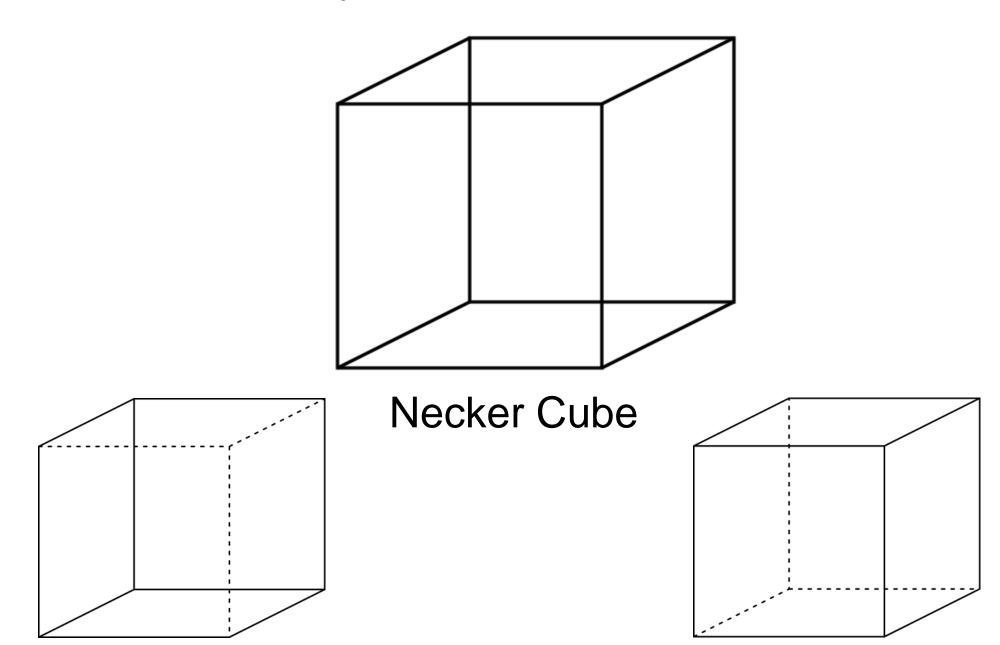
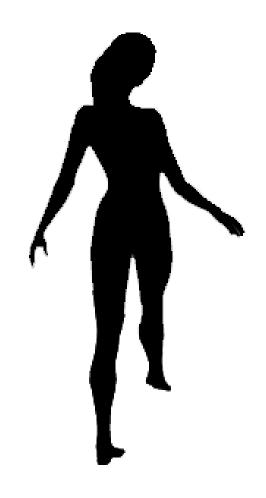
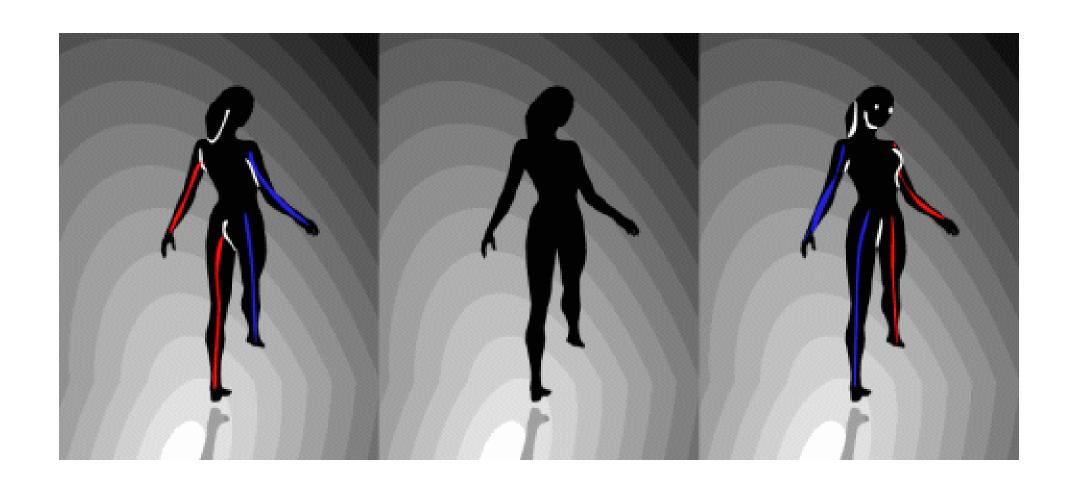
Multi-stable Perception







Feature Matching and Robust Fitting

Read Szeliski 7.4.2 and 2.1

Computer Vision

James Hays

Project 2

. Take two images of a building or structure near you. Save them in the additional data/ folder of the project and run your SIFT pipeline on them. Analyze the results - why do you think our pipeline may have performed well or poorly for the given image pair? Is there anything about the building that is helpful or detrimental to feature matching?

Algorithm 1: Harris Corner Detector

natching – multiple views of the same physical

ity checks are passing by running pytest tests

ubmission once you've finished the project using

s of a local feature matching algorithm (detecting

atching feature vectors). We'll implement two

patch feature in part2_patch_descriptor.py (see

rt4_sift_descriptor.py (see Szeliski 7.1.2)

d in the lecture materials and Szeliski 7.1.1.

screte convolutions with the weighting kernel w

r environment installation

2.ipynb

anized as follows:

see Szeliski 7.1.1)

Szeliski 7.1.3)

_corner.py)

ion 7.8 of book, p. 424)

 $\begin{bmatrix} I_x \\ I \end{bmatrix} \begin{bmatrix} I_x & I_y \end{bmatrix}$

tion matrix A as:

 $ace(A)^2$

The goal of this assignment is to create a local feature matching algorithm using techniques described in

Compute the horizontal and vertical derivatives I_x and I_y of the image by convolving the original image with a Sobel filter:

Compute the three images corresponding to the outer products of these gradients. (The matrix A is

er Gaussian

the formulas (Equation 2) discussed above.; hold and report them as detected feature point locations.:

will have to fill out the following methods in part1_harris_corner

image gradients using the Sobel filter.

