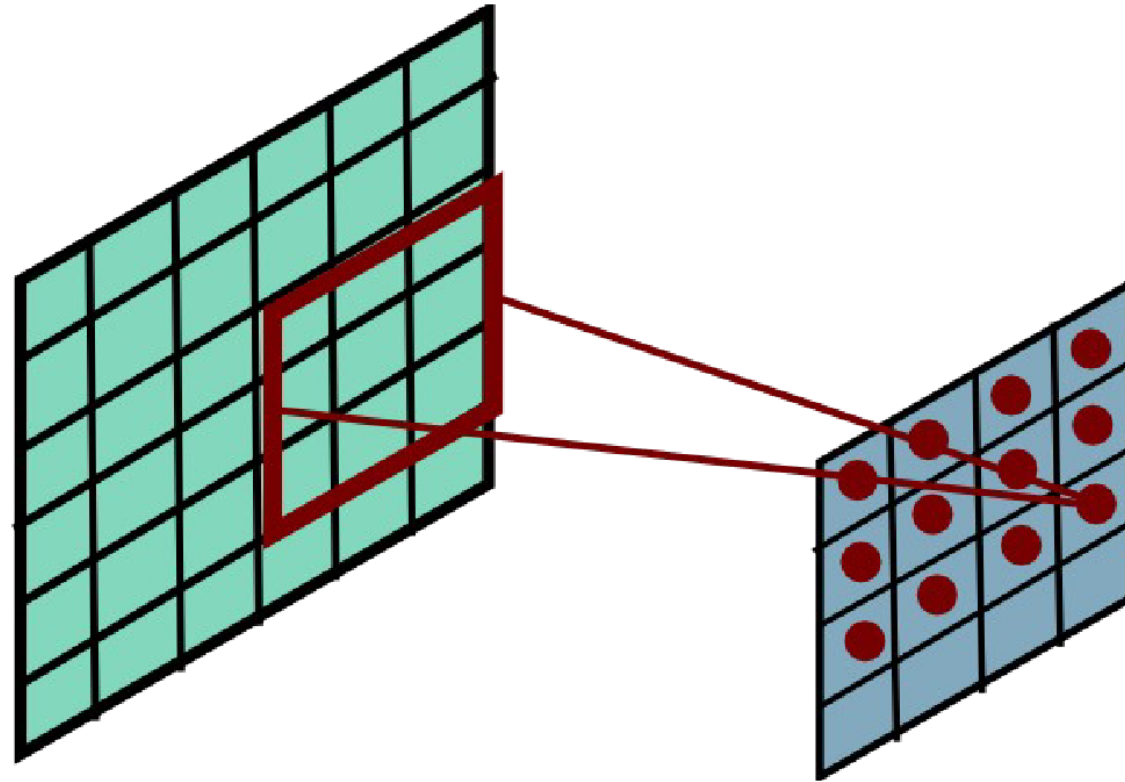
Convolutional Layer



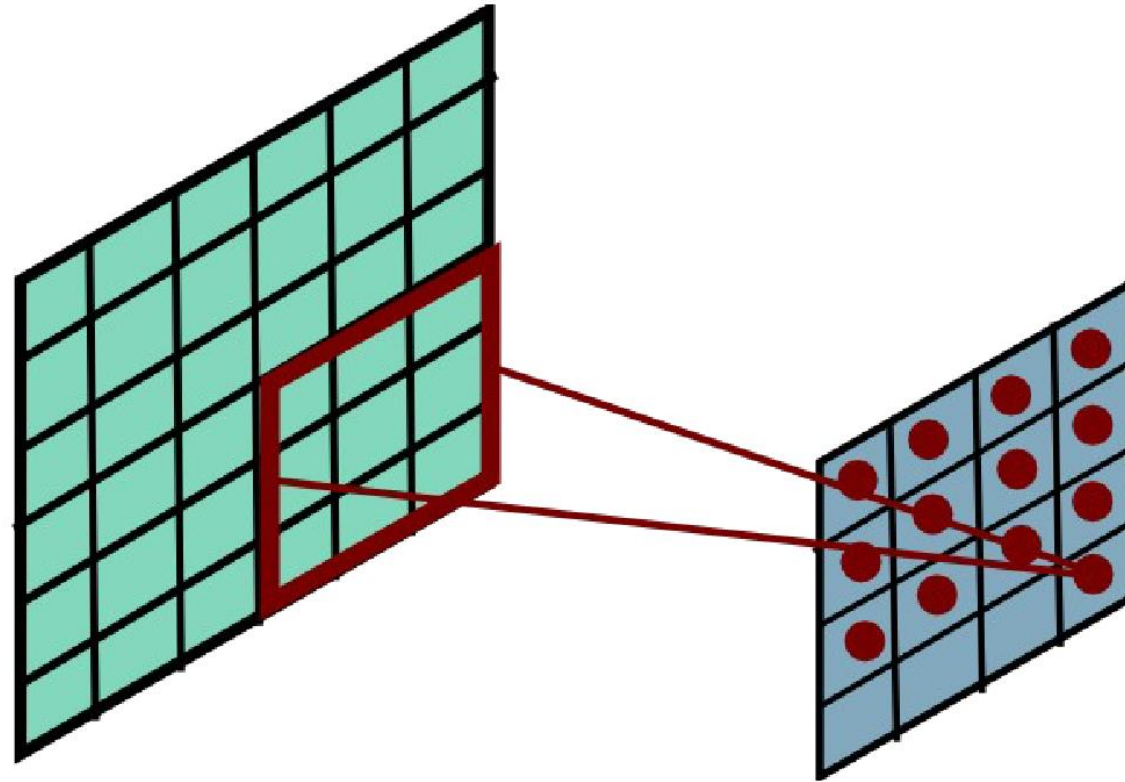
Convolutional Layer



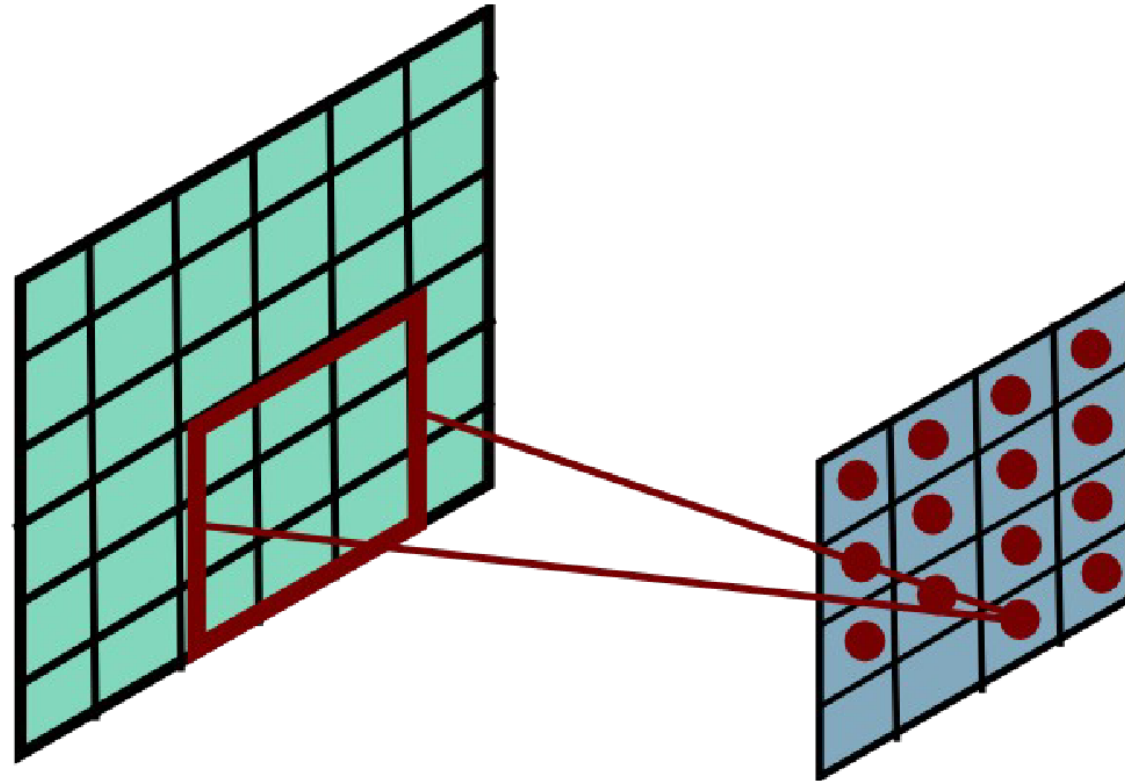
Convolutional Layer



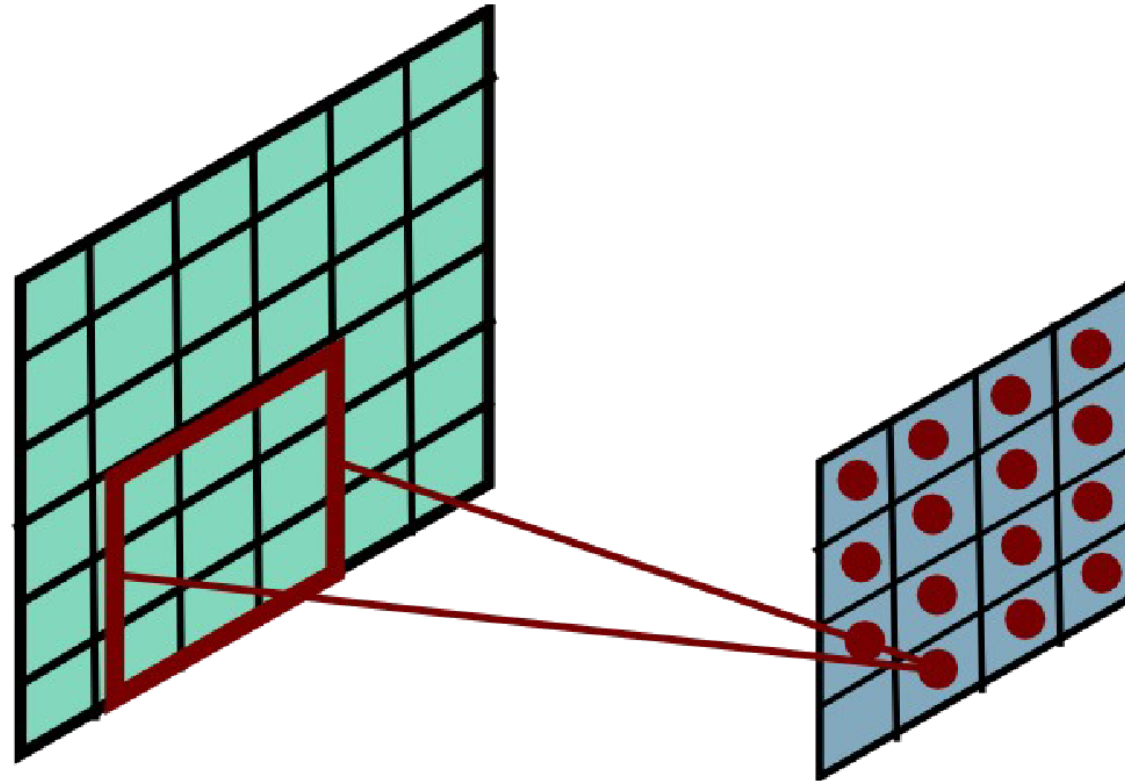
Convolutional Layer



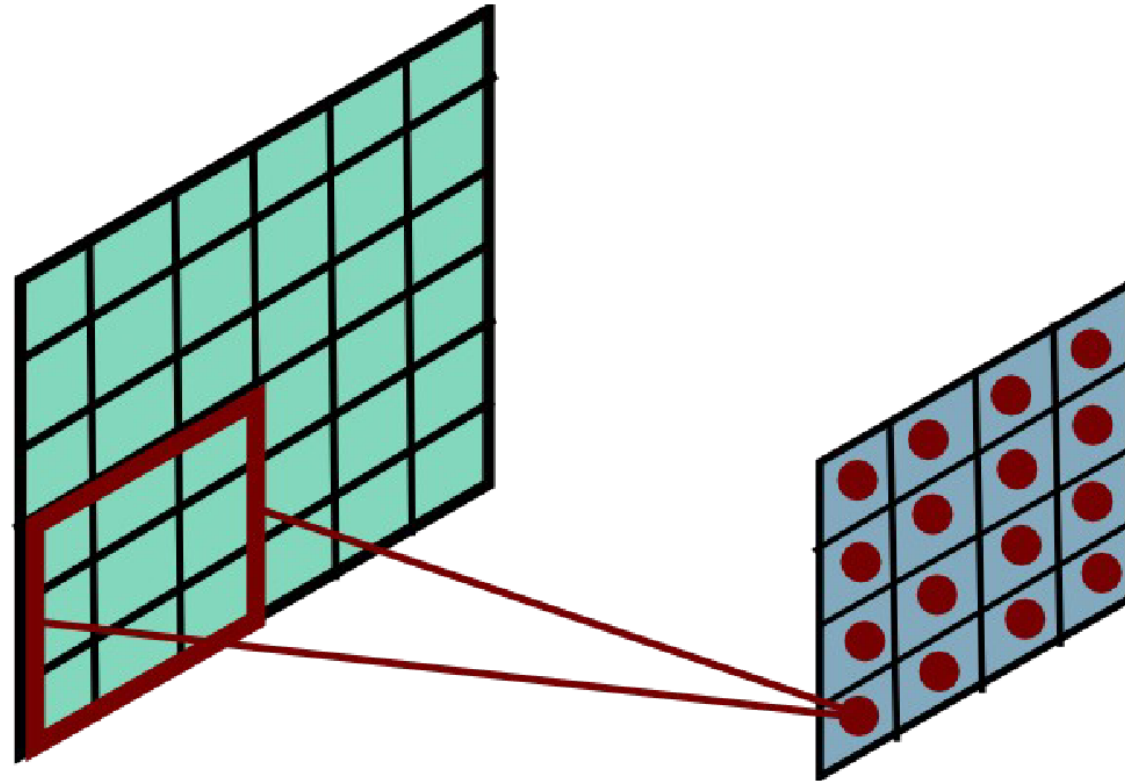
Convolutional Layer



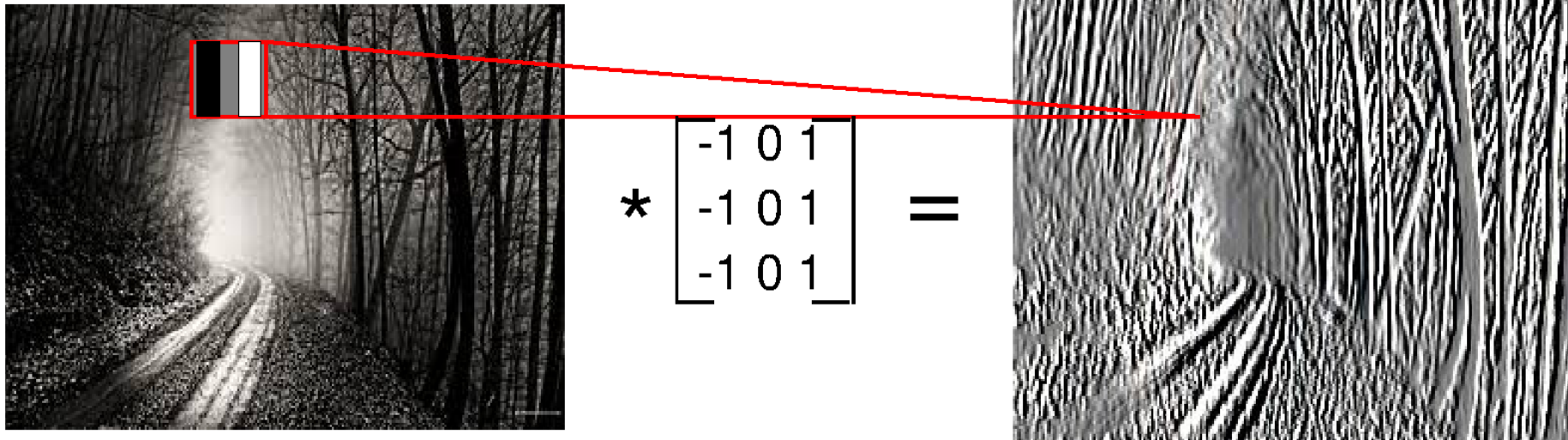
Convolutional Layer



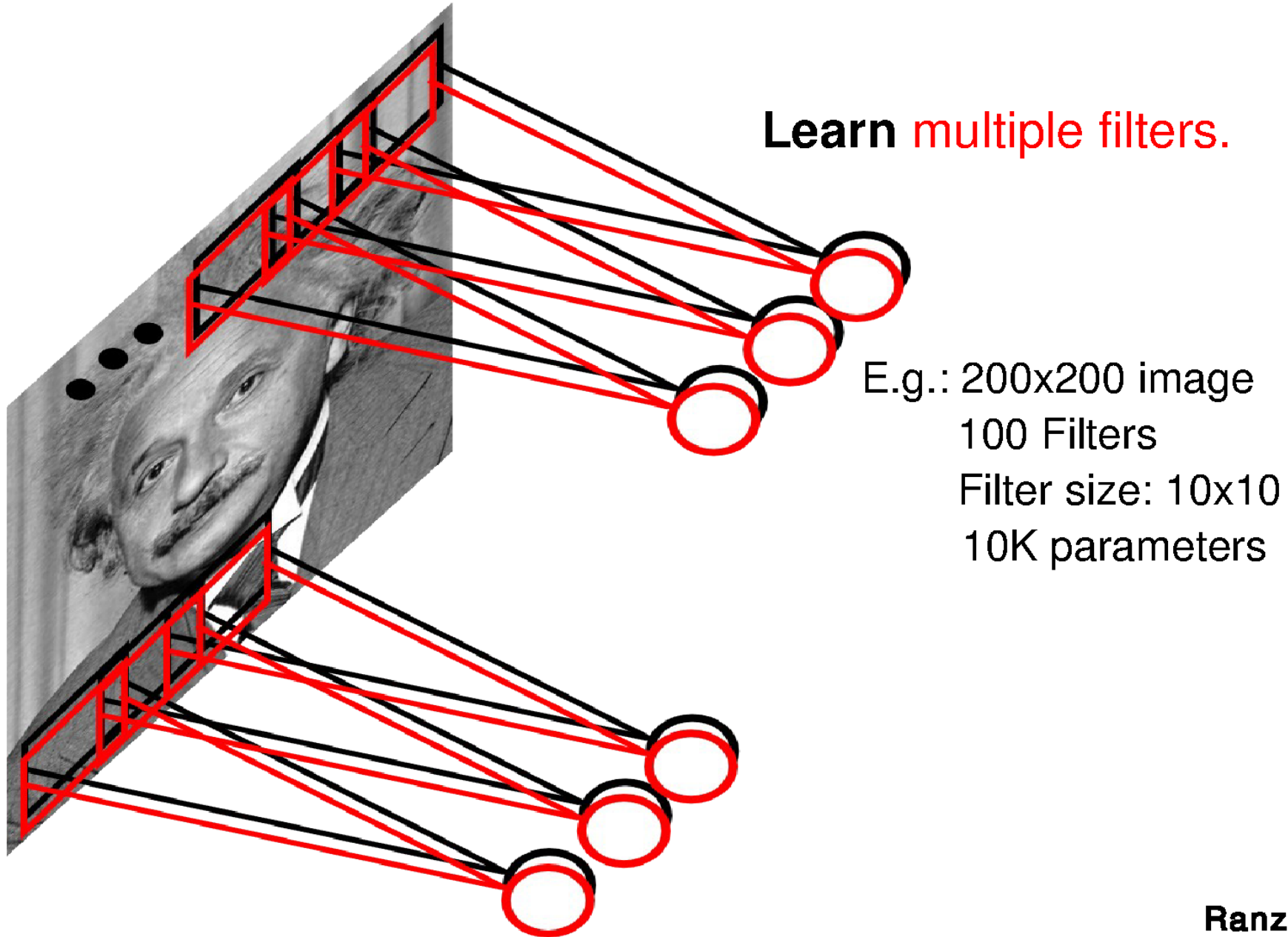
Convolutional Layer



Convolutional Layer



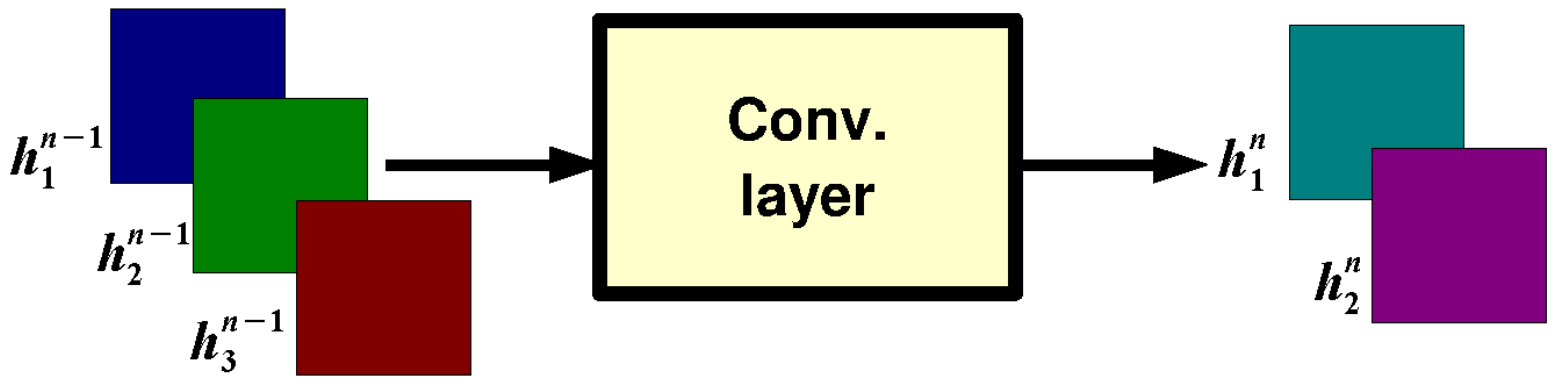
Convolutional Layer



Convolutional Layer

$$h_j^n = \max(0, \sum_{k=1}^K h_k^{n-1} * w_{kj}^n)$$

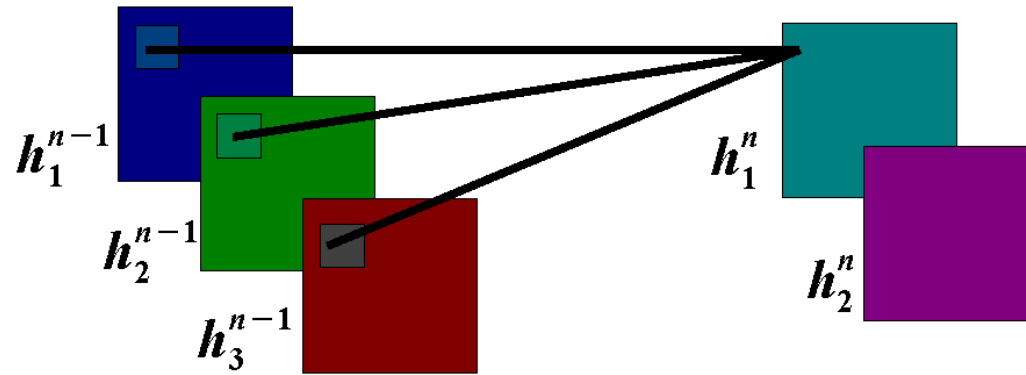
output feature map input feature map kernel



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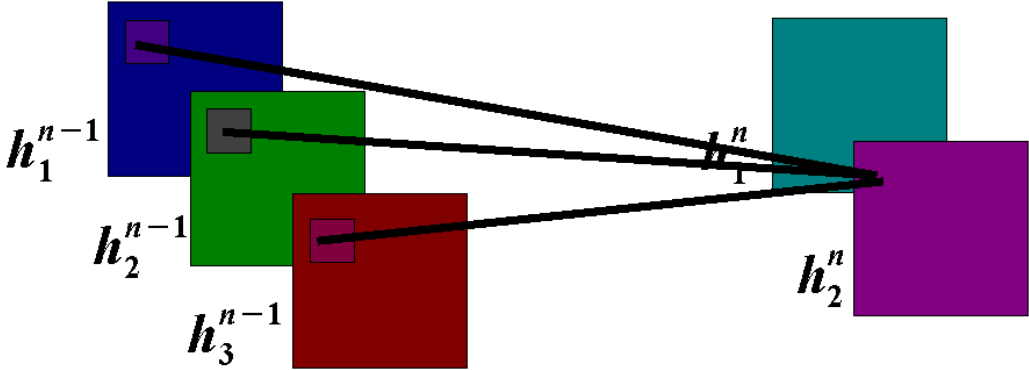
output feature map input feature map kernel



Convolutional Layer

$$h_j^n = \max(0, \sum_{k=1}^K h_k^{n-1} * w_{kj}^n)$$

output feature map input feature map kernel



Convolutional Layer

Question: What is the size of the output? What's the computational cost?

Answer: It is proportional to the number of filters and depends on the stride. If kernels have size $K \times K$, input has size $D \times D$, stride is 1, and there are M input feature maps and N output feature maps then:

- the input has size $M @ D \times D$
- the output has size $N @ (D-K+1) \times (D-K+1)$
- the kernels have $M \times N \times K \times K$ coefficients (which have to be learned)
- cost: $M * K * K * N * (D-K+1) * (D-K+1)$

Question: How many feature maps? What's the size of the filters?

Answer: Usually, there are more output feature maps than input feature maps. Convolutional layers can increase the number of hidden units by big factors (and are expensive to compute).

The size of the filters has to match the size/scale of the patterns we want to detect (task dependent).

Key Ideas

