

# Multivariate Visual Representations 1



CS 7450 - Information Visualization  
Sep. 14, 2016  
John Stasko

## Learning Objectives



- For the following visualization techniques/systems, be able to describe each and its visual encoding, know what type of data it's best for, know its strengths and limitations, and understand how to apply it
  - Iconic representations (Chernoff faces), Table Lens, InfoZoom, Mosaic plot, Attribute Explorer, Parallel Sets, Star plots, Star coordinates
- Explain the visual encoding and design issues of Parallel Coordinates, as well as their utility and limitations
- Understand how the different types of variables in a multivariate data set influence the visualization technique that should be chosen to represent the data
- Be able to apply any of these techniques to a data set that is an appropriate match for them

# How Many Variables?



- Data sets of dimensions 1, 2, 3 are common
- Number of variables per class
  - 1 - Univariate data
  - 2 - Bivariate data
  - 3 - Trivariate data
  - >3 – Hyper/Multivariate data **Focus Today**

## Earlier



- We examined a number of tried-and-true techniques/visualizations for presenting multivariate (typically  $\leq 3$ ) data sets
  - Bar graph, line graph, pie chart, scatterplot, box plot, trellis display, crosstab, radar graph, heatmap
- Hinted at how to go above 3 dimensions

# Hypervariate Data



- How about 4 to 20 or so variables (for instance)?
  - Lower-dimensional hypervariate data
  - Many data sets fall into this category

# Design Challenge



- Data set of 500 cases
- Attributes
  - 5 quantitative
  - 4 nominal
  - 2 ordinal
- Design a visualization

# More Dimensions



- Fundamentally, we have 2 geometric (position) display dimensions
- For data sets with  $>2$  variables, we must project data down to 2D
- Come up with visual mapping that locates each dimension into 2D plane
  
- Computer graphics: 3D- $\rightarrow$ 2D projections

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# Wait a Second



- A spreadsheet already does that
  - Each variable is positioned into a column
  - Data cases in rows
  - This is a projection (mapping)
  
- What about some other techniques?
  - Already seen a couple

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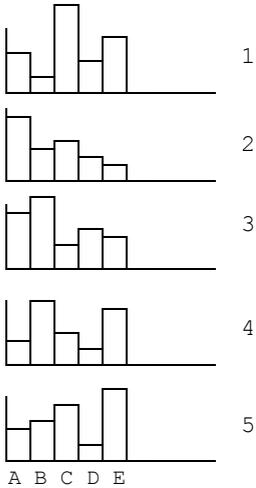
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# Multiple Views



Give each variable its own display

	A	B	C	D	E
1	4	1	8	3	5
2	6	3	4	2	1
3	5	7	2	4	3
4	2	6	3	1	5
5	3	4	5	1	7

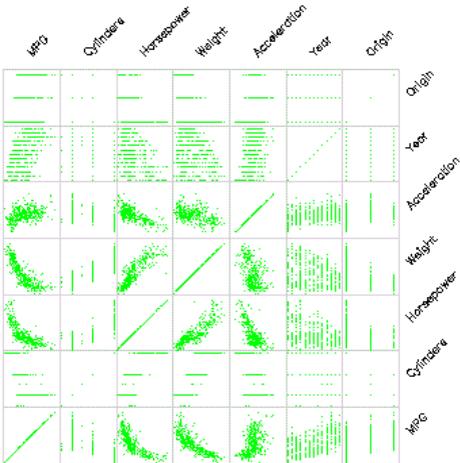


# Scatterplot Matrix



Represent each possible pair of variables in their own 2-D scatterplot

If pairwise correlation is key



## Key Principle (today)



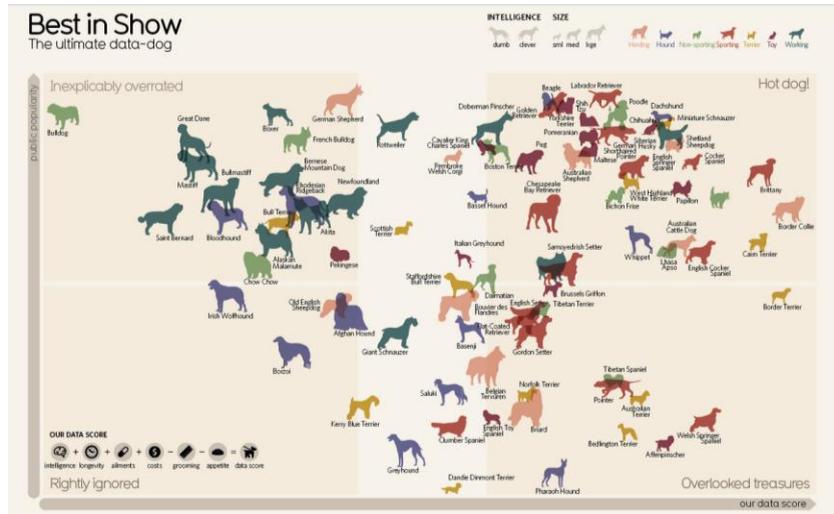
- Handle all data sets generically
  - Examine techniques not specific to some data or domain
  - Technique can generally handle all data sets