the raw corner responses over the entire image (the previously

maximum suppression using max-pooling. You can use PyTorch

interests points from the entire image (the previously imple-

nethods in part1_harris_corner.py:

reates a 2D Gaussian kernel (this is essentially the same as your

ond moments of the input image. This makes use of your

oling operation using just NumPy. This manual implementation

s close to the border that we can't create a useful SIFT window

gestions. You do not need to worry about scale invariance or eline Harris corner detector. The original paper by Chris Harris etector can be found here.

escriptors (part2_patch_descriptor.py)

nickly, you will implement a bare-bones feature descriptor in , grayscale image intensity patches as your local feature. See ompute_normalized_patch_descriptors()

e choices for center of a square window, as shown in Figure

patches on Notre Dame is around 40-45% and Mt Rushmore

$\lg (part3_feature_matching.py)$

nown as the "nearest neighbor distance ratio test") method of lecture materials and Szeliski 7.1.3 (page 444). See equation at pass the ratio test the easiest should have a greater tendency

dow, the vellow cells could all be considered the center. Please nter throughout this project.

this is. In part3_feature_matching.py, you will have to code e feature distances, and match_features_ratio_test() to perform feature lists.

(part4_sift_descriptor.py)

as described in the lecture materials and Szeliski 7.1.2. We'll e-Root SIFT") from a 2012 CVPR paper (linked here) to get a ts in the file part4_sift_descriptor.py for more details.

histograms. An unweighted 1D histogram with 3 bins could 1, 2.5, 5.8, 5.9, and the bins are defined over half-open intervals am h = [2, 1, 2].

bins and bin edges has each item weighted by some value. [5.8, 5.9], with weights w = [2, 3, 1, 0, 0], and the same bin edges ogram weight at a pixel is the magnitude of the image gradient

to implement the following:

Retrieves gradient magnitudes and orientations of the image.

ch (): Retrieves a feature consisting of concatenated histograms.

ture from a single point.

ure vectors corresponding to our interest points from an image.

pipeline on the Notre Dame image is at least 80%. Note that (close to 0) and think about why this could be happening.

Exploration

rameters: How big should the window around each feature be? How many orientations should each histogram have? Modify out the corresponding items in the report.

do a project report using the template slides provided emove any slides, as this will affect the grading process In the report you will describe your algorithm and any cular way. Then you will show and discuss the results of nce for what you should include in your report. A good me conclusions from the experiments. You must convert d then assign each PDF page to the relevant question

r the slides given in the template deck to describe your receive full credit for your extra credit implementations

rovided in the starter code includes file handling, visualcalls to placeholder versions of the three functions listed

ruth evaluation in the starter code as well. evaluate_ ct or incorrect based on hand-provided matches . The ences for two other image pairs (Mount Rushmore and incommenting the appropriate lines in project-2.ipynb.

you should see your performance according to evaluate_ useful, but don't overfit to the initial Notre Dame image m suggested here and in the starter code will give you

functions

atenate(), np.fliplr(), np.flipud(), np.histogram(), ewaxis, np.reshape(), np.sort().

ch.from_numpy(), torch.median(), torch.nn.functional , torch.nn.Parameter, torch.stack().

ementation, you might find torch.meshgrid, torch.norm,

Please use torch.nn.Conv2d OF torch.nn.functional nctions from other libraries (e.g., cv.filter2D(), scipy.

Szeliski chapter 7.1. The pipeline we suggest is a simplified version of the famous SIFT pipeline. The Project 2: SIFT Local Feature Matching

Overview

CS 4476

Fall 2023

Brief

• Due: Check Canvas for up to date information

• Project materials including report template: Project 2

Hand-in: through Gradescope

• Required files: <your_gt_username>.zip, <your_gt_username>_proj2.pdf

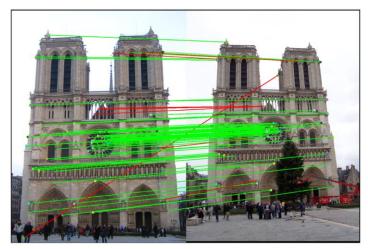
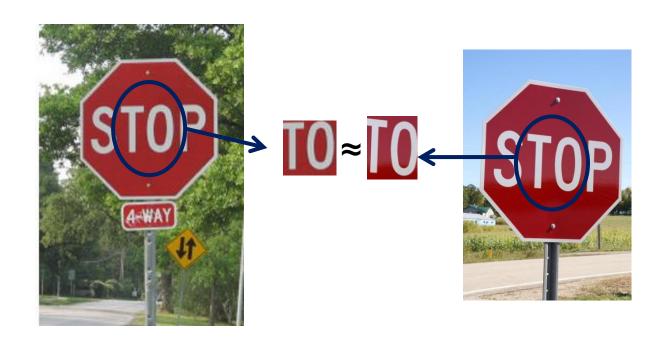


Figure 1: The top 100 most confident local feature matches from a baseline implementation of project 2. In this case, 89 were correct (lines shown in green), and 11 were incorrect (lines shown in red).

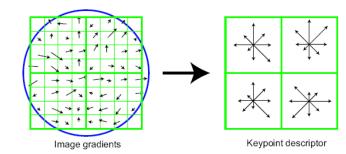
This section: correspondence and alignment

 Correspondence: matching points, patches, edges, or regions across images



Review: Local Descriptors

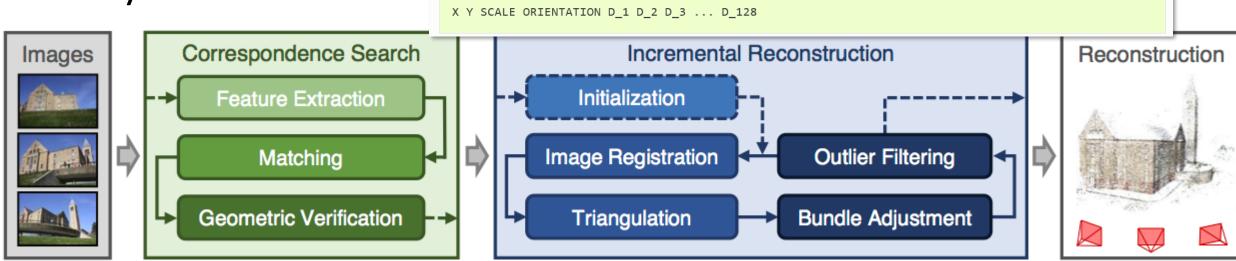
- Most features can be thought of as templates, histograms (counts), or combinations
- The ideal descriptor should be
 - Robust and Distinctive
 - Compact and Efficient



- Most available descriptors focus on edge/gradient information
 - Capture texture information
 - Color rarely used

What is "Geometric Verification"?