A standard neural net applied to images:

- scales quadratically with the size of the input
- does not leverage stationarity

Solution:

- connect each hidden unit to a small patch of the input
- share the weight across space

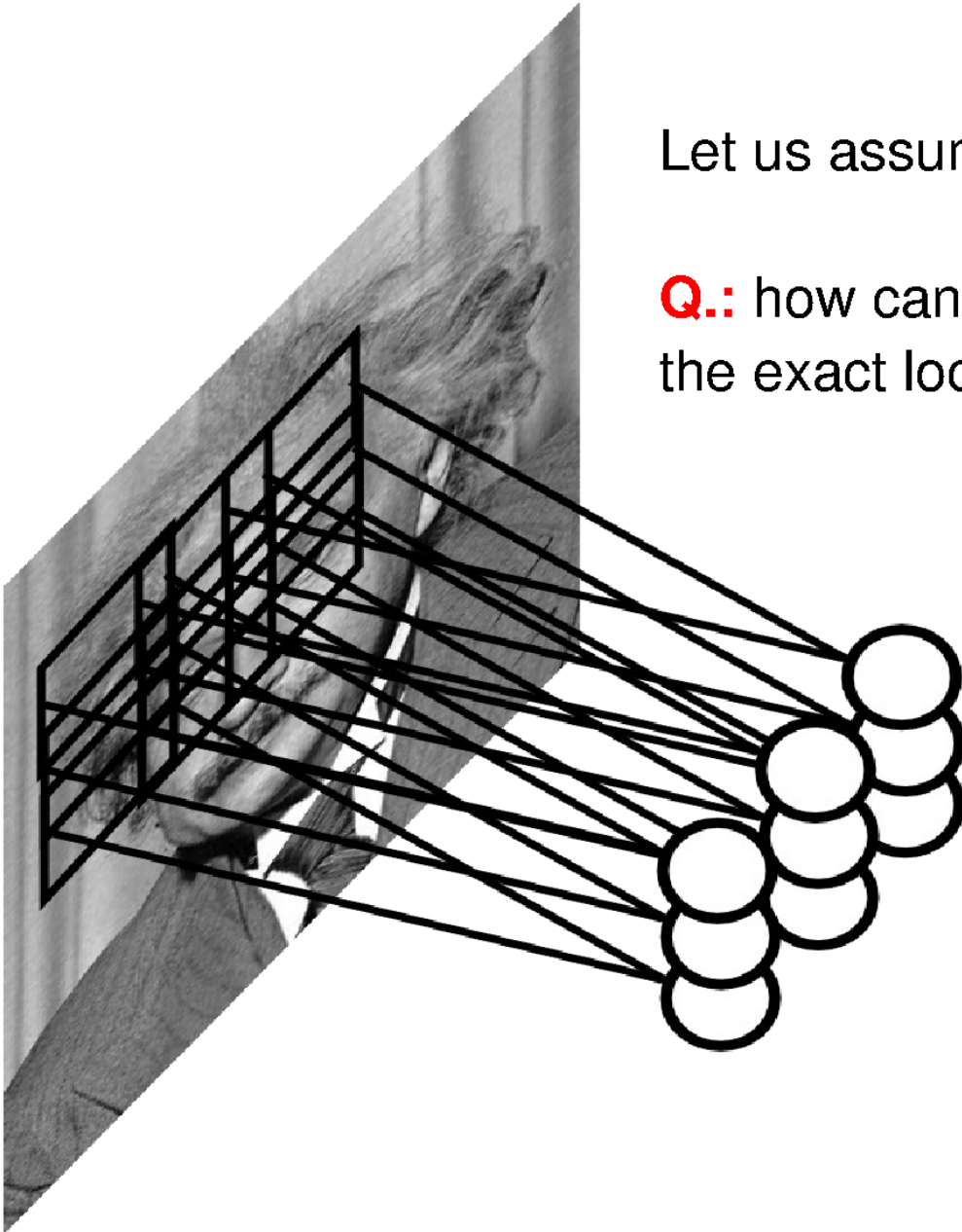
This is called: **convolutional layer.**

A network with convolutional layers is called **convolutional network.**

Pooling Layer

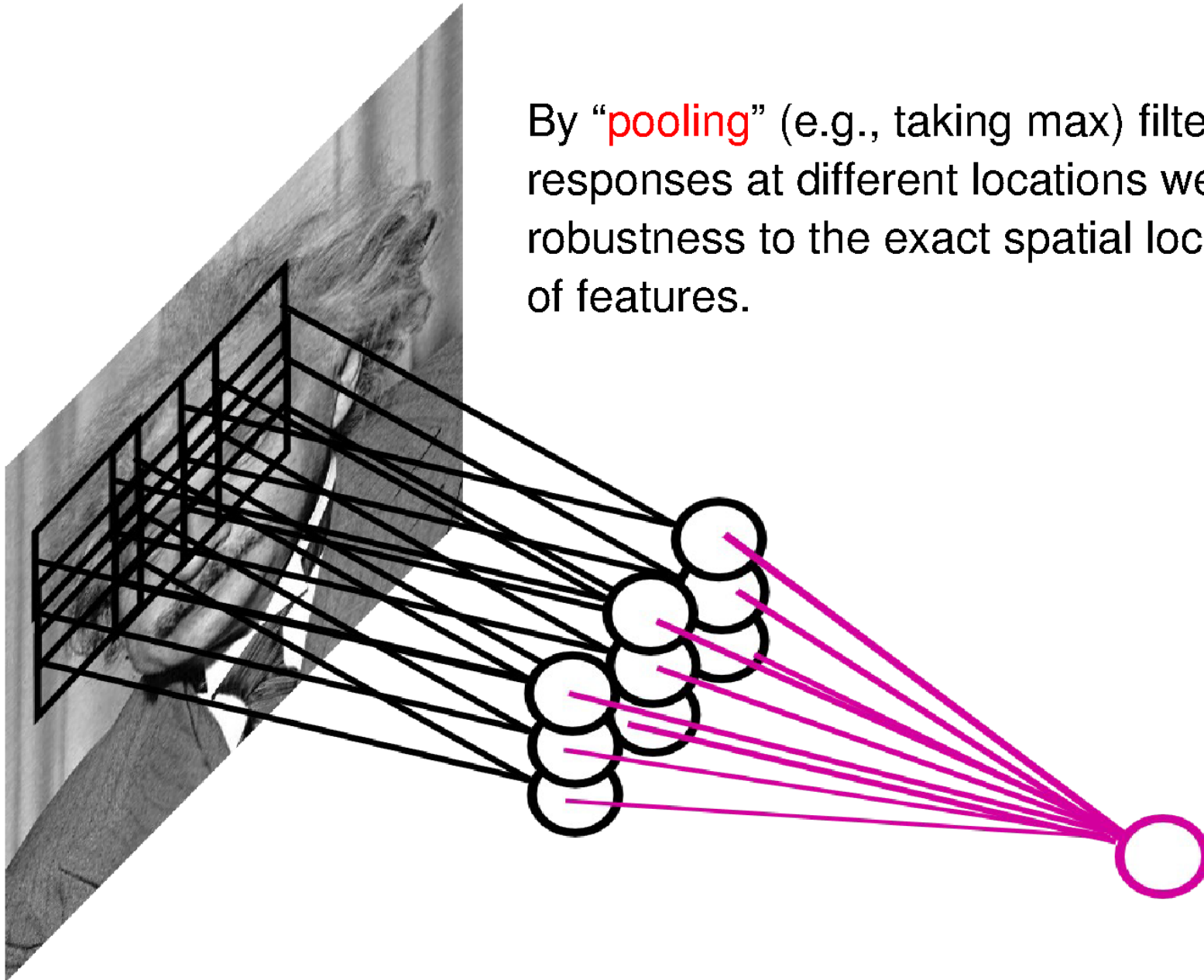
Let us assume filter is an “eye” detector.

Q.: how can we make the detection robust to the exact location of the eye?



Pooling Layer

By “pooling” (e.g., taking max) filter responses at different locations we gain robustness to the exact spatial location of features.



Pooling Layer: Examples

Max-pooling:

$$h_j^n(x, y) = \max_{\bar{x} \in N(x), \bar{y} \in N(y)} h_j^{n-1}(\bar{x}, \bar{y})$$

Average-pooling:

$$h_j^n(x, y) = 1/K \sum_{\bar{x} \in N(x), \bar{y} \in N(y)} h_j^{n-1}(\bar{x}, \bar{y})$$

L2-pooling:

$$h_j^n(x, y) = \sqrt{\sum_{\bar{x} \in N(x), \bar{y} \in N(y)} h_j^{n-1}(\bar{x}, \bar{y})^2}$$

L2-pooling over features:

$$h_j^n(x, y) = \sqrt{\sum_{k \in N(j)} h_k^{n-1}(x, y)^2}$$

Pooling Layer

Question: What is the size of the output? What's the computational cost?

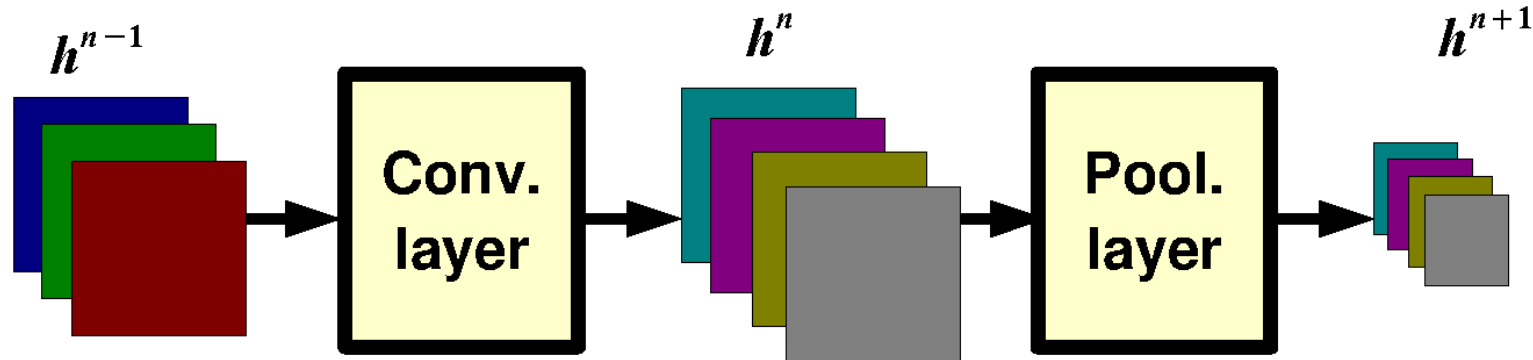
Answer: The size of the output depends on the stride between the pools. For instance, if pools do not overlap and have size $K \times K$, and the input has size $D \times D$ with M input feature maps, then:

- output is $M @ (D/K) \times (D/K)$
- the computational cost is proportional to the size of the input (negligible compared to a convolutional layer)

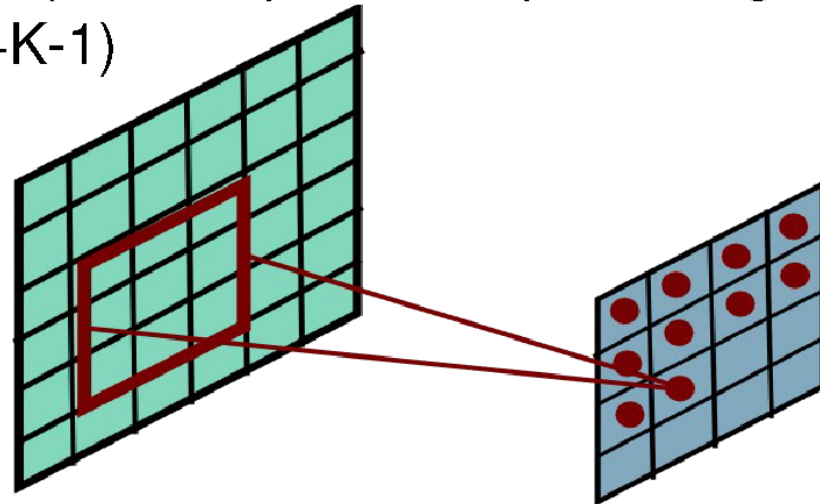
Question: How should I set the size of the pools?

Answer: It depends on how much “invariant” or robust to distortions we want the representation to be. It is best to pool slowly (via a few stacks of conv-pooling layers).