## Iconic Representations



- Glyph (graphical object) represents a data case
- Visual properties of glyph represent different variables

# Remember?



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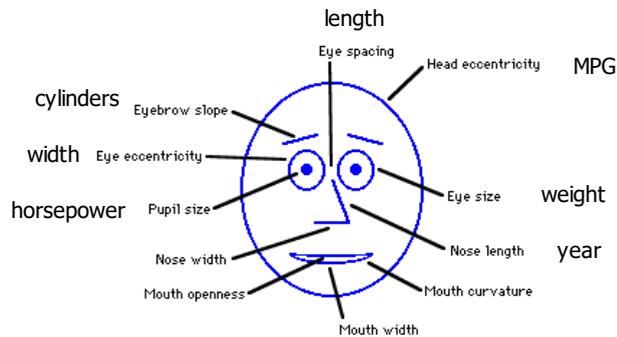
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# Chernoff Faces



Encode different variables' values in characteristics of human face

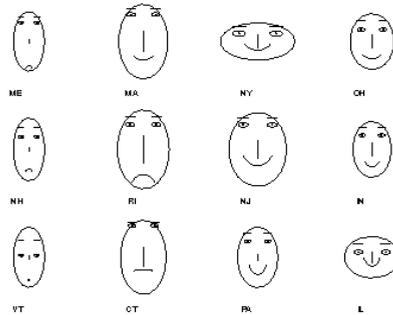


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# Examples



Cute applet: <http://www.cs.uchicago.edu/~wiseman/chernoff/>

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# Table Lens



- Spreadsheet is certainly one hypervariate data presentation
- Idea: Make the text more visual and symbolic
- Just leverage basic bar chart idea

Rao & Card  
CHI '94

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# Visual Mapping



	A	B	C	D	E	F
1	Sales rep	Quota	Variance to quota	% of quota	Forecast	Actual bookings
2	Albright, Gary	200,000	-16,062	92	205,000	183,938
3	Brown, Sheryl	150,000	84,983	157	260,000	234,983
4	Cartwright, Bonnie	100,000	-56,125	44	50,000	43,875
5	Caruthers, Michael	300,000	-25,125	92	324,000	274,875
6	Garibaldi, John	250,000	143,774	158	410,000	393,774
7	Giard, Jean	75,000	-48,117	36	50,000	26,883
8	Jones, Suzanne	140,000	-5,204	96	149,000	134,796
9	Larson, Terri	350,000	238,388	168	600,000	588,388
10	LeShan, George	200,000	-75,126	62	132,000	124,874
11	Levenson, Bernard	175,000	-9,267	95	193,000	165,733
12	Mulligan, Robert	225,000	34,383	115	275,000	259,383
13	Tetracelli, Sheila	50,000	-1,263	97	50,000	48,737
14	Wotisek, Gillian	190,000	-3,648	98	210,000	186,252
15						