 COLMAP is the standard way to do structure from motion these days You can either detect and extract new features from the images or import existing features from text files. COLMAP extracts SIFT [lowe04] features either on the GPU or the CPU. The GPU version requires an attached display, while the CPU version is recommended for use on a server. In general, the GPU version is favorable as it has a customized feature detection mode that often produces higher quality features in the case of high contrast images. If you import existing features, every image must have a text file next to it (e.g., /path/to/image1.jpg and /path/to/image1.jpg.txt) in the following format:

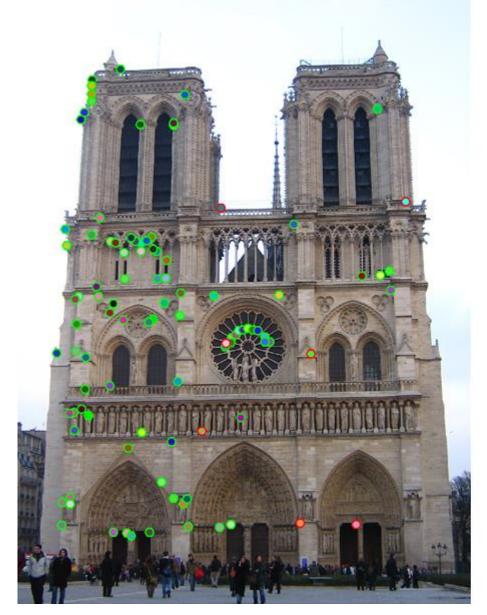


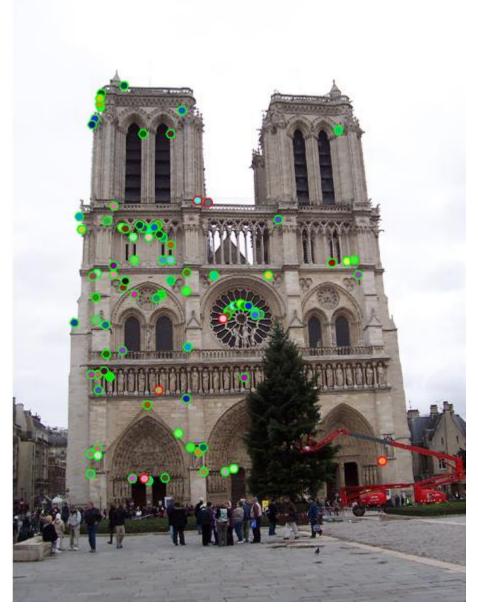
X Y SCALE ORIENTATION D_1 D_2 D_3 ... D_128

"Structure-From-Motion Revisited". Johannes L. Schonberger, Jan-Michael Frahm; CVPR 2016 5k+ citations

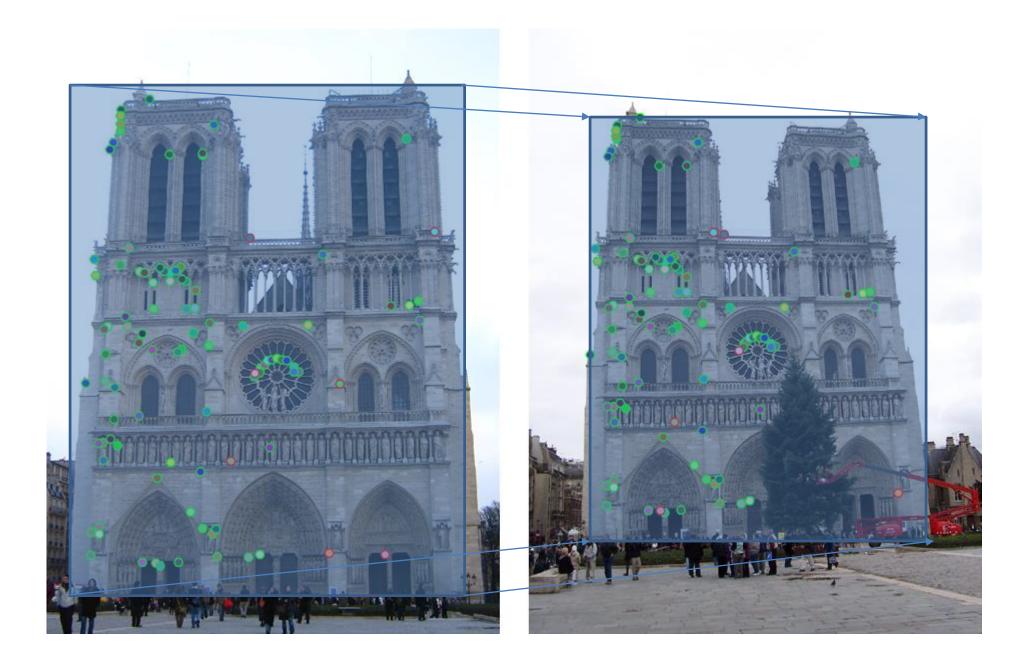
NUM FEATURES 128

Can we refine this further?