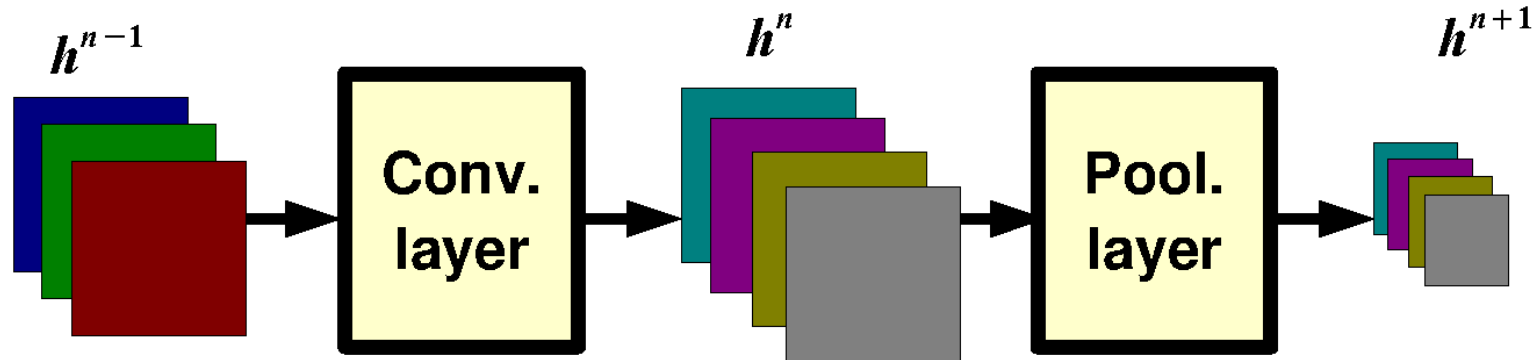
Pooling Layer: Receptive Field Size



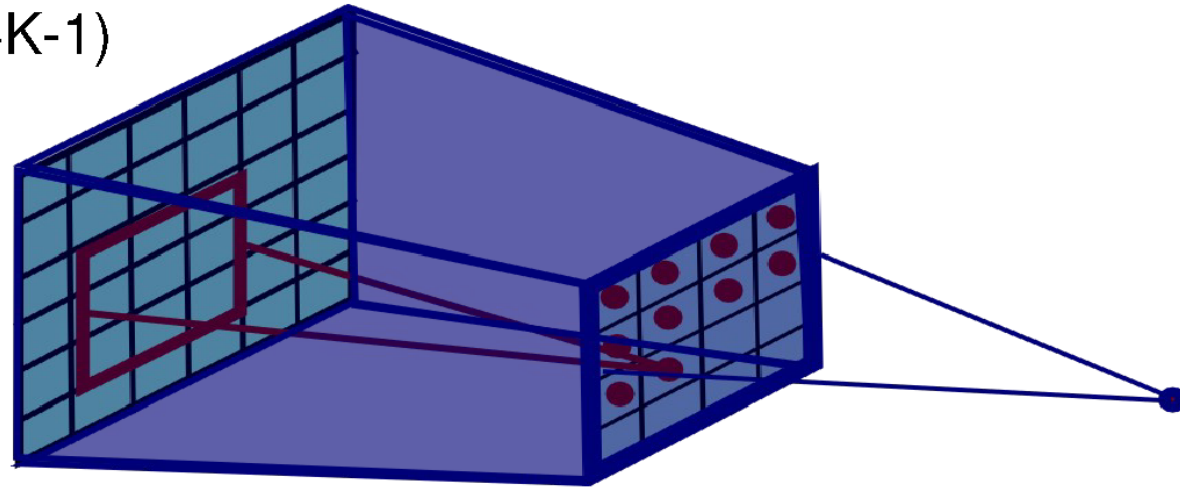
If convolutional filters have size $K \times K$ and stride 1, and pooling layer has pools of size $P \times P$, then each unit in the pooling layer depends upon a patch (at the input of the preceding conv. layer) of size:
 $(P+K-1) \times (P+K-1)$



Pooling Layer: Receptive Field Size

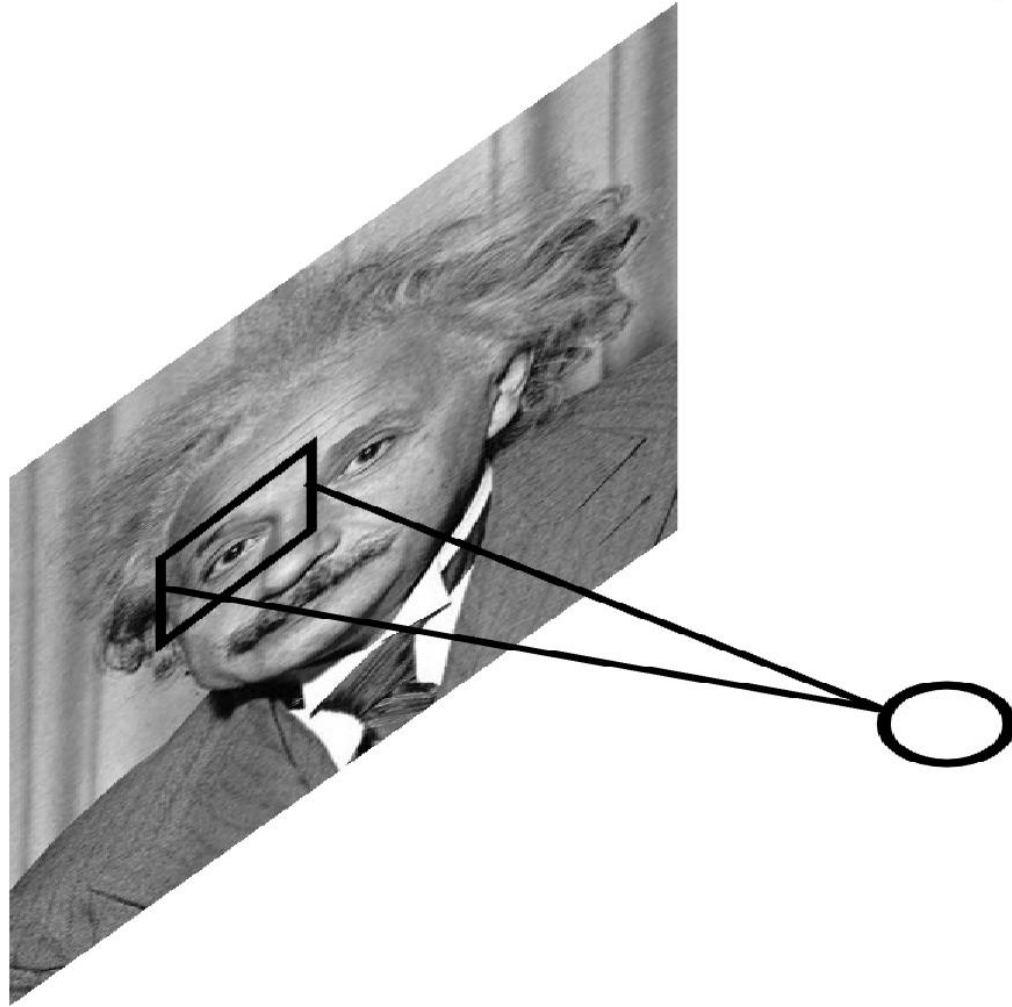


If convolutional filters have size $K \times K$ and stride 1, and pooling layer has pools of size $P \times P$, then each unit in the pooling layer depends upon a patch (at the input of the preceding conv. layer) of size:
 $(P+K-1) \times (P+K-1)$



Local Contrast Normalization

$$h^{i+1}(x, y) = \frac{h^i(x, y) - m^i(N(x, y))}{\sigma^i(N(x, y))}$$



Local Contrast Normalization

$$h^{i+1}(x, y) = \frac{h^i(x, y) - m^i(N(x, y))}{\sigma^i(N(x, y))}$$



We want the same response.

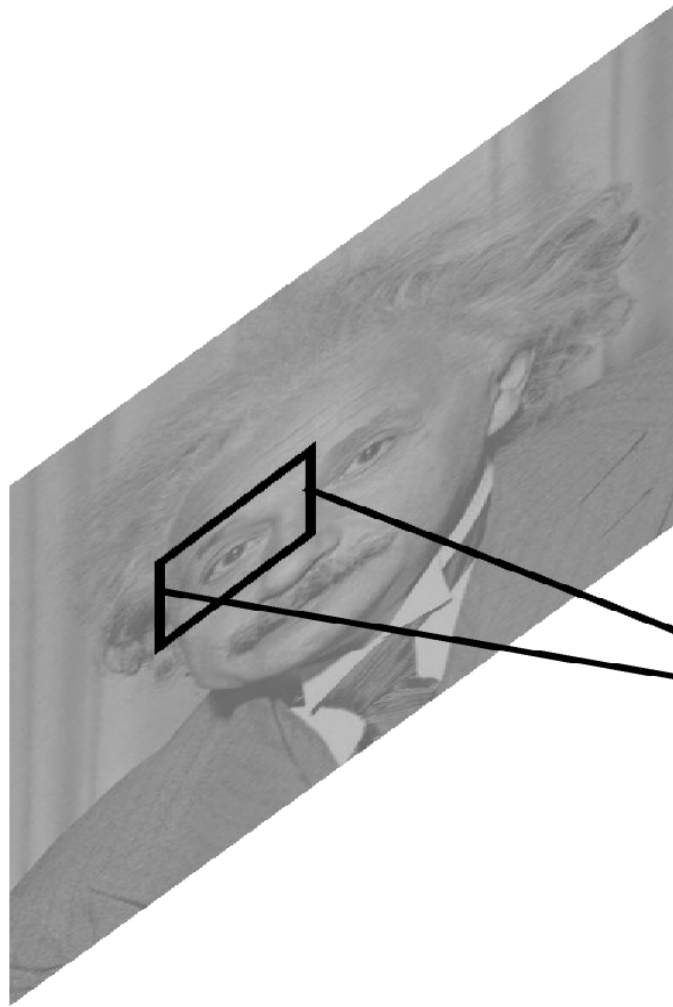
Local Contrast Normalization

$$h^{i+1}(x, y) = \frac{h^i(x, y) - m^i(N(x, y))}{\sigma^i(N(x, y))}$$

Performed also across features and in the higher layers..

Effects:

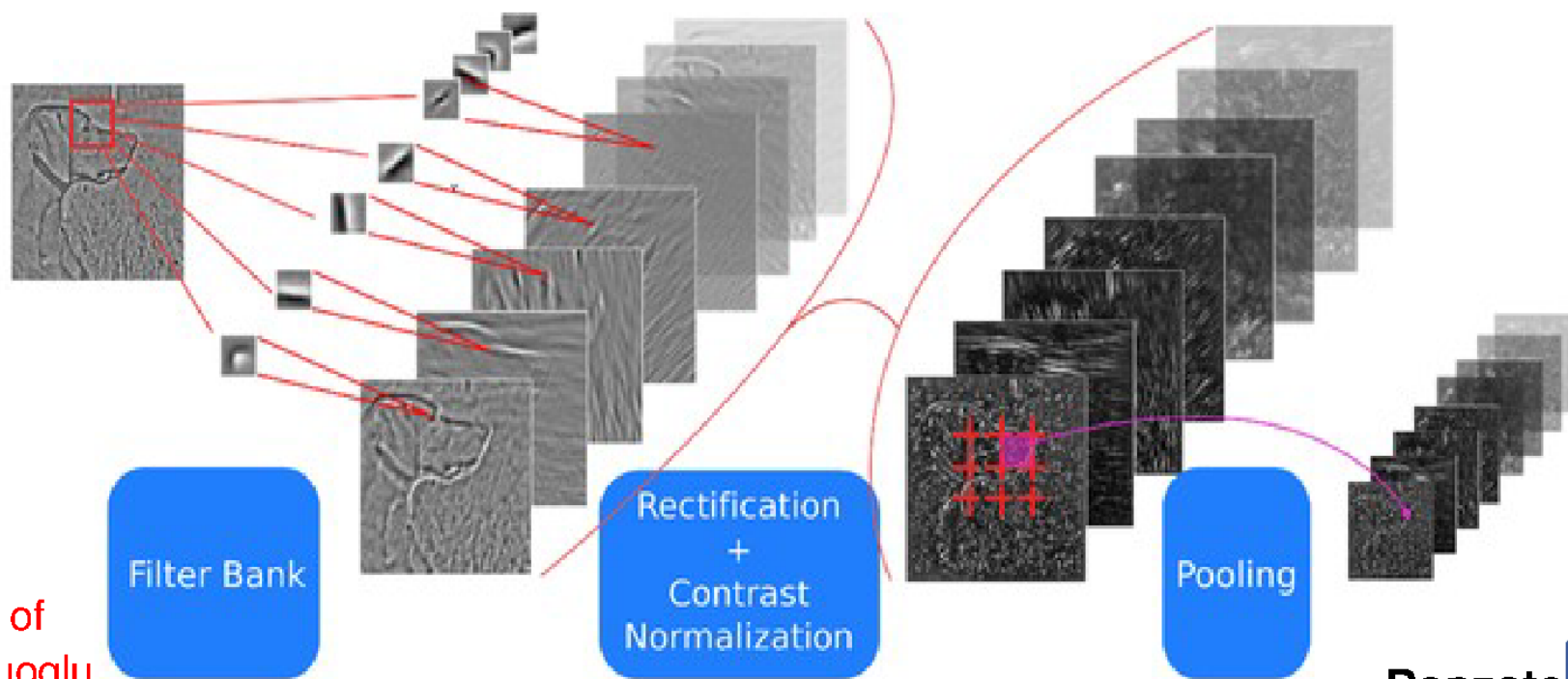
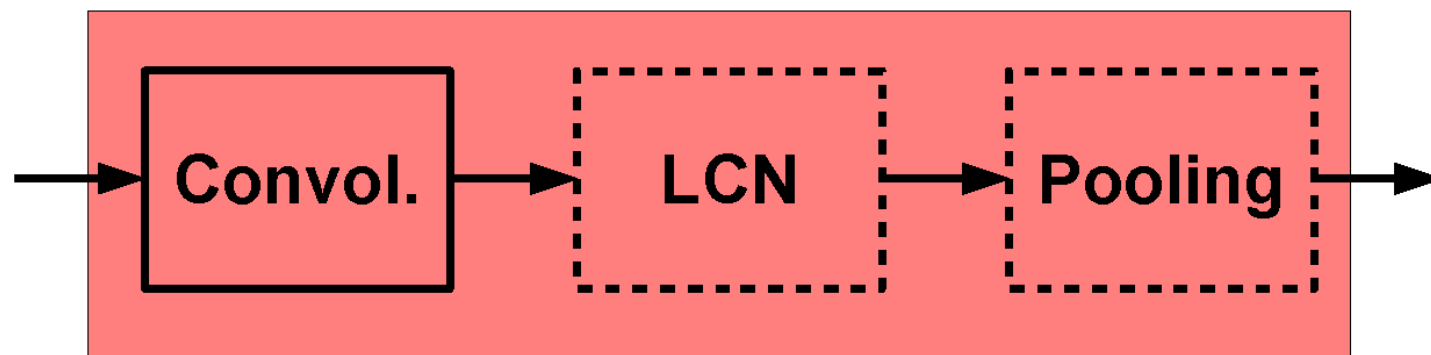
- improves invariance
- improves optimization
- increases sparsity



Note: computational cost is negligible w.r.t. conv. layer.

ConvNets: Typical Stage

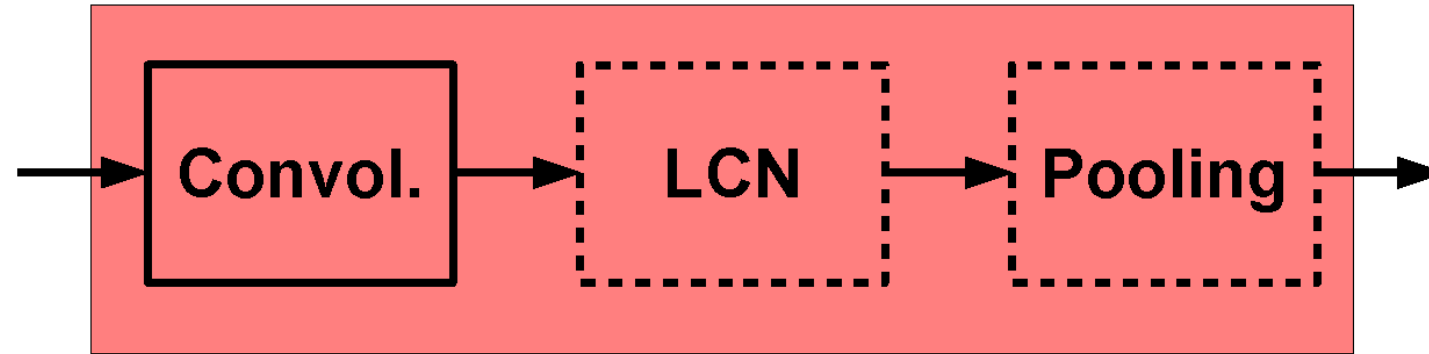
One stage (zoom)



courtesy of
K. Kavukcuoglu

ConvNets: Typical Stage

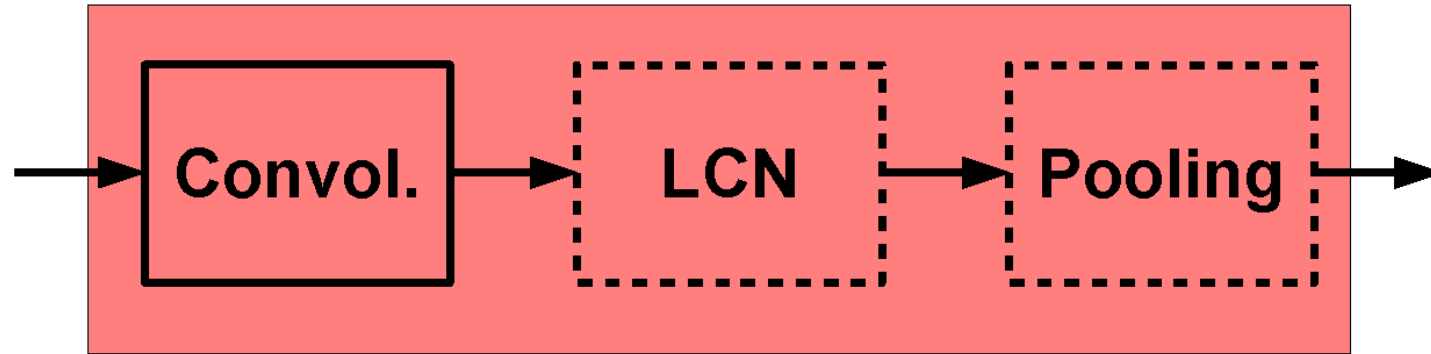
One stage (zoom)



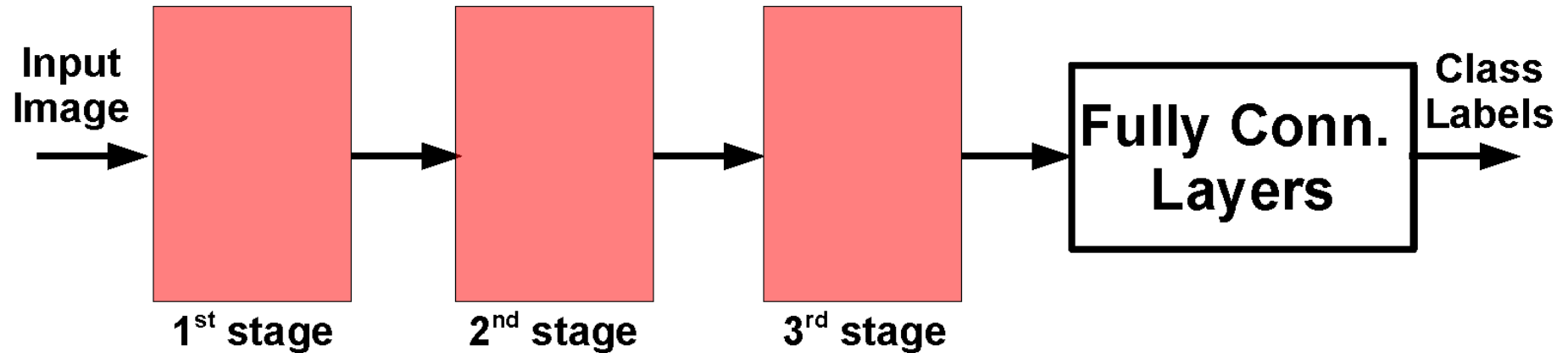
Conceptually similar to: SIFT, HoG, etc.