Change quantitative values to bars



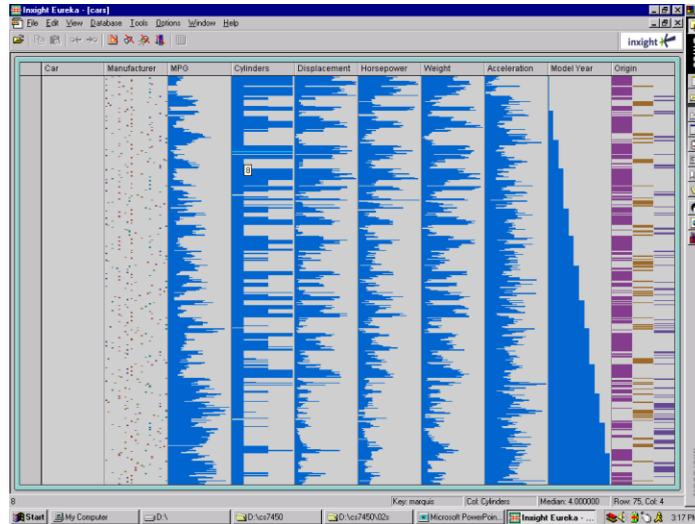
# Tricky Part



	A	B	C	D	E	F	G	H	I
1	Cereal	Manufacture	Type	Calories	Protein	Fat	Sodium	Fiber	Carbol
2	Frosted Mini-Wheats	K	C	100	3	0	0	3	
3	Raisin Squares	K	C	90	2	0	0	2	
4	Shredded Wheat	N	C	80	2	0	0	3	
5	Shredded Wheat n'Bran	N	C	90	3	0	0	4	
6	Shredded Wheat spoon s	N	C	90	3	0	0	3	
7	Puffed Rice	Q	C	50	1	0	0	0	
8	Puffed Wheat	Q	C	50	2	0	0	1	
9	Maypo	A	H	100	4	1	0	0	
10	Quaker Oatmeal	Q	H	100	5	2	0	2.7	
11	Strawberry Fruit Wheats	N	C	90	2	0	15	3	
12	100% Natural Bran	Q	C	120	3	5	15	2	
13	Golden Crisp	P	C	100	2	0	45	0	
14	Smacks	K	C	110	2	1	70	1	
15	Great Grains Pecan	P	C	120	3	3	75	3	
16	Cream of Wheat (Quick)	N	H	100	3	0	80	1	
17	Corn Pops	K	C	110	1	0	90	1	
18	Muesli Raisins, Dates, & R	C	C	150	4	3	95	3	
19	Anna Marie	K	C	110	2	0	125	1	

What do you do for nominal data?

# Instantiation



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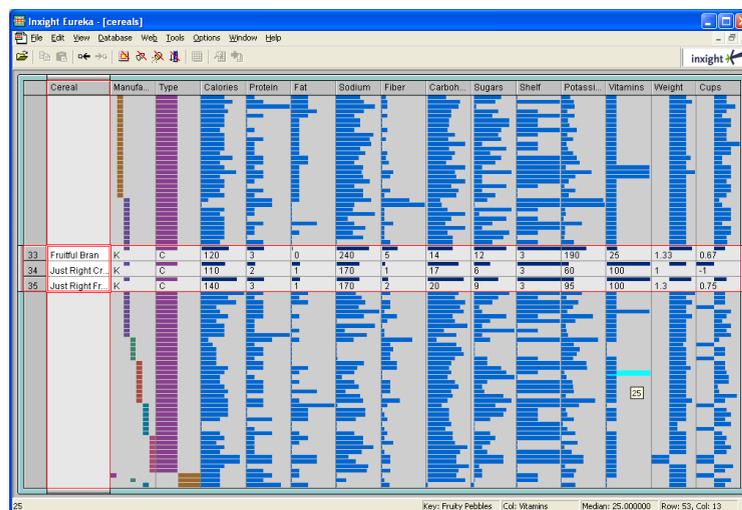
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# Details



Focus on item(s) while showing the context

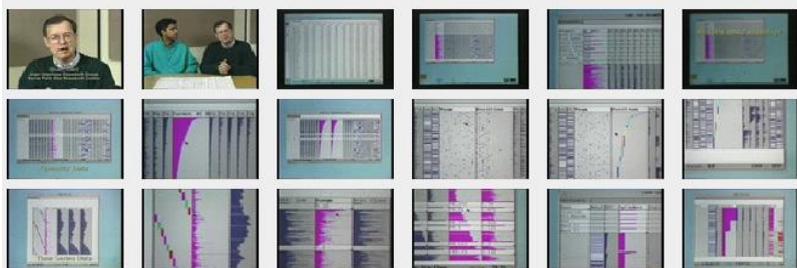


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# See It



<http://www.open-video.org/details.php?videoid=8304>

Video

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# FOCUS



- Feature-Oriented Catalog User Interface
- Leverages spreadsheet metaphor again
- Items in columns, attributes in rows
- Uses bars and other representations for attribute values