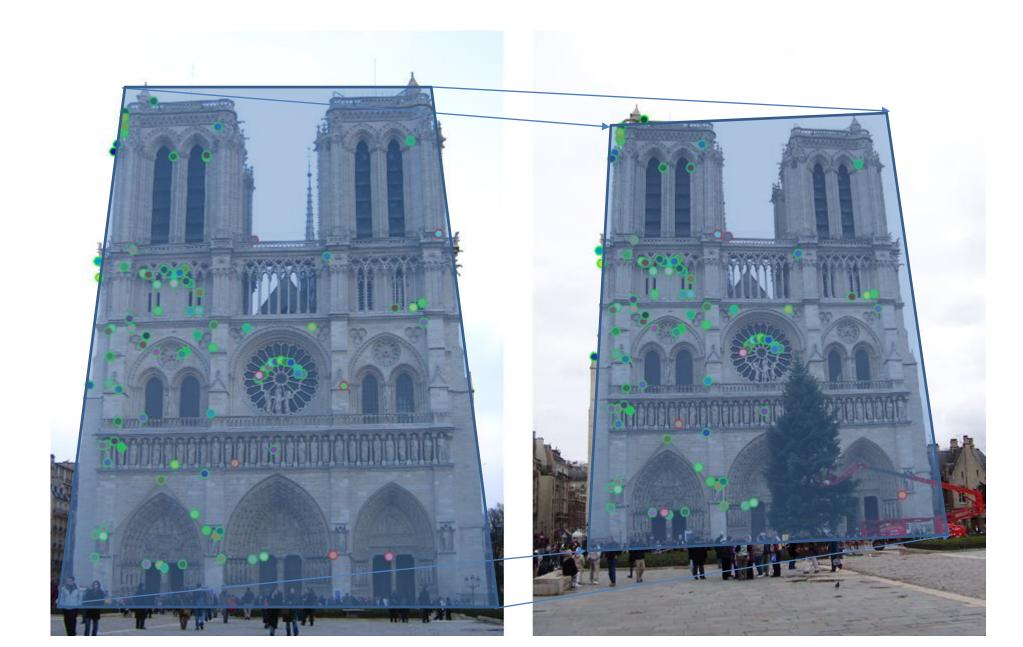




Can we refine this further?



Can we refine this further?



Fitting: find the parameters of a model that best fit the data

Alignment: find the parameters of the transformation that best align matched points

Fitting and Alignment

- Design challenges
 - Design a suitable goodness of fit measure
 - Similarity should reflect application goals
 - Encode robustness to outliers and noise
 - Design an optimization method
 - Avoid local optima
 - Find best parameters quickly

Fitting and Alignment: Methods

- Global optimization / Search for parameters
 - Least squares fit
 - Robust least squares
 - Other parameter search methods
- Hypothesize and test
 - Generalized Hough transform
 - RANSAC
- Iterative Closest Points (ICP)

Fitting and Alignment: Methods

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Simple example: Fitting a line

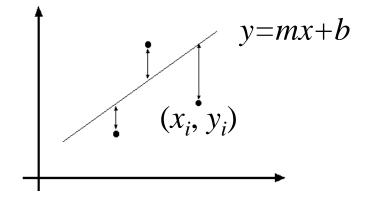
Least squares line fitting

•Data: $(x_1, y_1), ..., (x_n, y_n)$

•Line equation: $y_i = mx_i + b$

•Find (*m*, *b*) to minimize

$$E = \sum_{i=1}^{n} (y_i - mx_i - b)^2$$



$$E = \sum_{i=1}^{n} \left(\begin{bmatrix} x_i & 1 \end{bmatrix} \begin{bmatrix} m \\ b \end{bmatrix} - y_i \right)^2 = \begin{bmatrix} x_1 & 1 \\ \vdots & \vdots \\ x_n & 1 \end{bmatrix} \begin{bmatrix} m \\ b \end{bmatrix} - \begin{bmatrix} y_1 \\ \vdots \\ y_n \end{bmatrix} = \|\mathbf{A}\mathbf{p} - \mathbf{y}\|^2$$

$$= \mathbf{y}^T \mathbf{y} - 2(\mathbf{A}\mathbf{p})^T \mathbf{y} + (\mathbf{A}\mathbf{p})^T (\mathbf{A}\mathbf{p})$$

Matlab: $p = A \setminus y$;

$$\frac{dE}{dp} = 2\mathbf{A}^T \mathbf{A} \mathbf{p} - 2\mathbf{A}^T \mathbf{y} = 0$$
 Python: p =

numpy.linalg.lstsq(A, y)

$$\mathbf{A}^T \mathbf{A} \mathbf{p} = \mathbf{A}^T \mathbf{y} \Longrightarrow \mathbf{p} = (\mathbf{A}^T \mathbf{A})^{-1} \mathbf{A}^T \mathbf{y}$$

Least squares (global) optimization

Good

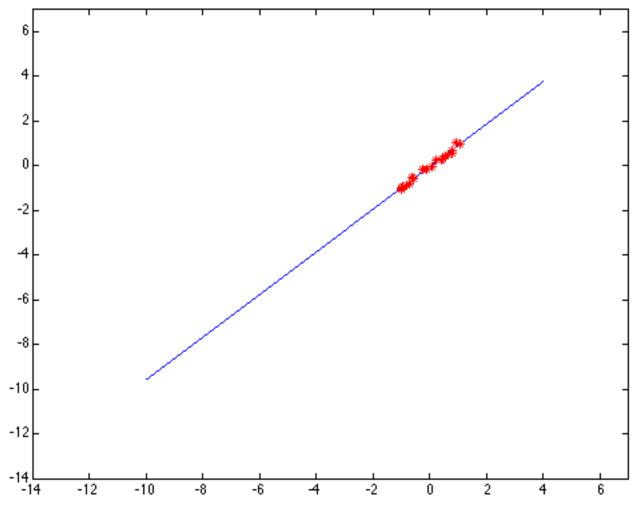
- Clearly specified objective
- Optimization is easy

Bad

- May not be what you want to optimize
- Sensitive to outliers
 - Bad matches, extra points
- Doesn't allow you to get multiple good fits
 - Detecting multiple objects, lines, etc.