ConvNets: Typical Architecture

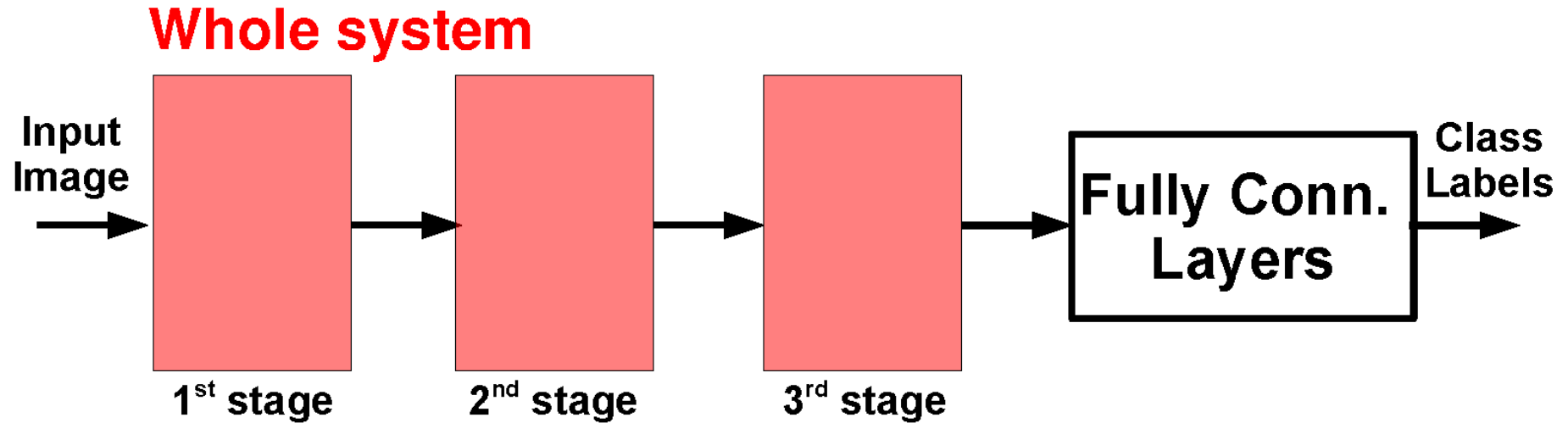
One stage (zoom)



Whole system



ConvNets: Typical Architecture



Conceptually similar to:

SIFT → K-Means → Pyramid Pooling → SVM

Lazebnik et al. "...Spatial Pyramid Matching..." CVPR 2006

SIFT → Fisher Vect. → Pooling → SVM

Sanchez et al. "Image classification with F.V.: Theory and practice" IJCV 2012

ConvNets: Training

All layers are differentiable (a.e.).

We can use standard back-propagation.

Algorithm:

Given a small mini-batch

- F-PROP

- B-PROP

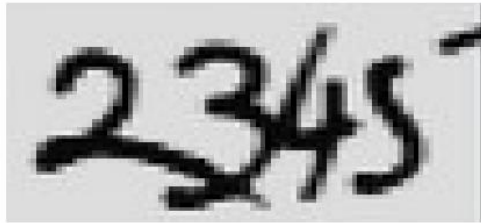
- PARAMETER UPDATE

Outline

- Supervised Neural Networks
- Convolutional Neural Networks
- **Examples**
- Tips

CONV NETS: EXAMPLES

- OCR / House number & Traffic sign classification



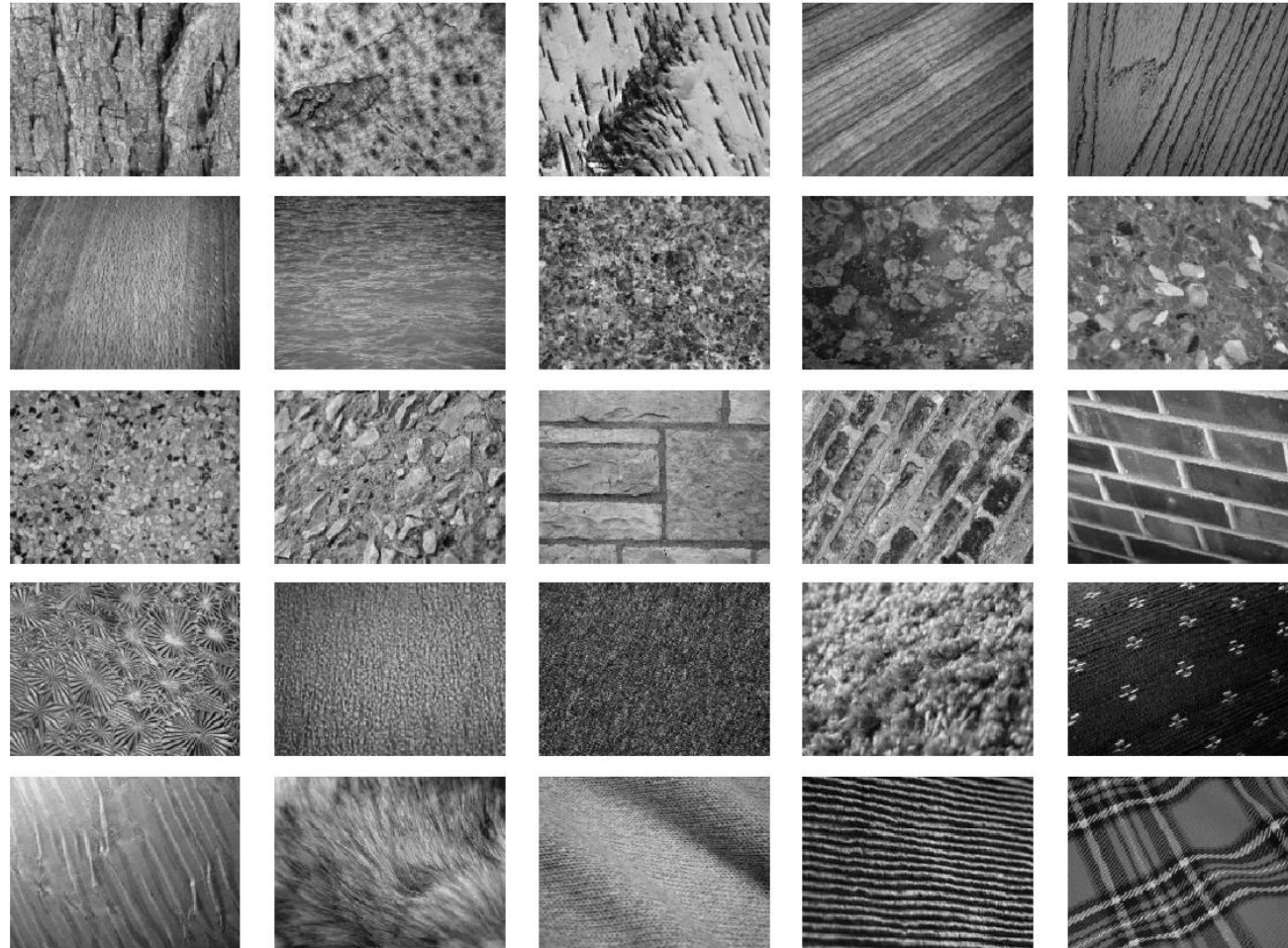
Ciresan et al. "MCDNN for image classification" CVPR 2012

Wan et al. "Regularization of neural networks using dropconnect" ICML 2013

Jaderberg et al. "Synthetic data and ANN for natural scene text recognition" arXiv 2014

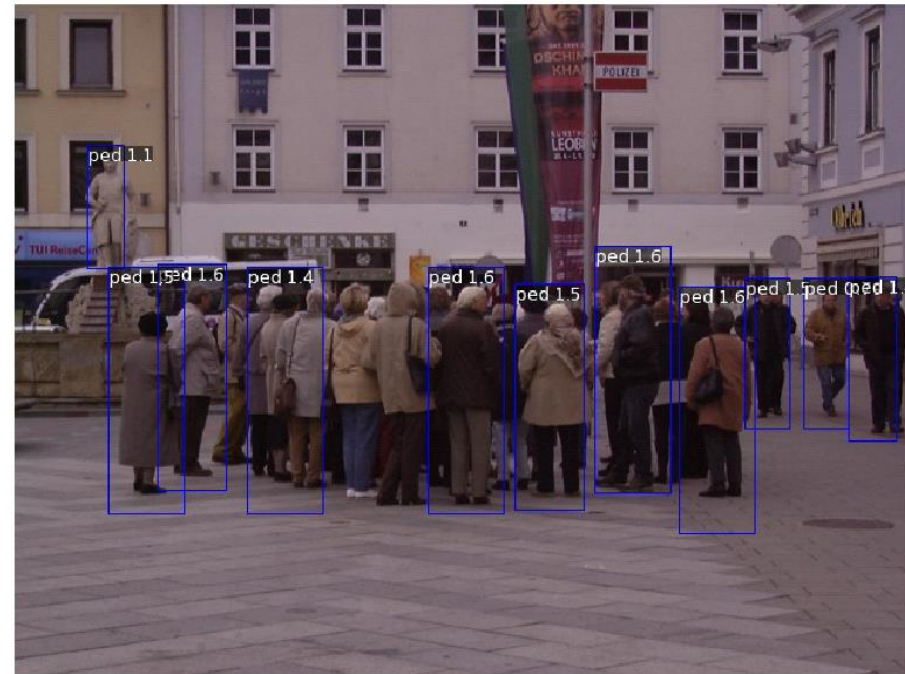
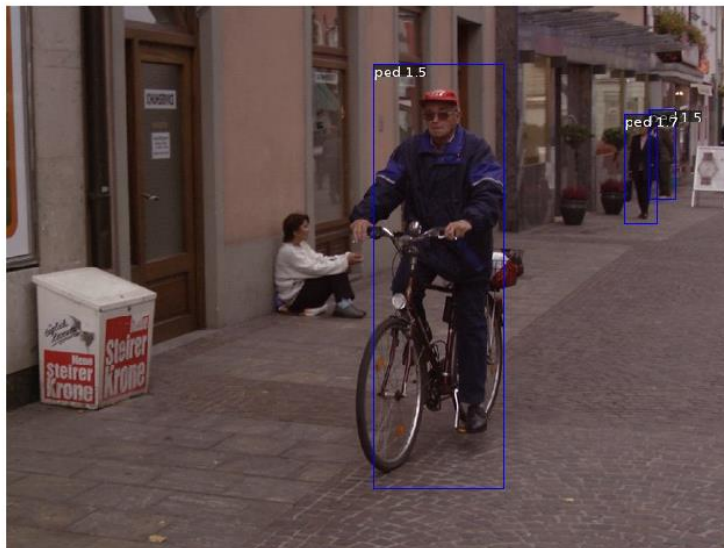
CONV NETS: EXAMPLES

- Texture classification



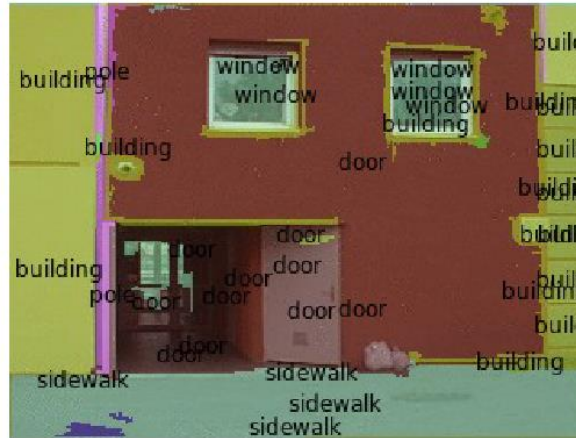
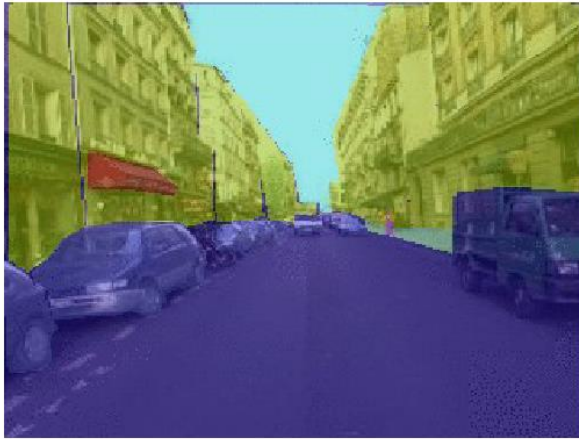
CONV NETS: EXAMPLES

- Pedestrian detection



CONV NETS: EXAMPLES

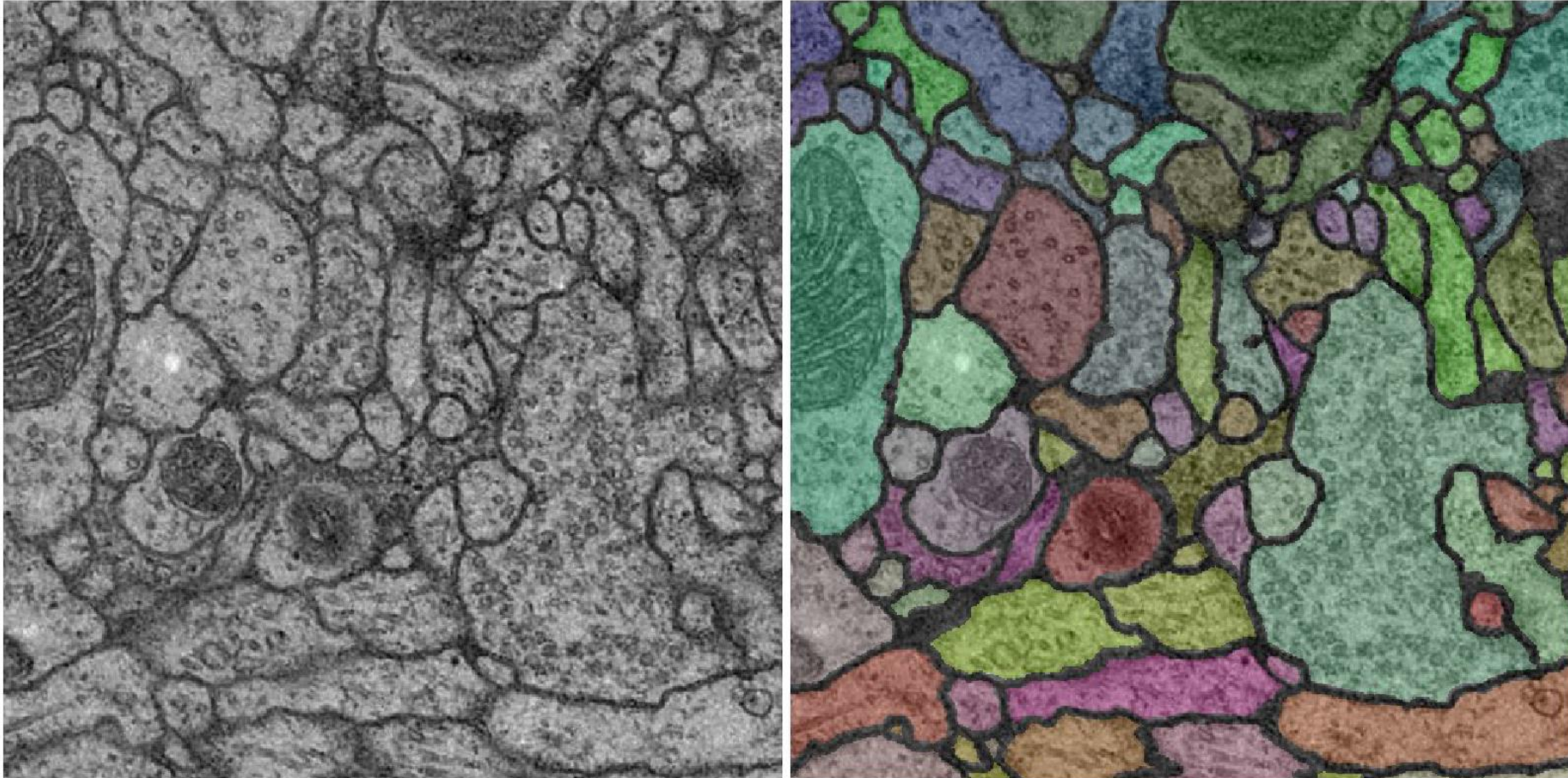
- Scene Parsing



Farabet et al. "Learning hierarchical features for scene labeling" PAMI 2013
Pinheiro et al. "Recurrent CNN for scene parsing" arxiv 2013

CONV NETS: EXAMPLES

- Segmentation 3D volumetric images



Ciresan et al. "DNN segment neuronal membranes..." NIPS 2012

Turaga et al. "Maximin learning of image segmentation" NIPS 2009

CONV NETS: EXAMPLES

- Action recognition from videos



Taylor et al. "Convolutional learning of spatio-temporal features" ECCV 2010

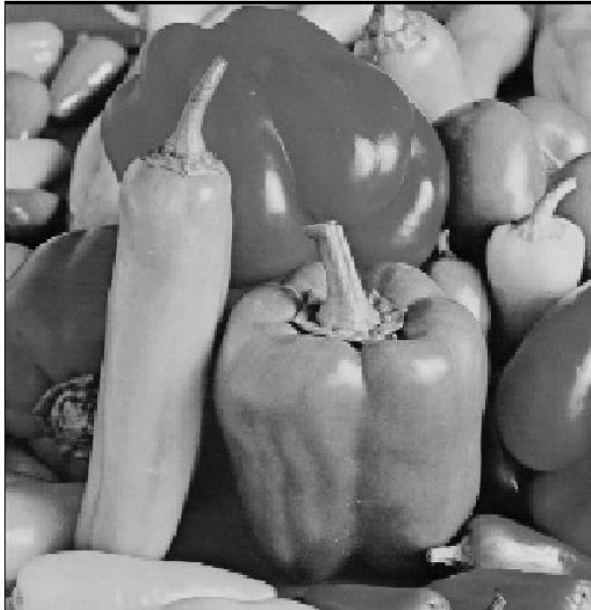
Karpathy et al. "Large-scale video classification with CNNs" CVPR 2014