Spenke, Beilken, & Berlage  
UIST '96

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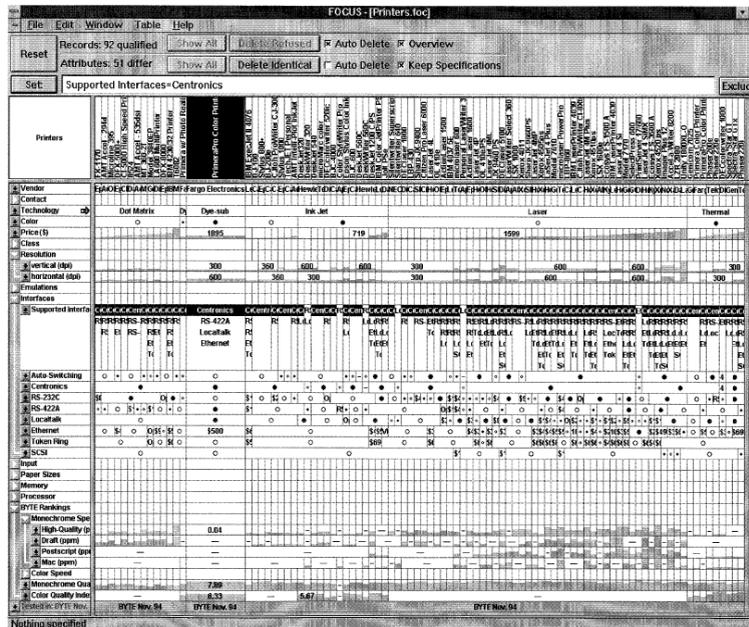


Figure 1: An overview of the printer table.

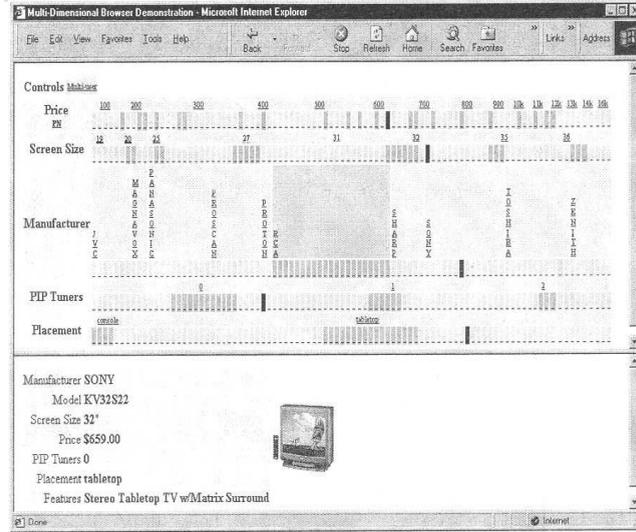
## Characteristics



- Can sort on any attribute (row)
- Focus on an attribute value (show only cases having that value) by double-clicking on it
- Can type in queries on different attributes to limit what is presented too



# Interface

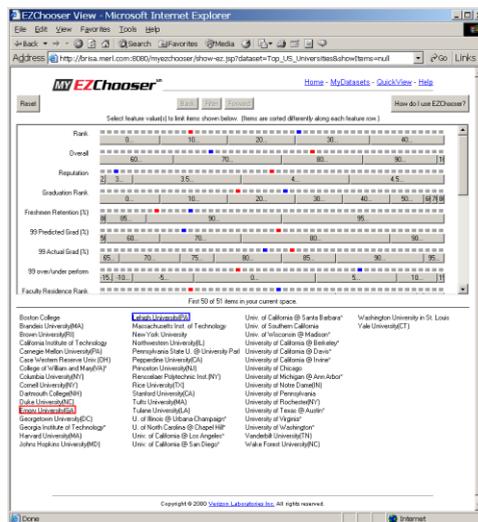


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# Instantiation



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# Alternate UI



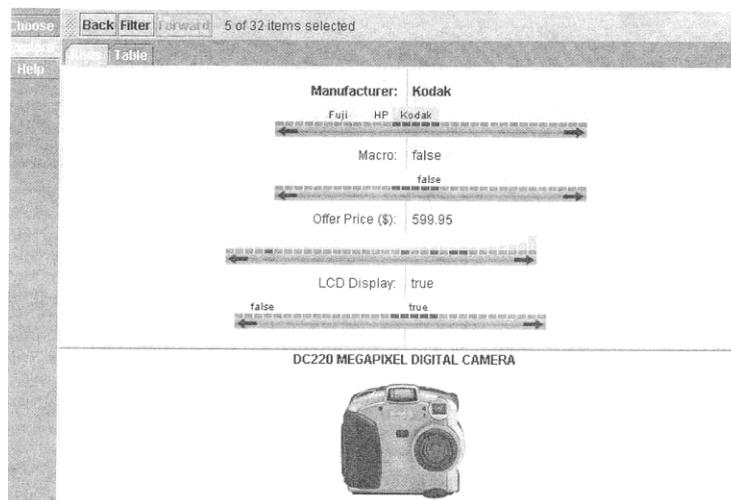
- Can slide the values in a row horizontally
- A particular data case then can be lined up in one column, but the rows are pushed unequally left and right

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# Attributes as Sliding Rods



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# Limitations



- Number of cases (horizontal space)
- Nominal & textual attributes don't work quite as well