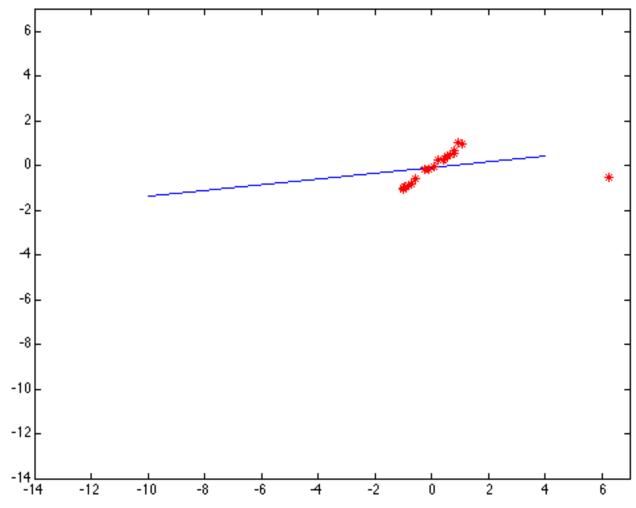
Least squares: Robustness to noise

• Least squares fit to the red points:



Least squares: Robustness to noise

• Least squares fit with an outlier:



Problem: squared error heavily penalizes outliers

Fitting and Alignment: Methods

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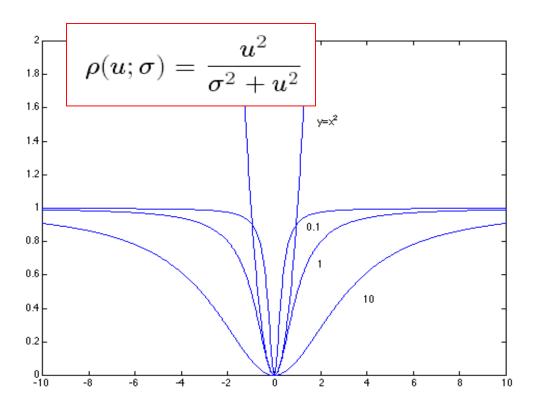
Robust least squares (to deal with outliers)

General approach:

minimize

$$\sum_{i} \rho(\mathbf{u}_{i}(\mathbf{x}_{i},\boldsymbol{\theta});\boldsymbol{\sigma}) \qquad u^{2} = \sum_{i=1}^{n} (y_{i} - mx_{i} - b)^{2}$$

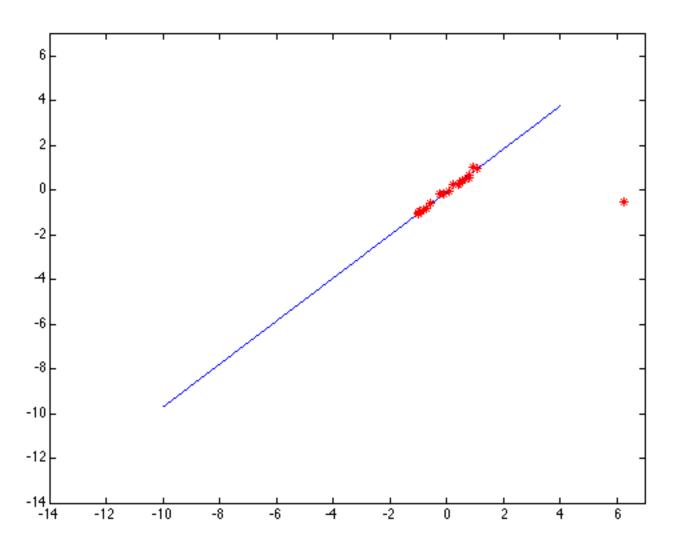
 $u_i(x_i, \theta)$ – residual of ith point w.r.t. model parameters ϑ ρ – robust function with scale parameter σ



The robust function ρ

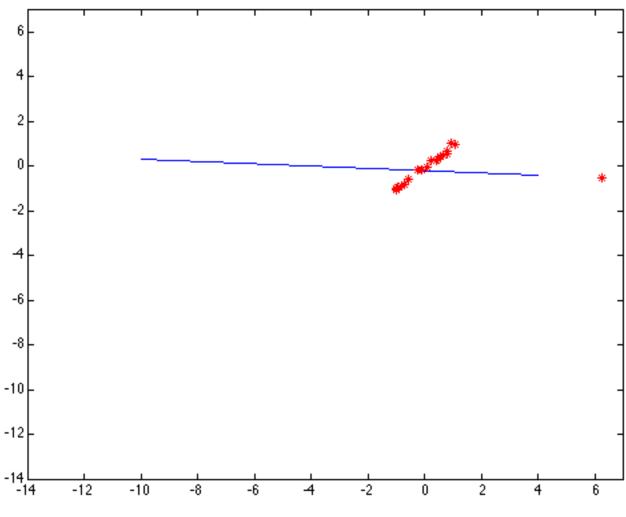
- Favors a configuration with small residuals
- Constant penalty for large residuals

Choosing the scale: Just right



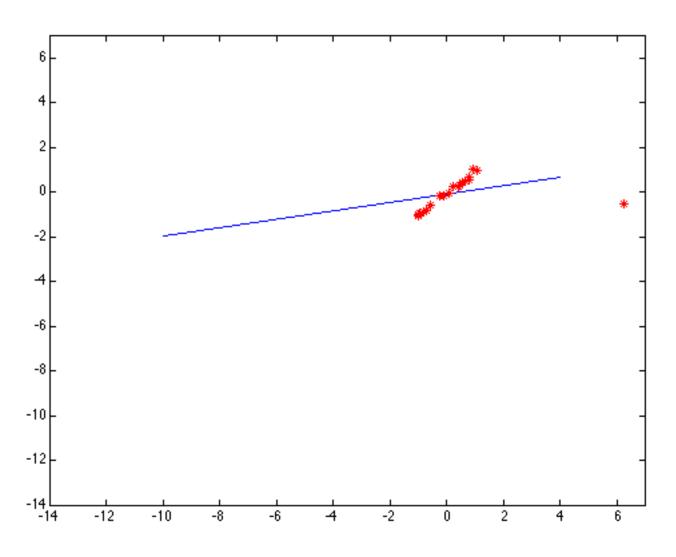
The effect of the outlier is minimized

Choosing the scale: Too small



The error value is almost the same for every point and the fit is very poor

Choosing the scale: Too large



Behaves much the same as least squares

Robust estimation: Details

- Robust fitting is a nonlinear optimization problem that must be solved iteratively
- Least squares solution can be used for initialization
- Scale of robust function should be chosen adaptively based on median residual