Simonyan et al. "Two-stream CNNs for action recognition in videos" arXiv 2014

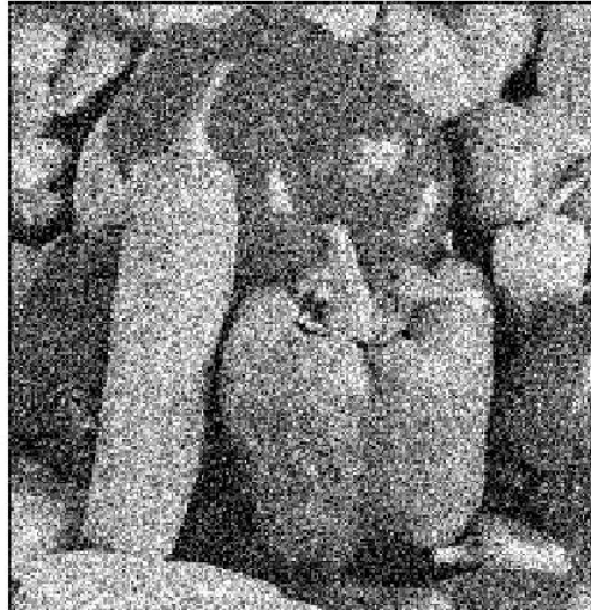
CONV NETS: EXAMPLES

- Denoising

original



noised



denoised

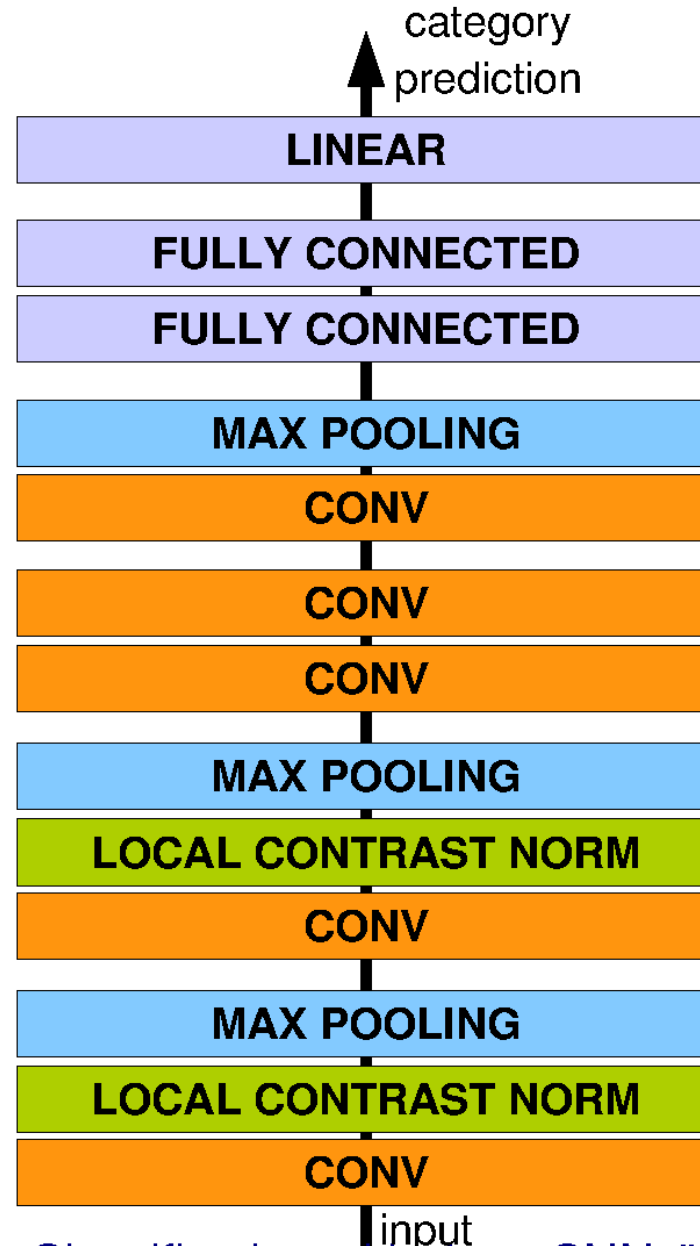


ImageNet

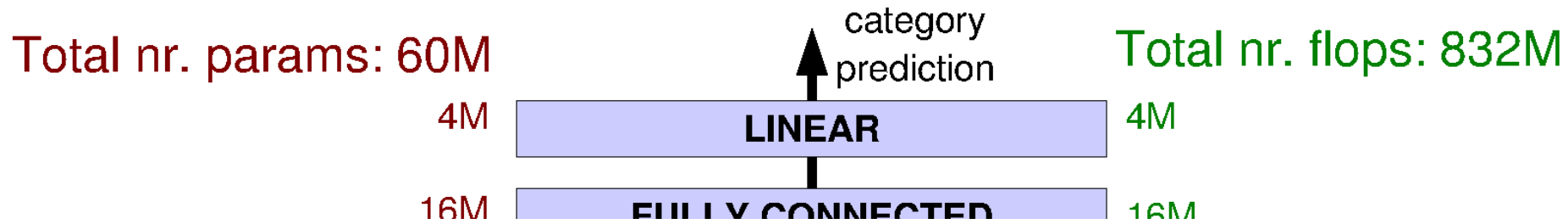
Examples of hammer:



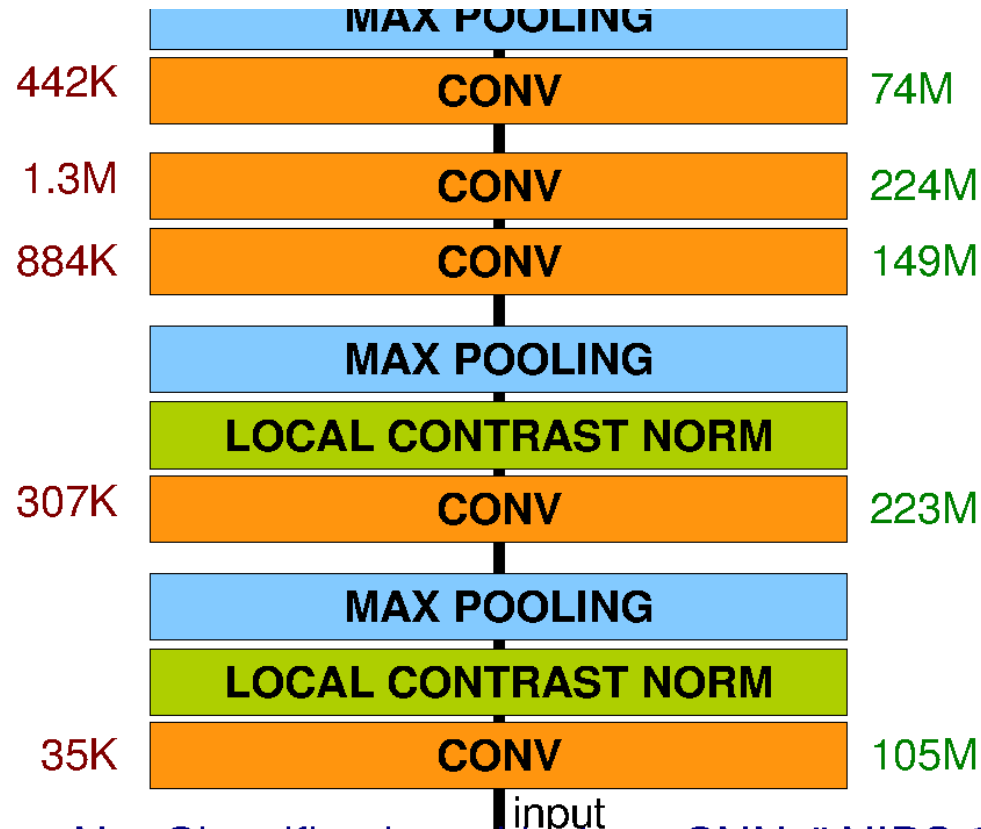
Architecture for Classification



Architecture for Classification



The first convolutional layer filters the $224 \times 224 \times 3$ input image with 96 kernels of size $11 \times 11 \times 3$ with a stride of 4 pixels (this is the distance between the receptive field centers of neighboring



Optimization

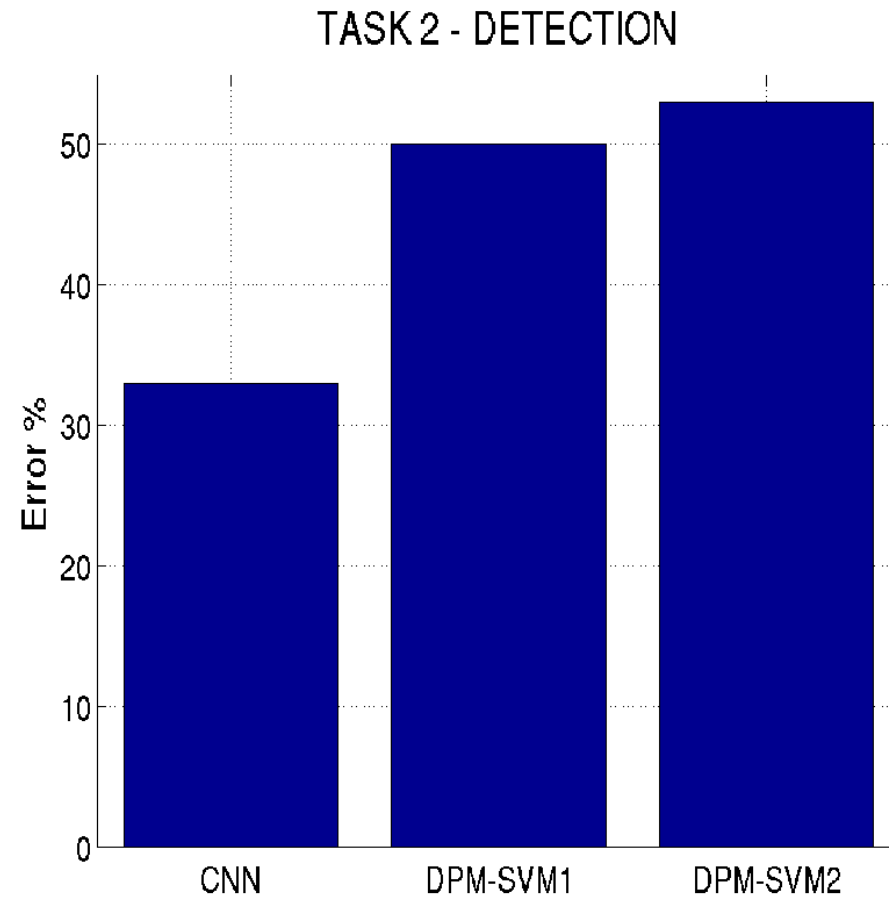
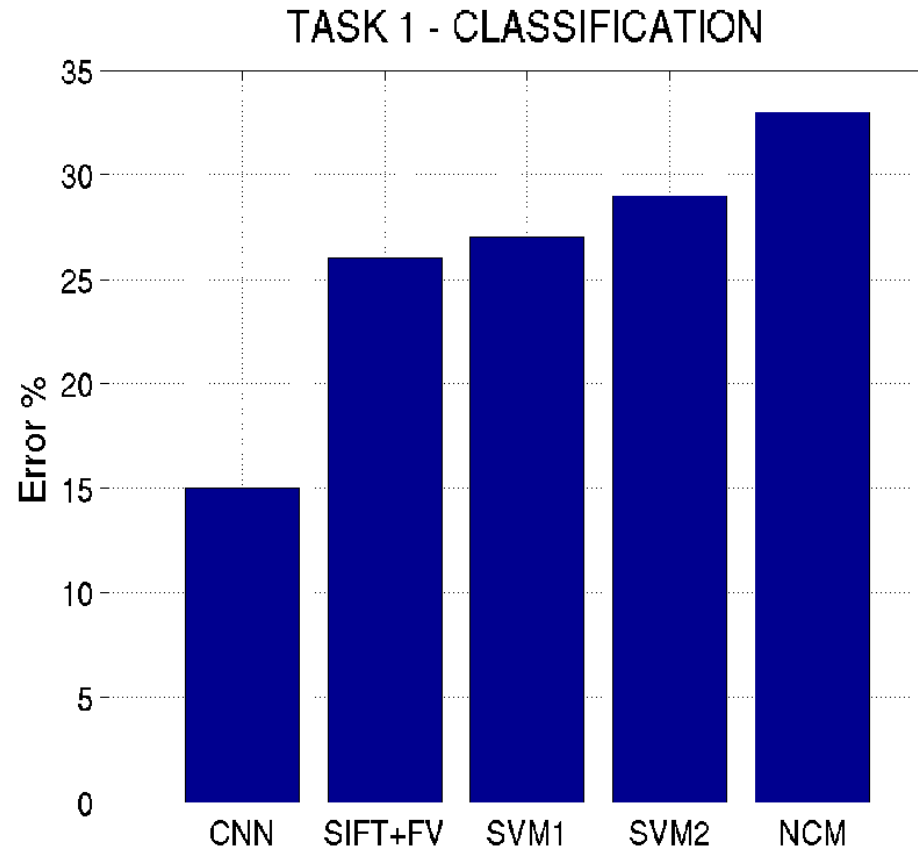
SGD with momentum:

- Learning rate = 0.01
- Momentum = 0.9

Improving generalization by:

- Weight sharing (convolution)
- Input distortions
- Dropout = 0.5
- Weight decay = 0.0005

Results: ILSVRC 2012





mite



container ship



motor scooter



leopard

	mite
	black widow
	cockroach
	tick
	starfish

	container ship
	lifeboat
	amphibian
	fireboat
	drilling platform

	motor scooter
	go-kart
	moped
	bumper car
	golfcart

	leopard
	jaguar
	cheetah
	snow leopard
	Egyptian cat



grille



mushroom



cherry



Madagascar cat

	convertible
	grille
	pickup
	beach wagon
	fire engine

	agaric
	mushroom
	jelly fungus
	gill fungus
	dead-man's-fingers

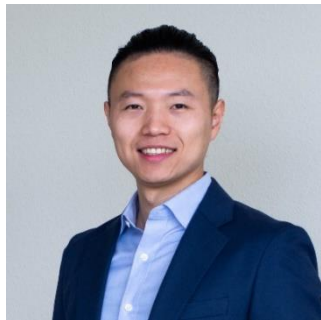
	dalmatian
	grape
	elderberry
	ffordshire bullterrier
	currant

	squirrel monkey
	spider monkey
	titi
	indri
	howler monkey



Object Detectors Emerge in Deep Scene CNNs

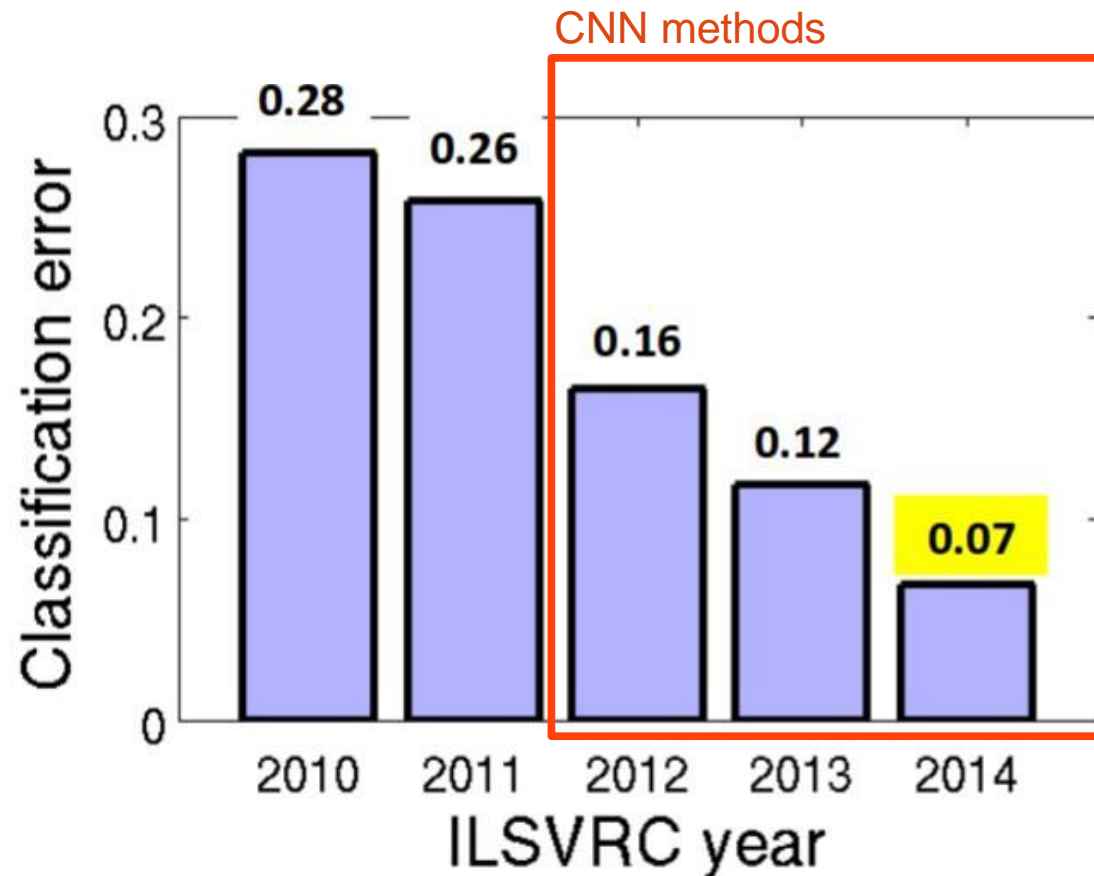
Bolei Zhou, Aditya Khosla, Agata Lapedriza, Aude Oliva, Antonio Torralba



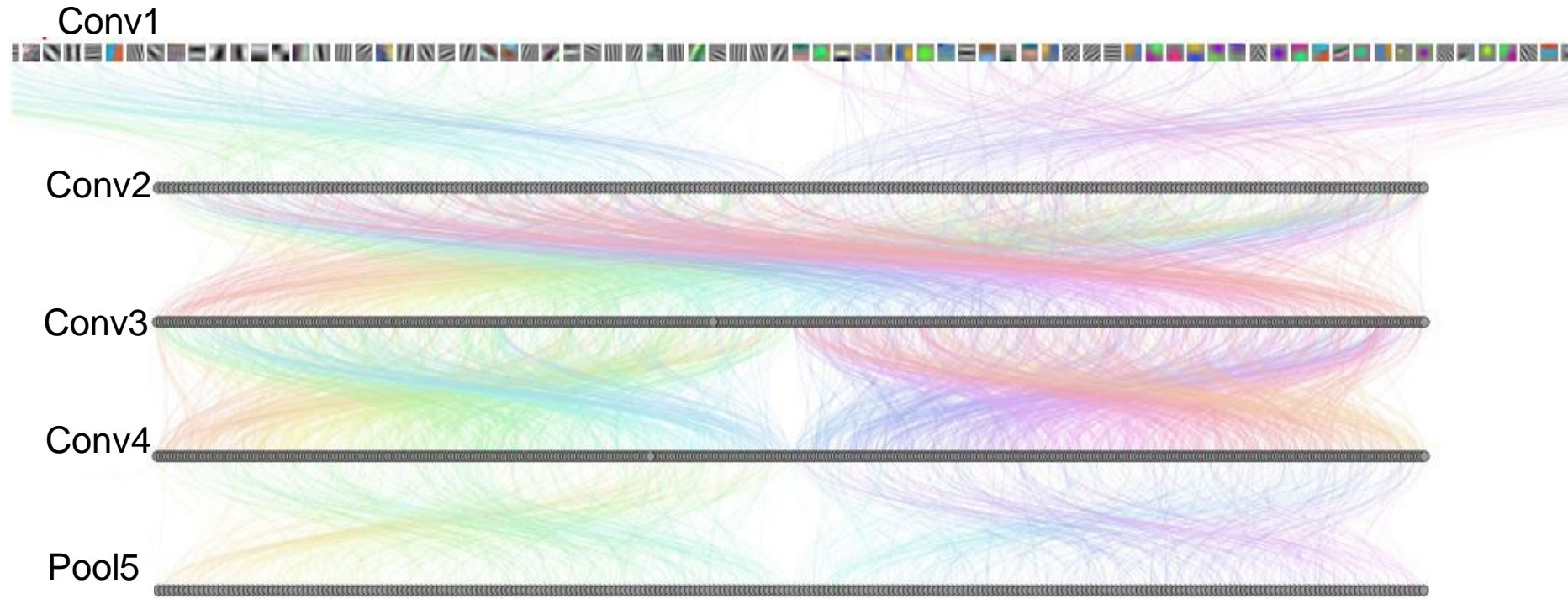
Massachusetts Institute of Technology

CNN for Object Recognition

Large-scale image classification result on ImageNet



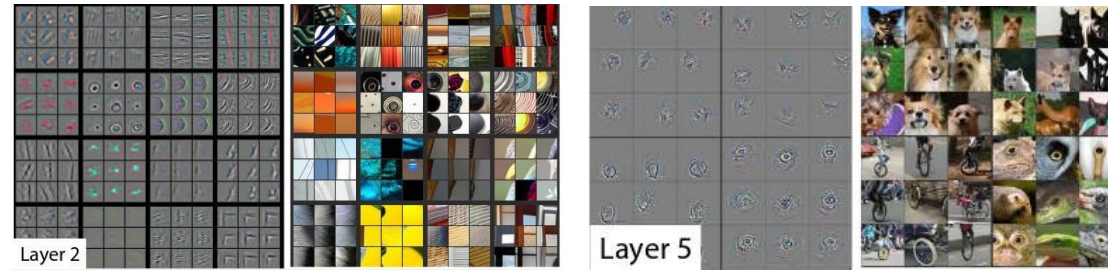
How Objects are Represented in CNN?



DrawCNN: visualizing the units' connections

How Objects are Represented in CNN?

Deconvolution



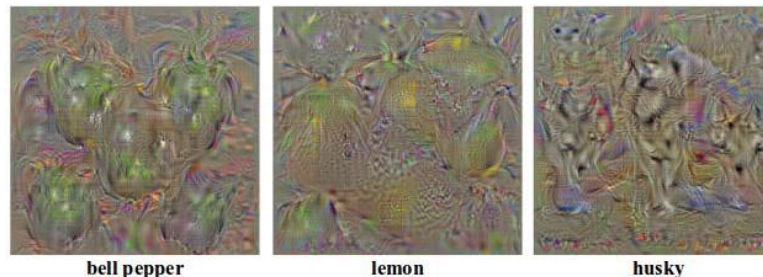
Zeiler, M. et al. Visualizing and Understanding Convolutional Networks, ECCV 2014.

Strong activation image



Girshick, R., Donahue, J., Darrell, T., Malik, J.: Rich feature hierarchies for accurate object detection and semantic segmentation. CVPR 2014

Back-propagation



Simonyan, K. et al. Deep inside convolutional networks: Visualising image classification models and saliency maps. ICLR workshop, 2014

Object Representations in Computer Vision

Part-based models are used to represent objects and visual patterns.

- Object as a set of parts
- Relative locations between parts

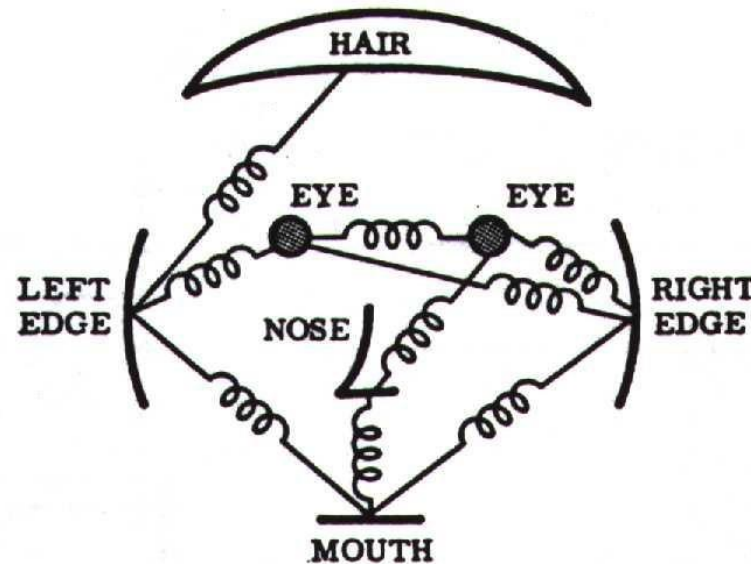


Figure from Fischler & Elschlager (1973)

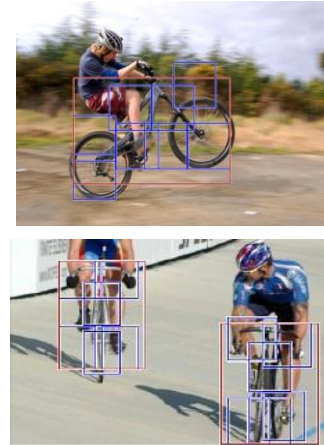
Object Representations in Computer Vision

Constellation model



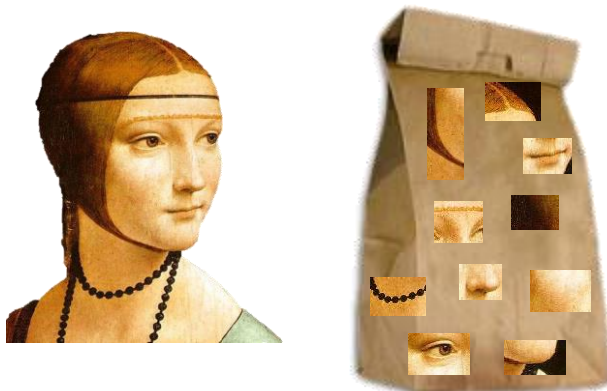
Weber, Welling & Perona (2000),
Fergus, Perona & Zisserman (2003)

Deformable Part model



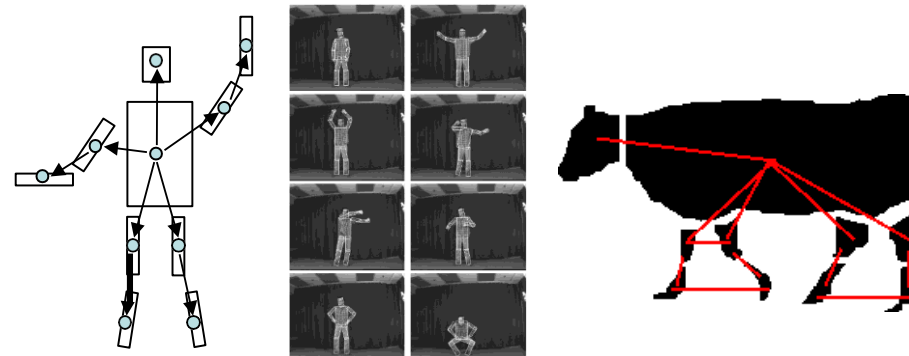
P. Felzenszwalb, R. Girshick, D. McAllester, D.
Ramanan (2010)

Bag-of-words model



Lazebnik, Schmid & Ponce(2003), Fei-Fei Perona (2005)

Class-specific graph model



Kumar, Torr and Zisserman (2005), Felzenszwalb & Huttenlocher (2005)

Learning to Recognize Objects

IMAGENET

brambling

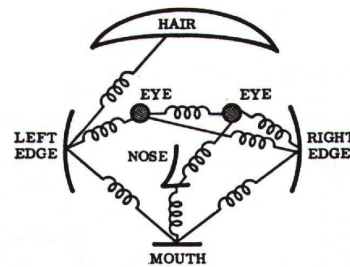


terrier



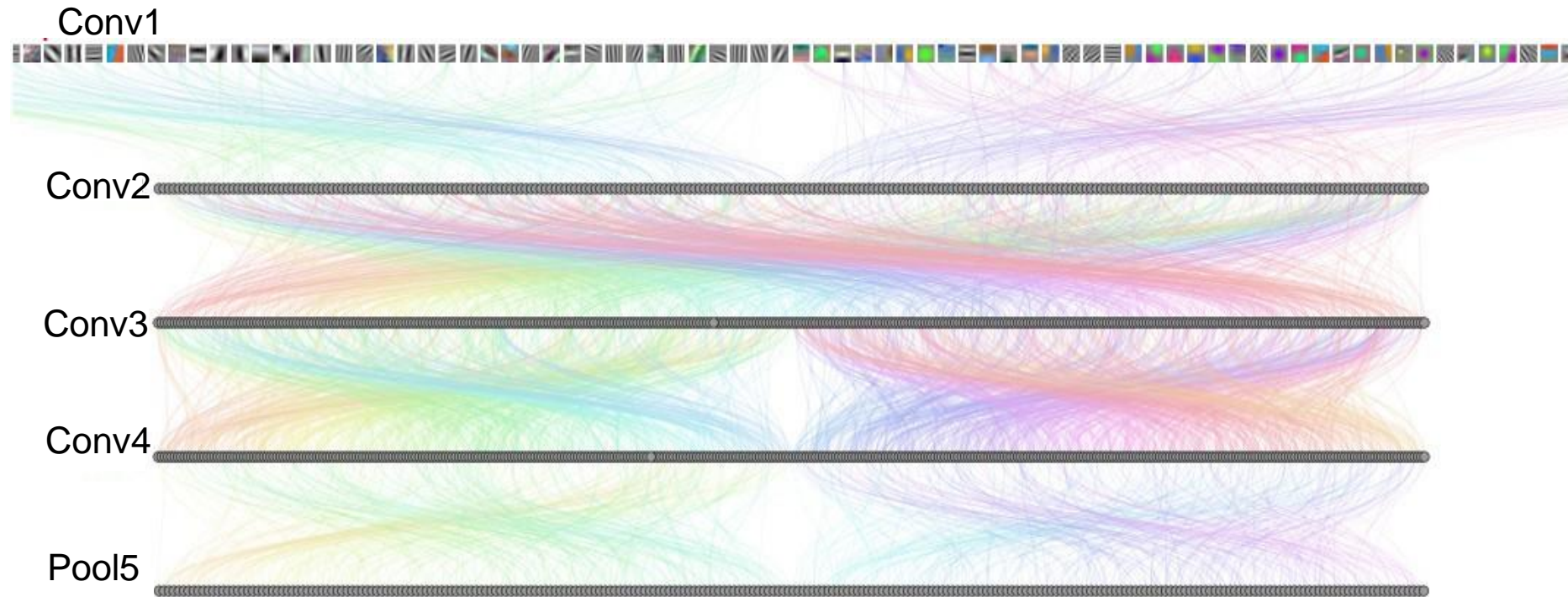
Possible internal representations:

- Object parts
- Textures
- Attributes



How Objects are Represented in CNN?

CNN uses **distributed code** to represent objects.



Agrawal, et al. Analyzing the performance of multilayer neural networks for object recognition. ECCV, 2014

Szegedy, et al. Intriguing properties of neural networks. arXiv preprint arXiv:1312.6199, 2013.

Zeiler, M. et al. Visualizing and Understanding Convolutional Networks, ECCV 2014.

Scene Recognition

Given an image, predict which place we are in.



Bedroom



Harbor

Learning to Recognize Scenes

bedroom

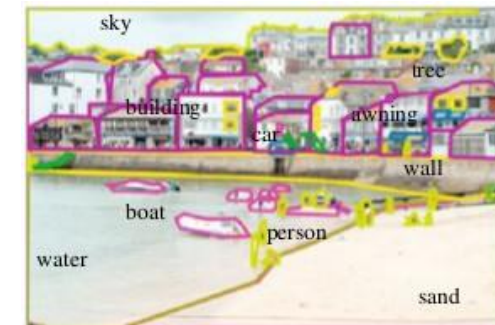


mountain



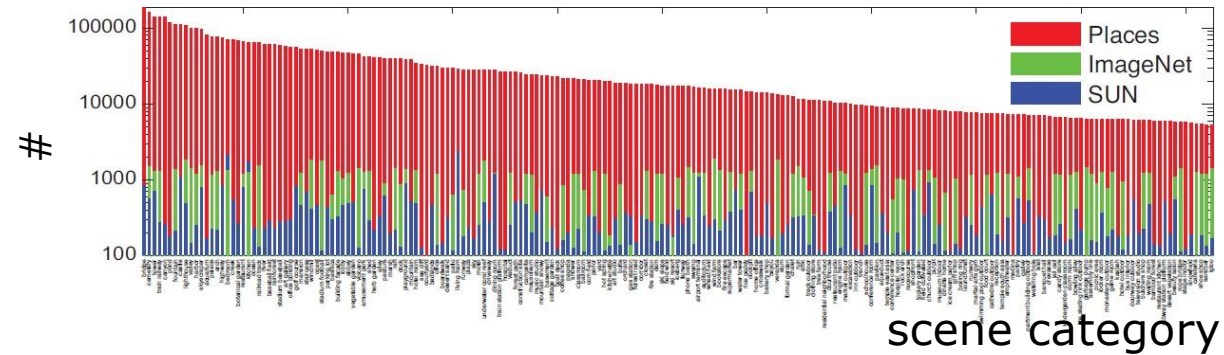
Possible internal representations:

- Objects (scene parts?)
- Scene attributes
- Object parts
- Textures



CNN for Scene Recognition

Places Database: 7 million images from 400 scene categories



Places-CNN: AlexNet CNN on 2.5 million images from 205 scene categories.

	Places 205	SUN 205
Places-CNN	50.0%	66.2%
ImageNet CNN feature+SVM	40.8%	49.6%

Scene Recognition Demo: 78% top-5 recognition accuracy in the wild



Predictions:

- **type:** indoor
- **semantic categories:**
coffee_shop:0.47, restaurant:0.17,
cafeteria:0.08, food_court:0.06



Predictions:

- **type:** indoor
- **semantic categories:**
conference_center:0.51,
auditorium:0.12, office:0.08,

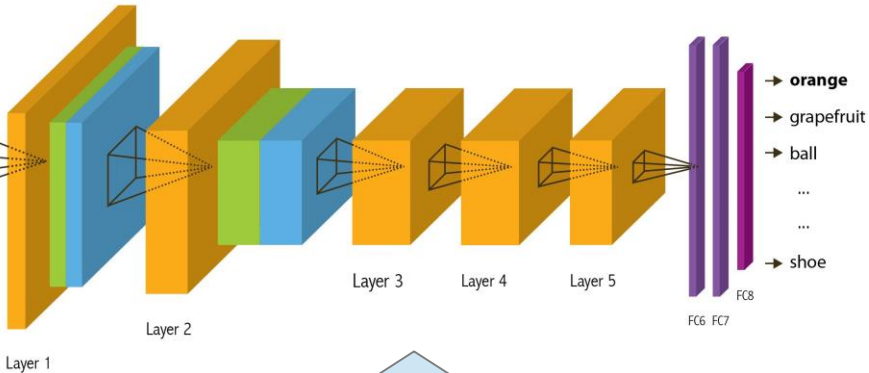
<http://places.csail.mit.edu>

ImageNet CNN and Places CNN

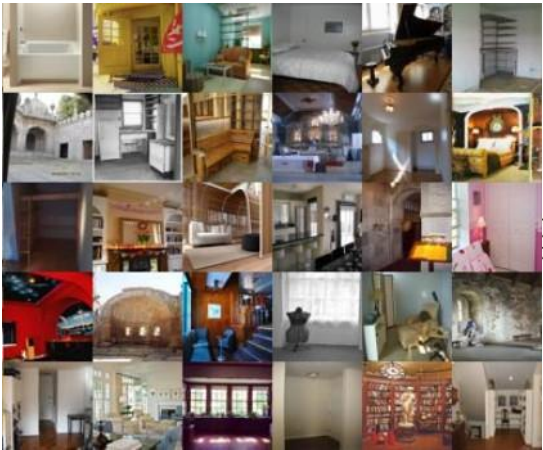


IMAGENET

ImageNet CNN for Object Classification

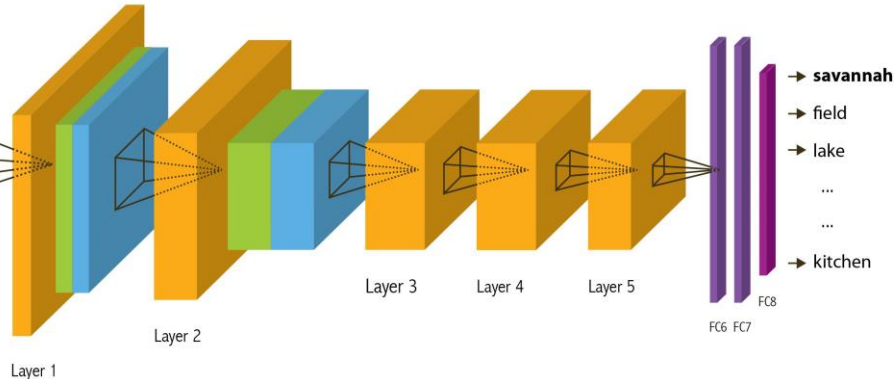


Same architecture: AlexNet



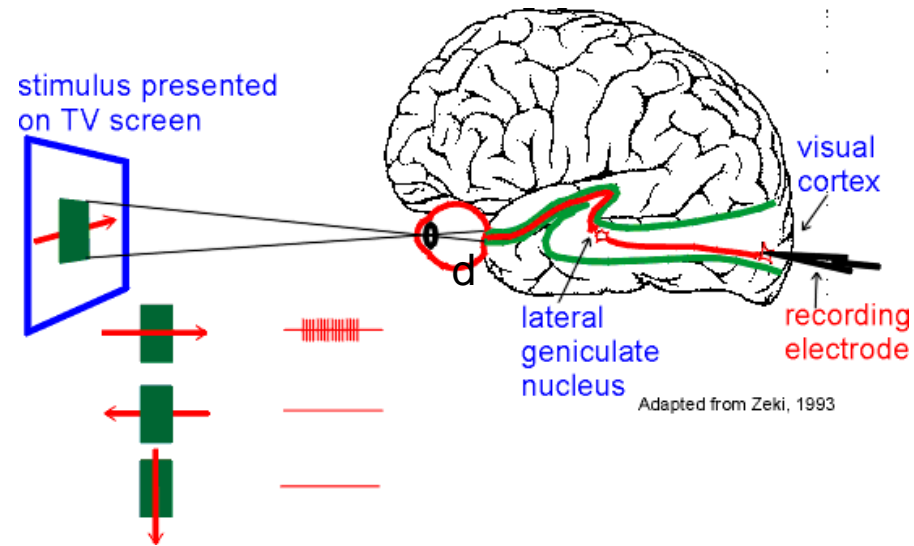
Places

Places CNN for Scene Classification

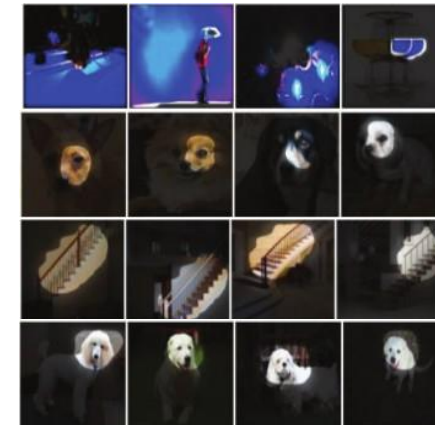
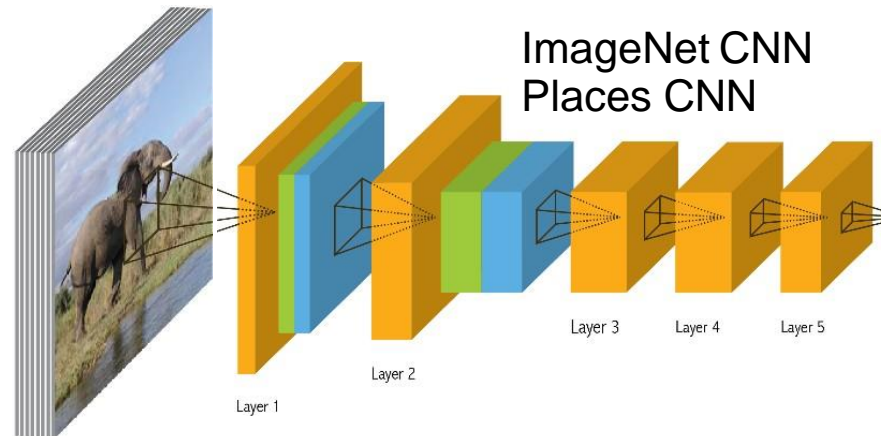