Fitting and Alignment: Methods

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Other ways to search for parameters (for when no closed form solution exists)

- Line search (see also "coordinate descent")
 - 1. For each parameter, step through values and choose value that gives best fit
 - 2. Repeat (1) until no parameter changes

Grid search

- 1. Propose several sets of parameters, evenly sampled in the joint set
- Choose best (or top few) and sample joint parameters around the current best; repeat

Gradient descent

- 1. Provide initial position (e.g., random)
- 2. Locally search for better parameters by following gradient

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Hough Transform: Outline

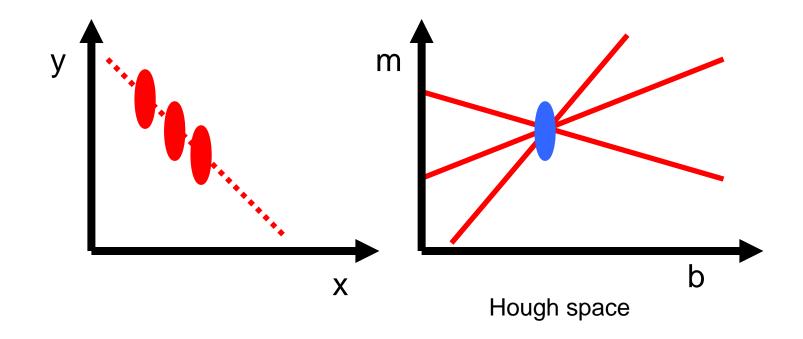
1. Create a grid of parameter values

2. Each point votes for a set of parameters, incrementing those values in grid

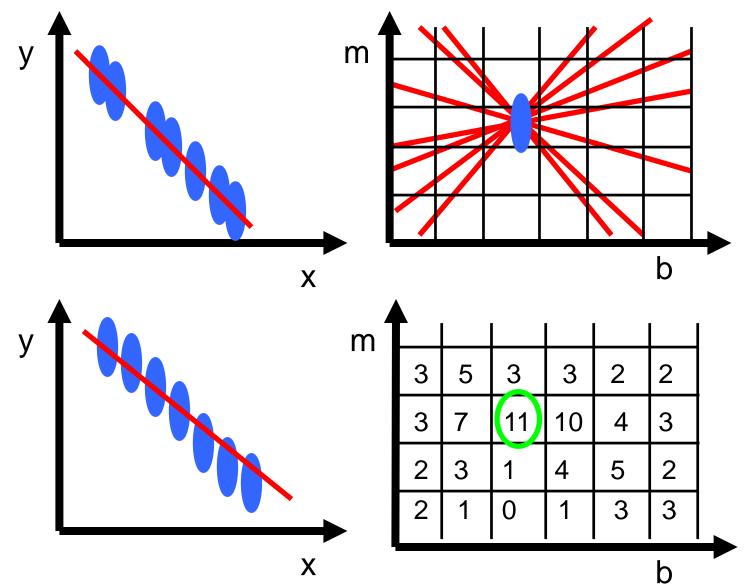
3. Find maximum or local maxima in grid

P.V.C. Hough, *Machine Analysis of Bubble Chamber Pictures*, Proc. Int. Conf. High Energy Accelerators and Instrumentation, 1959

Given a set of points, find the curve or line that explains the data points best



$$y = m x + b$$



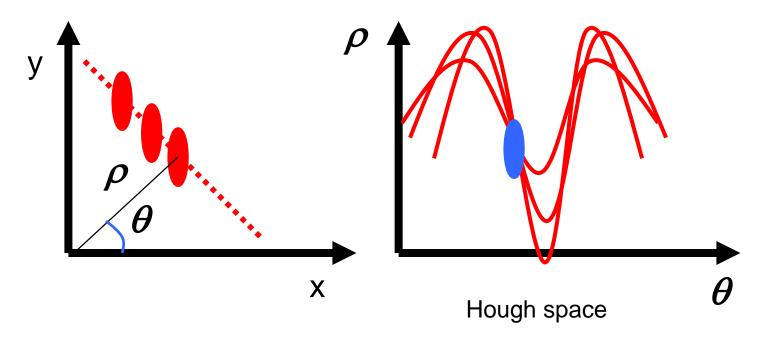
P.V.C. Hough, *Machine Analysis of Bubble Chamber Pictures,* Proc. Int. Conf. High Energy Accelerators and Instrumentation, 1959

Issue: parameter space [m,b] is unbounded...

P.V.C. Hough, *Machine Analysis of Bubble Chamber Pictures*, Proc. Int. Conf. High Energy Accelerators and Instrumentation, 1959

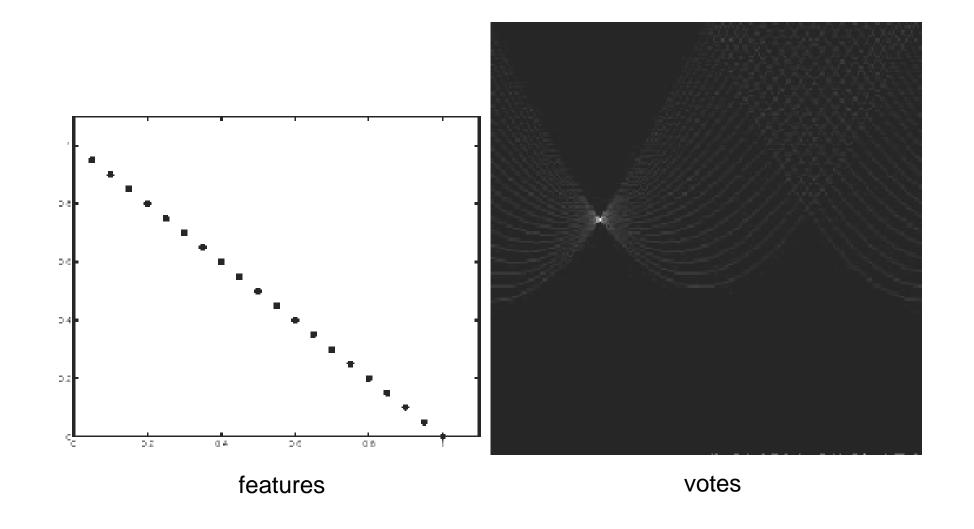
Issue: parameter space [m,b] is unbounded...

Use a polar representation for the parameter space

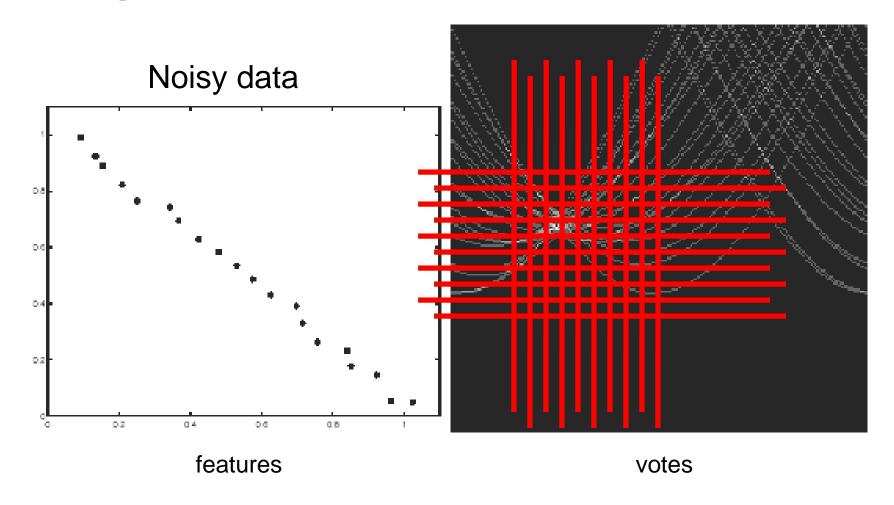


$$x\cos\theta + y\sin\theta = \rho$$

Hough transform - experiments

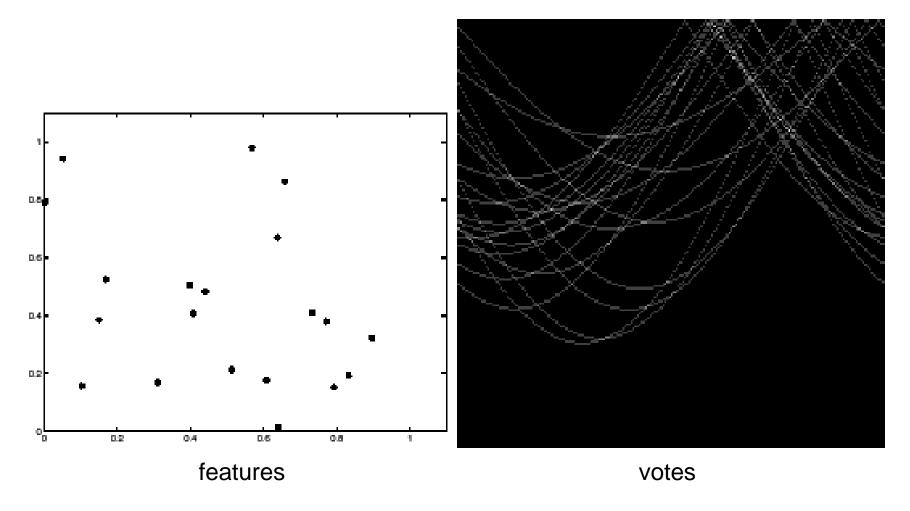


Hough transform - experiments



Need to adjust grid size or smooth

Hough transform - experiments



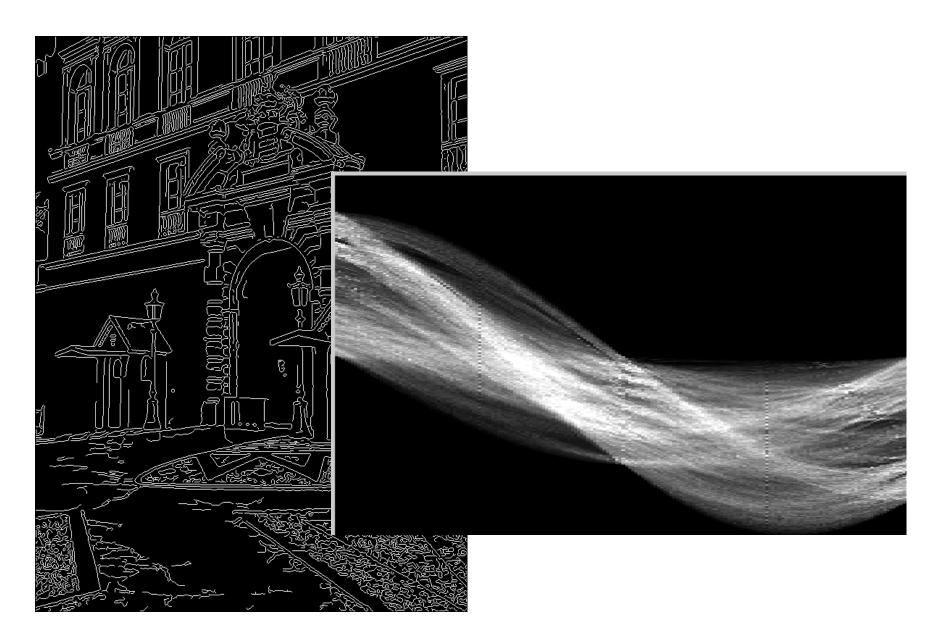
Issue: spurious peaks due to uniform noise