Data-Driven Approach to Study CNN

Neuroscientists study brain



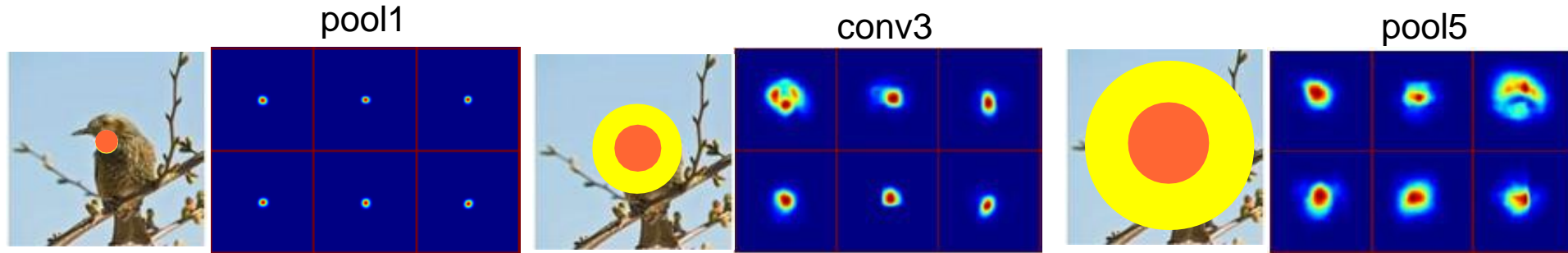
200,000 image stimuli of objects and scene categories (ImageNet TestSet+SUN database)



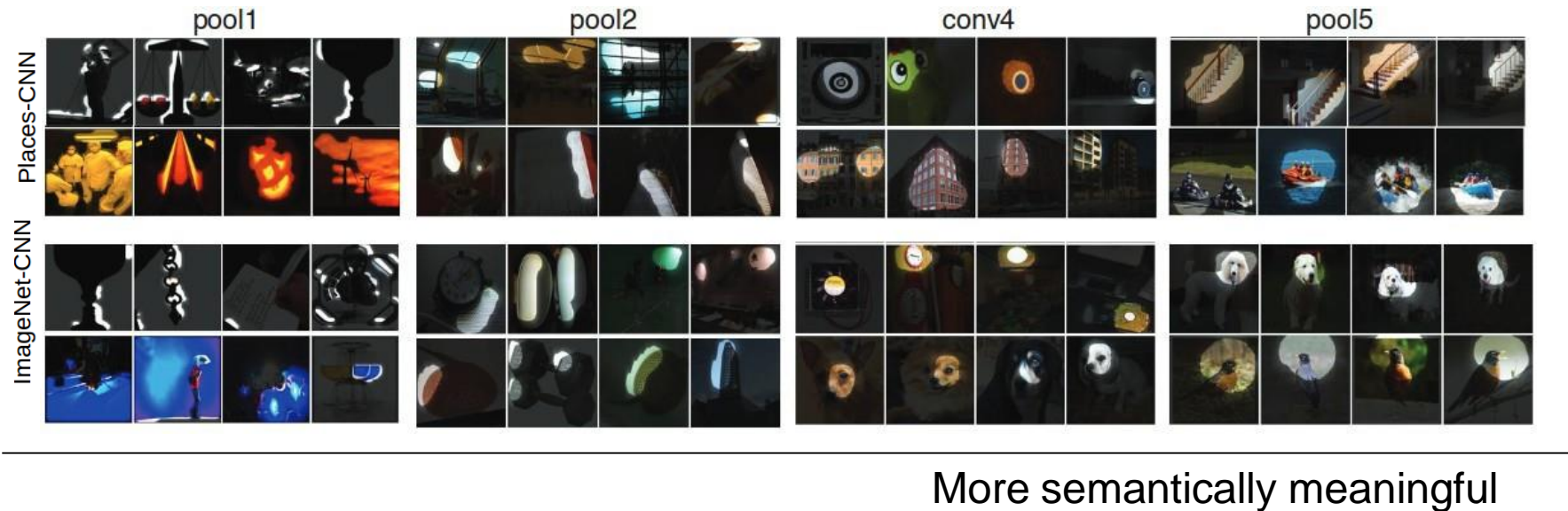
Estimating the Receptive Fields

Estimated receptive fields

Actual size of RF is much smaller than the theoretic size



Segmentation using the RF of Units



Annotating the Semantics of Units

Top ranked segmented images are cropped and sent to Amazon Turk for annotation.

Task 1

Word/Short description:

lower

Task 2

Mark (by clicking on them) the images which don't correspond to the short description you just wrote



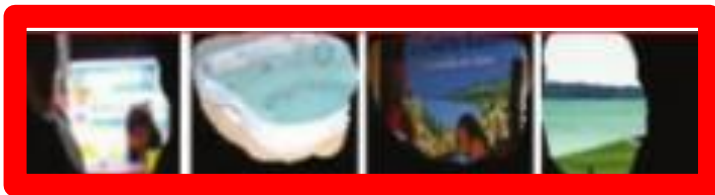
Task 3

Which category does your short description mostly belong to?

- Scene (kitchen, corridor, street, beach, ...)
- Region or surface (road, grass, wall, floor, sky, ...)
- Object (bed, car, building, tree, ...)
- Object part (leg, head, wheel, roof, ...)
- Texture or material (striped, rugged, wooden, plastic, ...)
- Simple elements or colors (vertical line, curved line, color blue, ...)

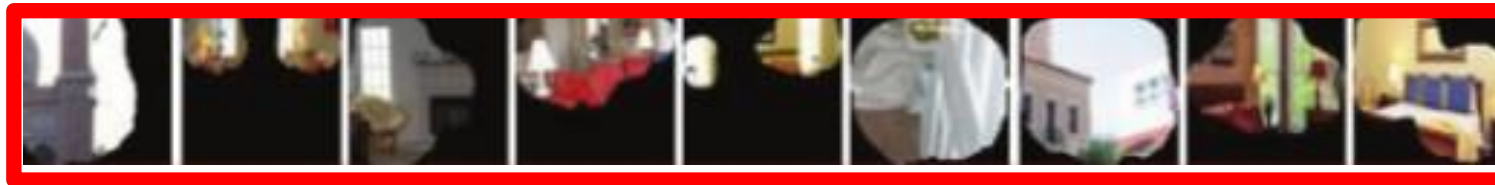
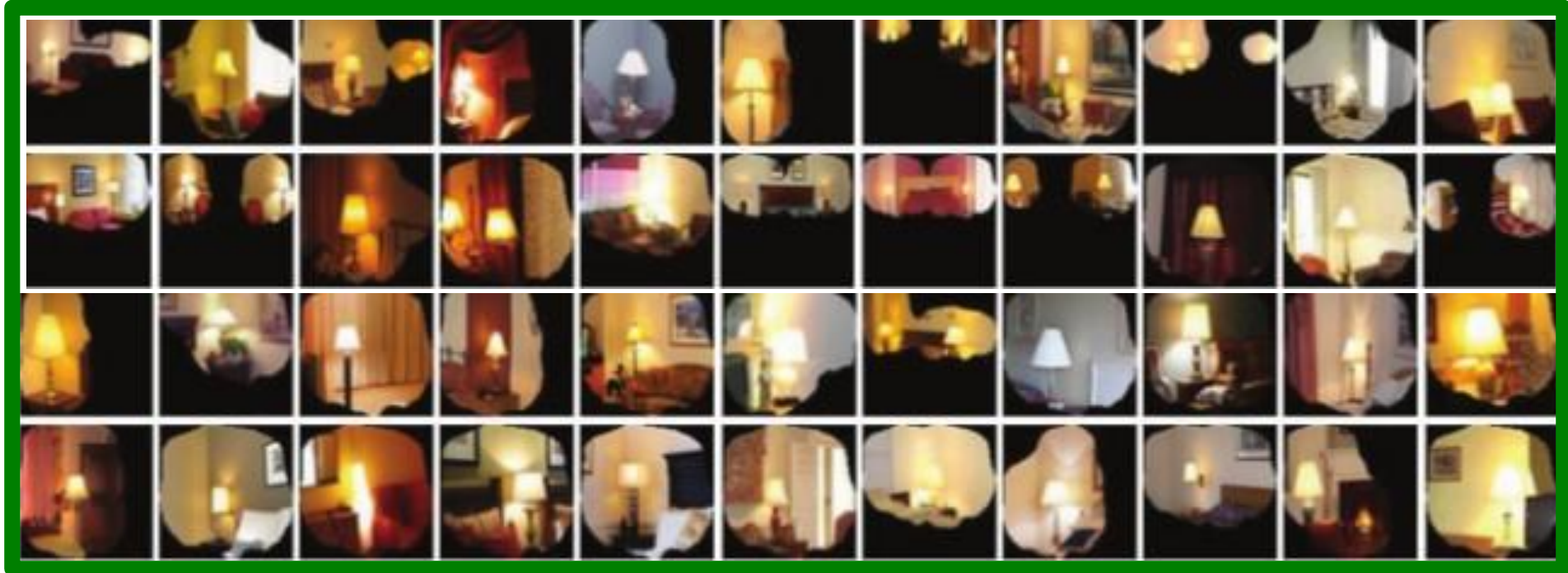
Annotating the Semantics of Units

Pool5, unit 76; Label: ocean; Type: scene; Precision: 93%



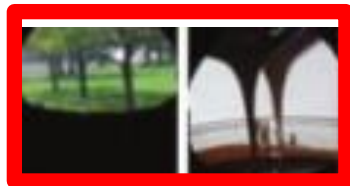
Annotating the Semantics of Units

Pool5, unit 13; Label: Lamps; Type: object; Precision: 84%



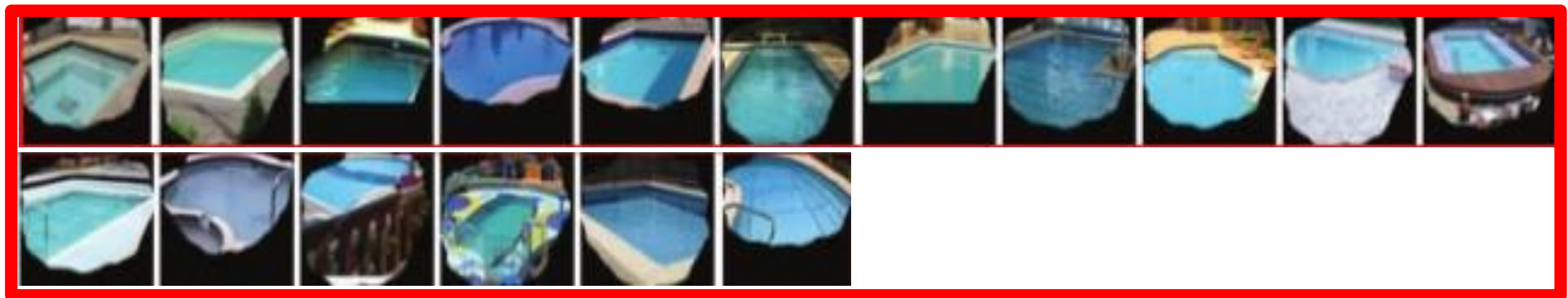
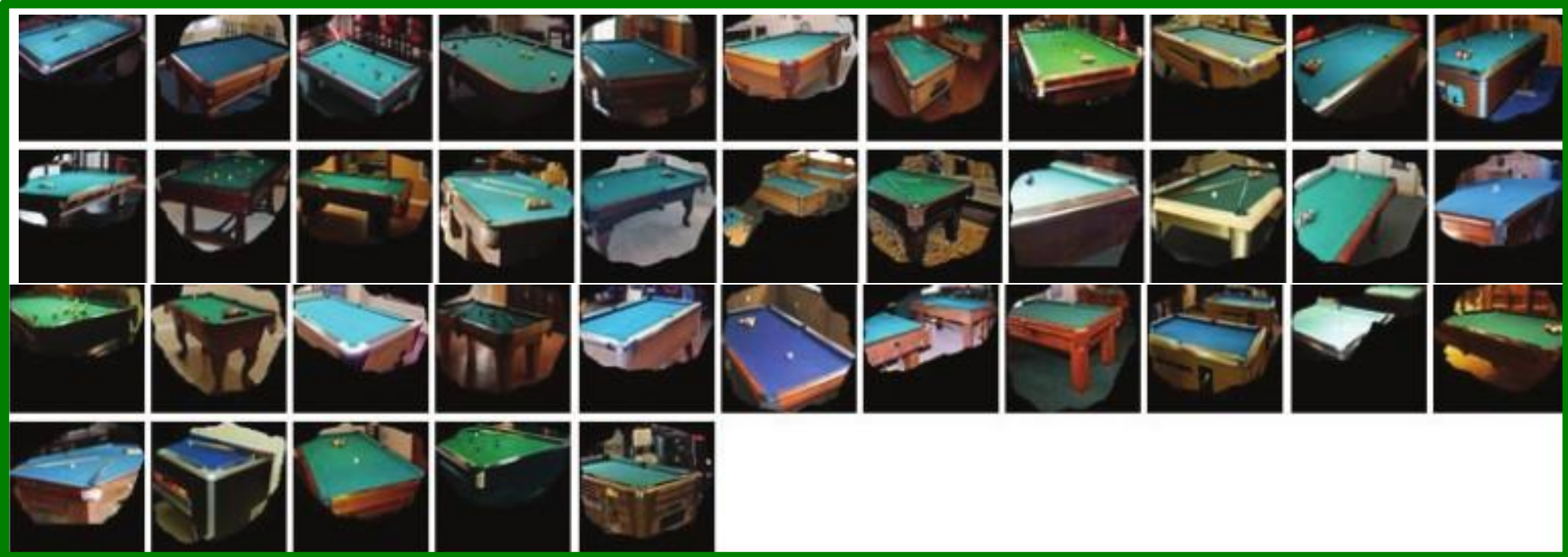
Annotating the Semantics of Units

Pool5, unit 77; Label: legs; Type: object part; Precision: 96%



Annotating the Semantics of Units

Pool5, unit 112; Label: pool table; Type: object; Precision: 70%

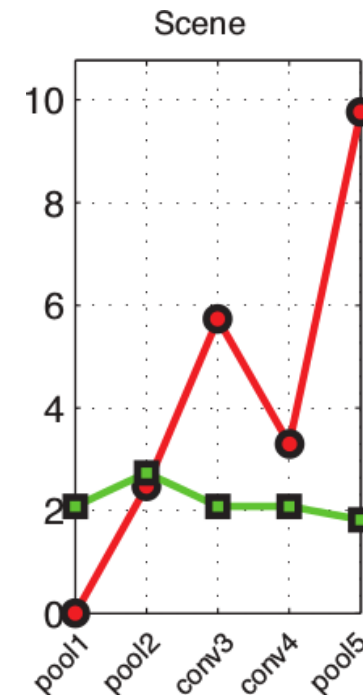
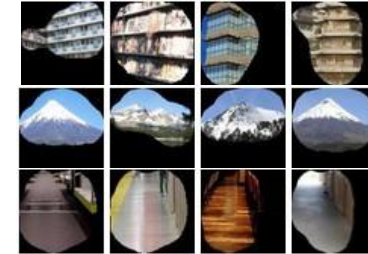
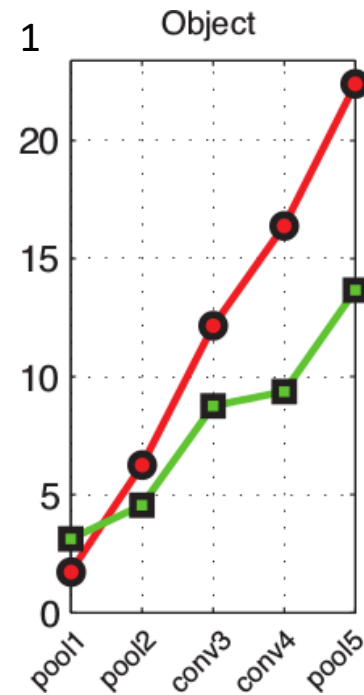
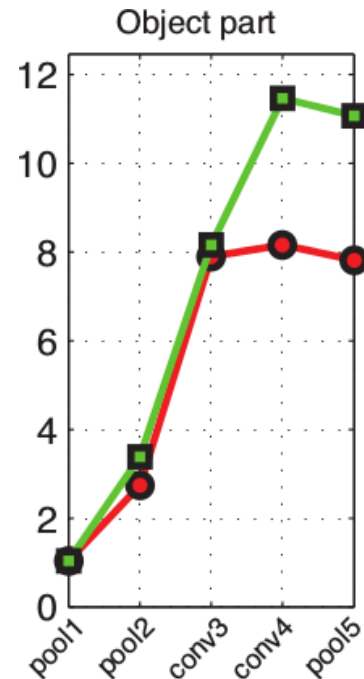
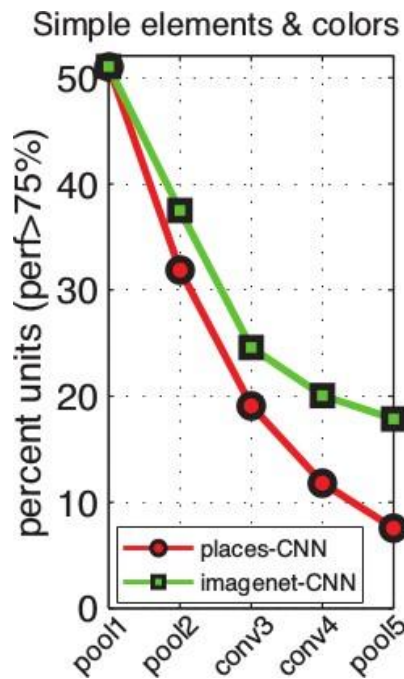
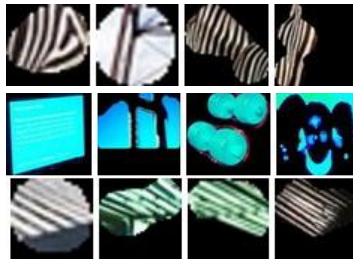