1. Image → Canny Edge Detection



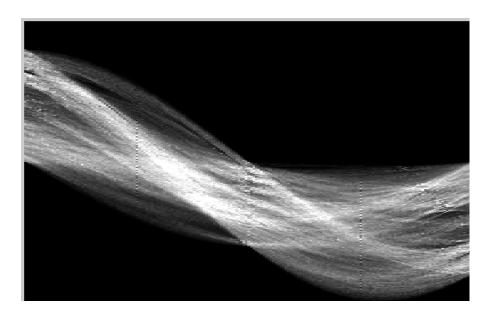


2. Canny → Hough votes



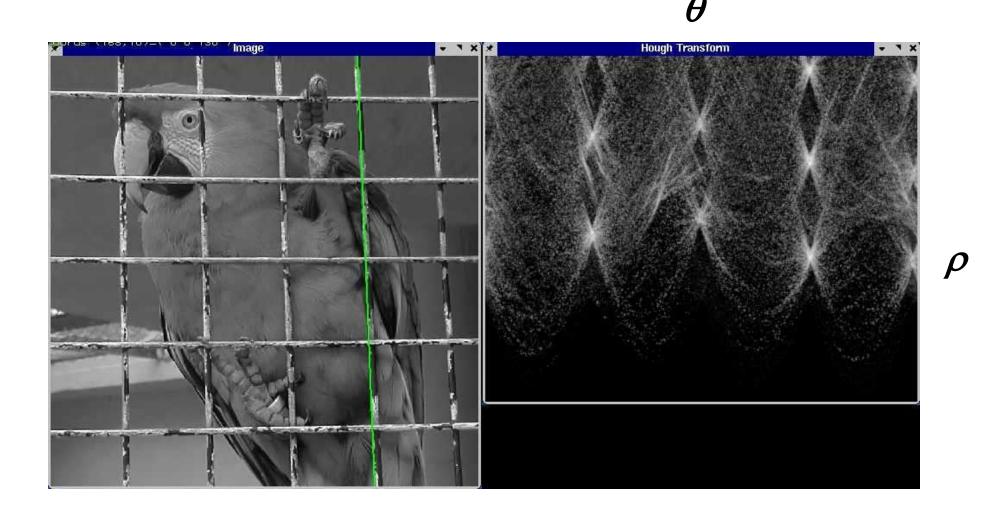
3. Hough votes → Edges

Find peaks and post-process





Hough transform example



Finding lines using Hough transform

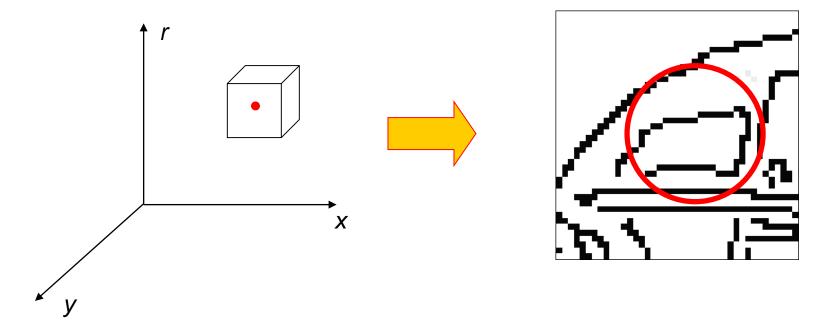
- Using m,b parameterization
- Using r, theta parameterization
 - Using oriented gradients
- Practical considerations
 - Bin size
 - Smoothing
 - Finding multiple lines
 - Finding line segments

Hough Transform

- How would we find circles?
 - Of fixed radius
 - Of unknown radius
 - Of unknown radius but with known edge orientation

Hough transform for circles

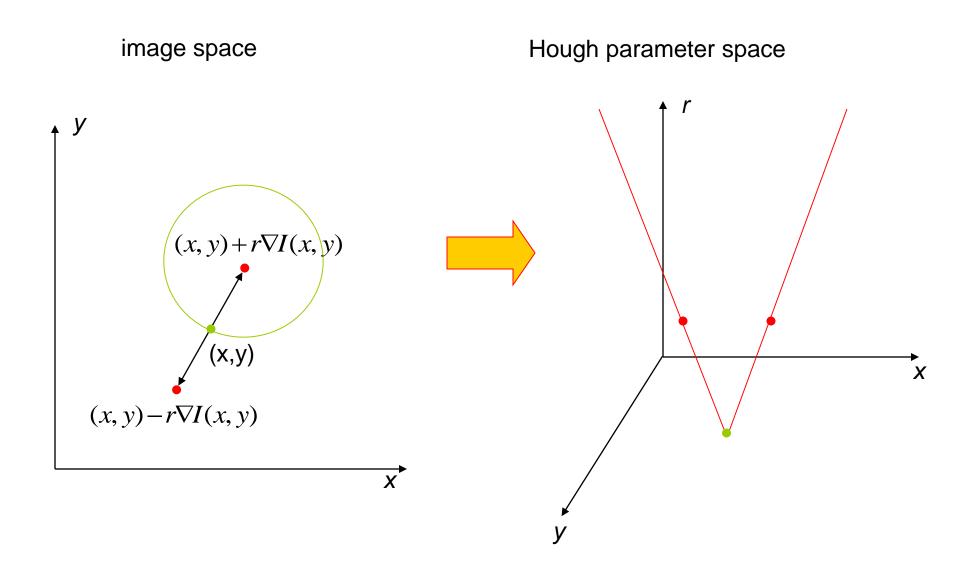
 Grid search equivalent procedure: for each (x,y,r), draw the corresponding circle in the image and compute its "support"



Hough Transform

- How would we find circles?
 - Of fixed radius
 - Of unknown radius
 - Of unknown radius but with known edge orientation

Hough transform for circles



Hough transform conclusions

Good

- Robust to outliers: each point votes separately
- Fairly efficient (often faster than trying all sets of parameters)
- Provides multiple good fits

Bad

- Some sensitivity to noise
- Bin size trades off between noise tolerance, precision, and speed/memory
 - Can be hard to find sweet spot
- Not suitable for more than a few parameters
 - grid size grows exponentially

Common applications

- Line fitting (also circles, ellipses, etc.)
- Object instance recognition (parameters are affine transform)
- Object category recognition (parameters are position/scale)