Annotating the Semantics of Units

Pool5, unit 22; Label: dinner table; Type: scene; Precision: 60%



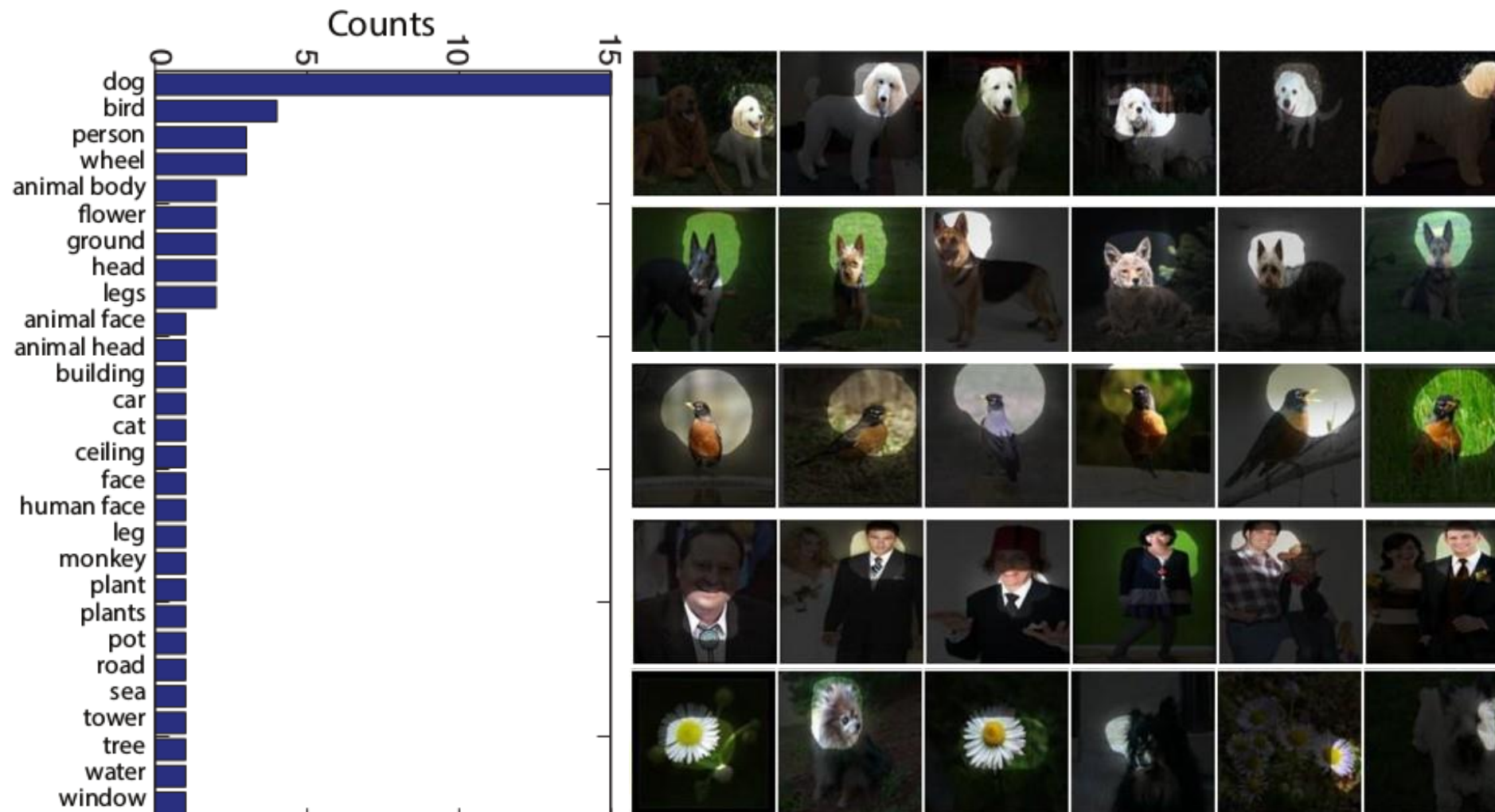
Distribution of Semantic Types at Each Layer



Object detectors emerge within CNN trained to classify scenes, without any object supervision!

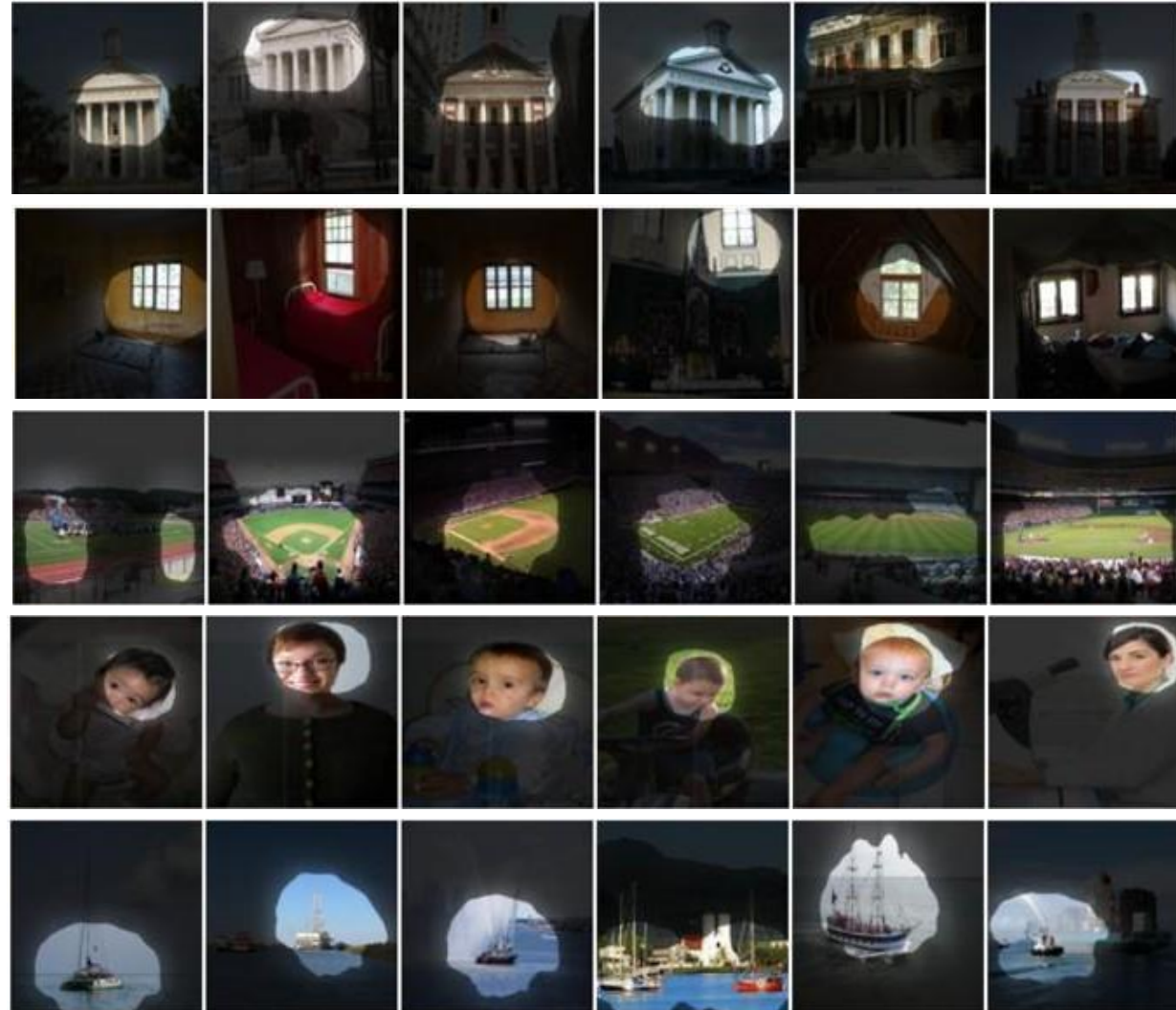
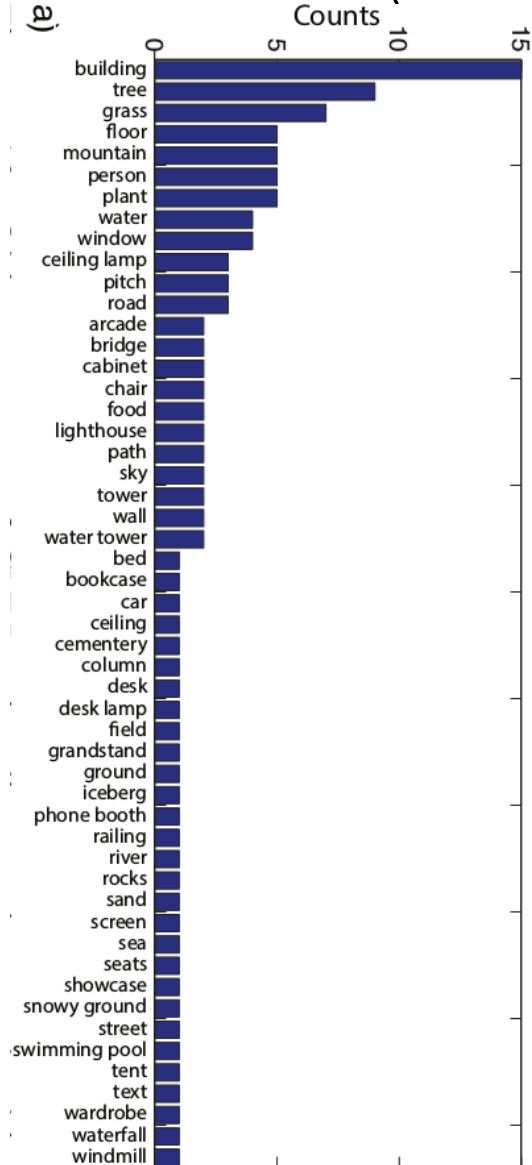
Histogram of Emerged Objects in Pool5

ImageNet-CNN (59/256)



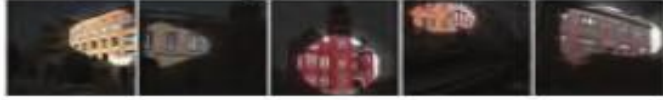
Histogram of Emerged Objects in Pool5

Places-CNN (151/256)



Buildings

56) building



120) arcade



8) bridge



123) building



119) building



9) lighthouse

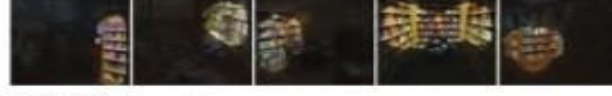


Furniture

18) billard table



155) bookcase



116) bed



38) cabinet



85) chair



People

3) person



49) person



138) person



100) person



Lighting

55) ceiling lamp



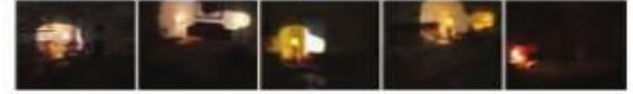
174) ceiling lamp



223) ceiling lamp



13) desk lamp



Nature

195) grass



89) iceberg



140) mountain

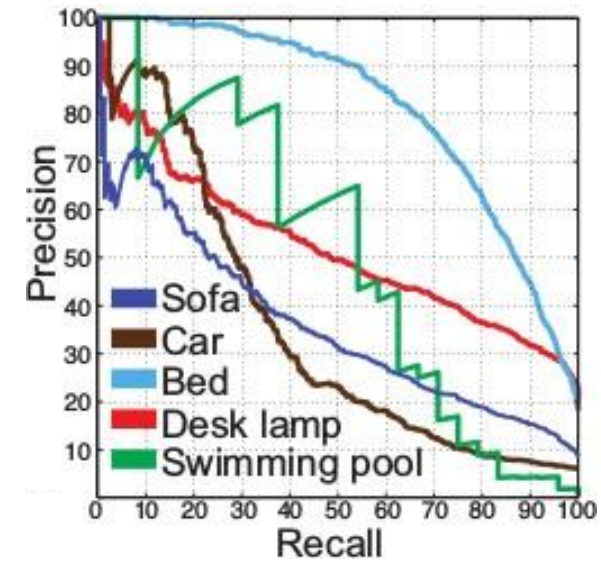
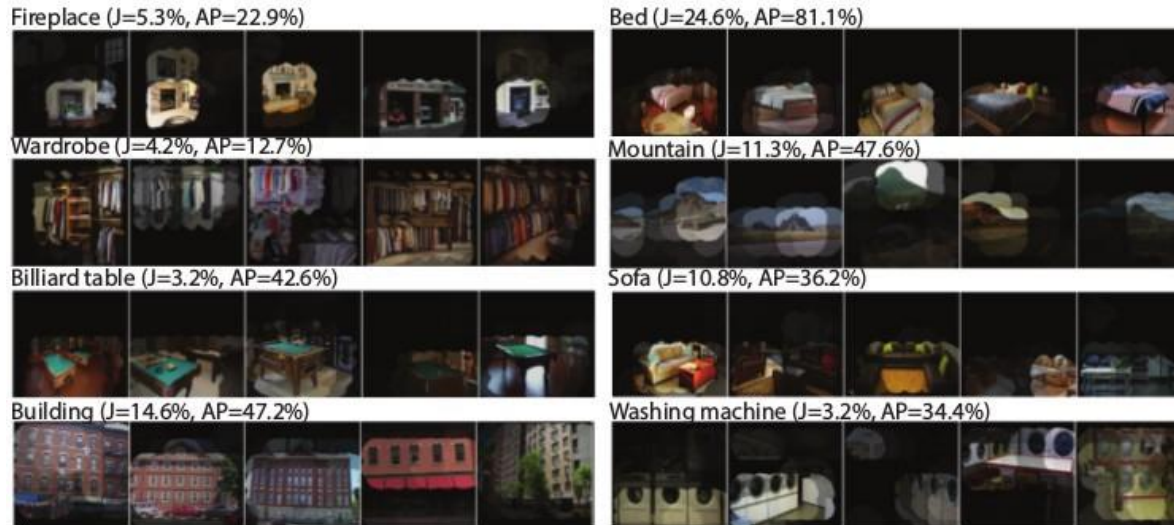


159) sand

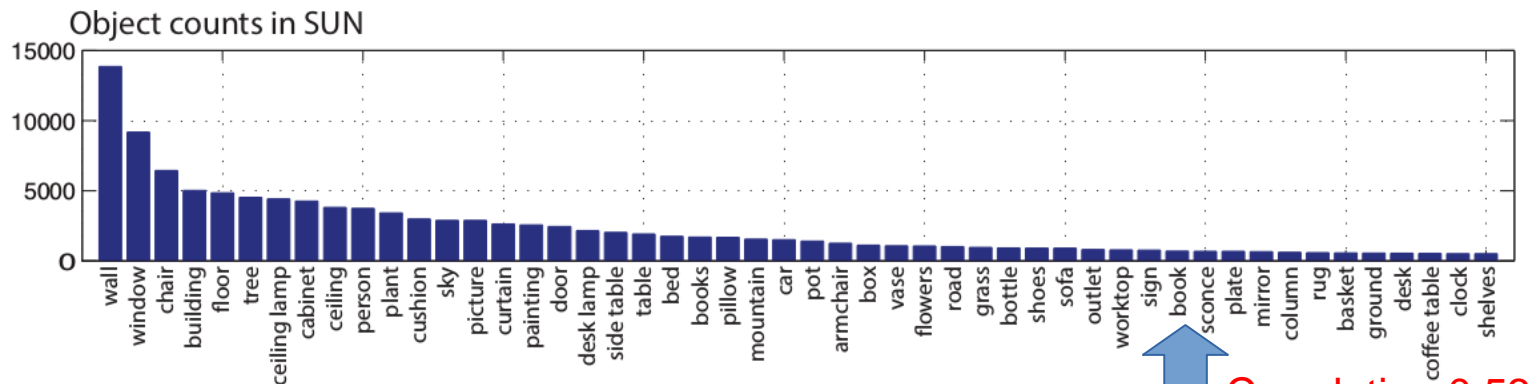


Evaluation on SUN Database

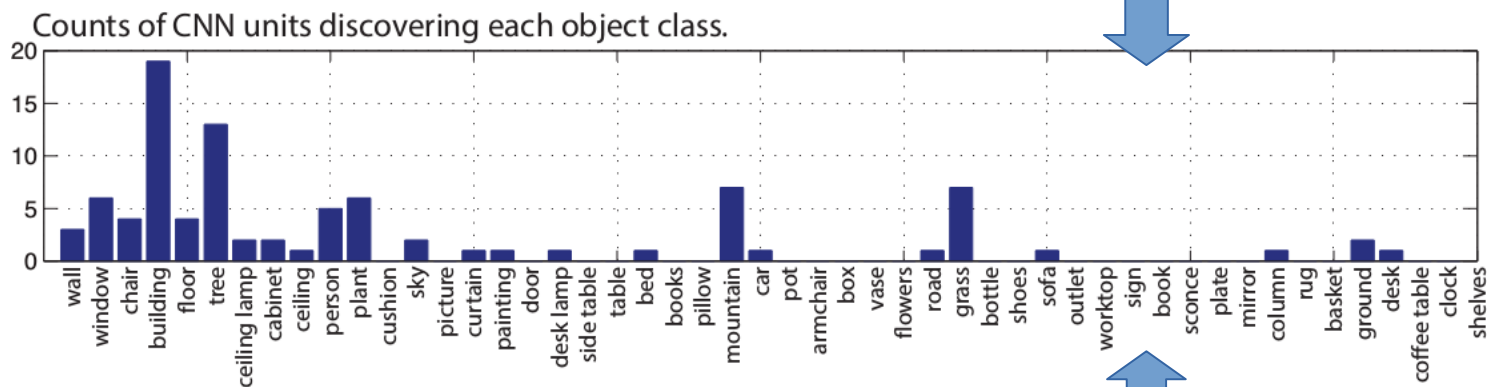
Evaluate the performance of the emerged object detectors



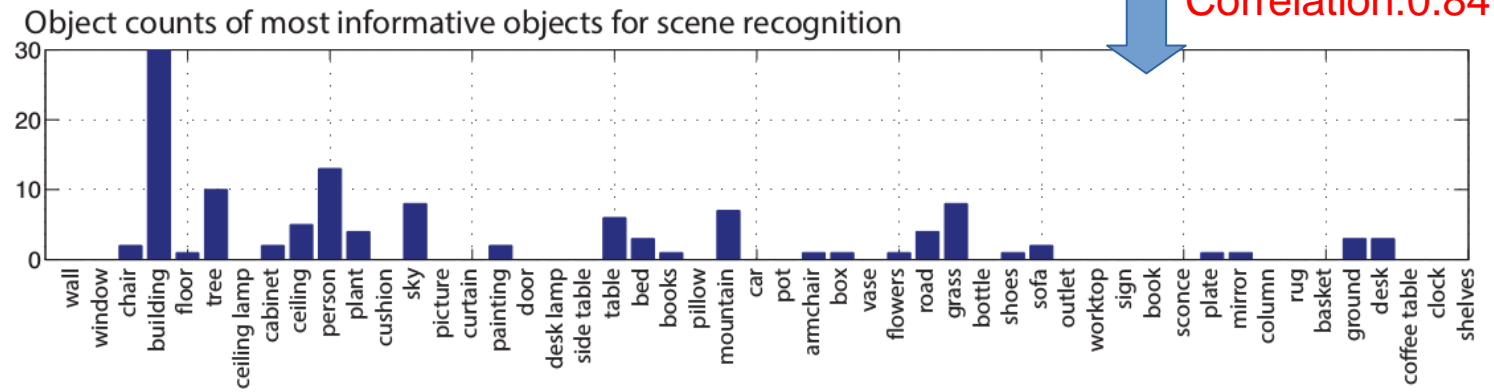
Evaluation on SUN Database



Correlation:0.53



Correlation:0.84





Conclusion



We show that object detectors emerge inside a CNN trained to classify scenes, without any object supervision.

Object detectors for free!



Places database, Places CNN, and unit annotations could be downloaded at

<http://places.csail.mit.edu>