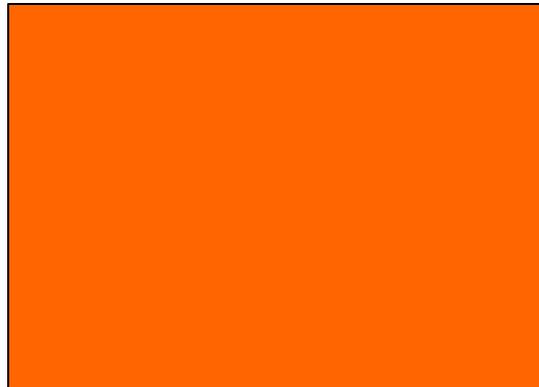
# An Application



- What if you cared about ranking items?
  - Think of the attributes per item as contributing to some score or value for it
- Apply the representations we've seen earlier



# Mosaic Plot

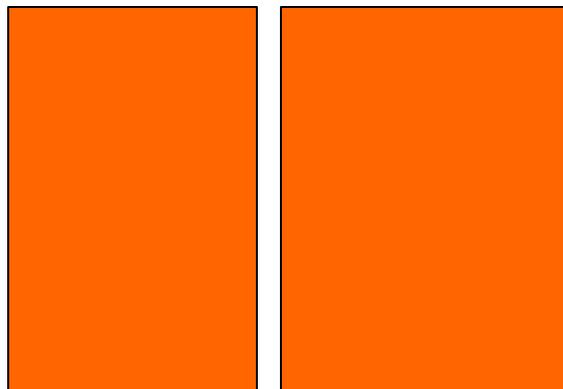


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# Mosaic Plot



Women

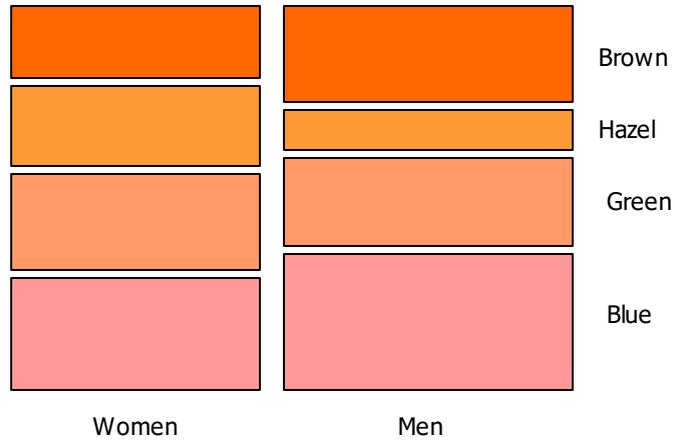
Men

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# Mosaic Plot

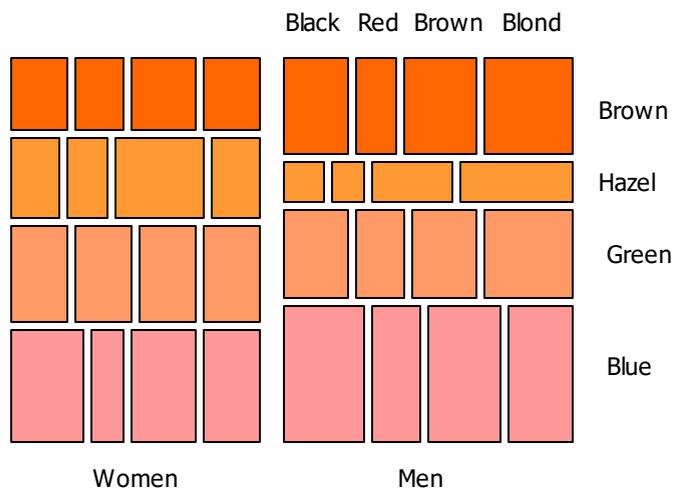


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# Mosaic Plot



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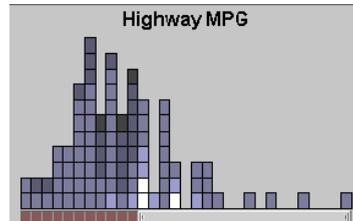
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# Attribute Explorer



- General hypervariate data representation combined with flexible interaction



Spence & Tweedie  
*Inter w Computers '98*

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# Characteristics



- Multiple histogram views, one per attribute (like trellis)
- Each data case represented by a square
- Square is positioned relative to that case's value on that attribute
- Selecting case in one view lights it up in others
- Query sliders for narrowing
- Use shading to indicate level of query match (darkest for full match)

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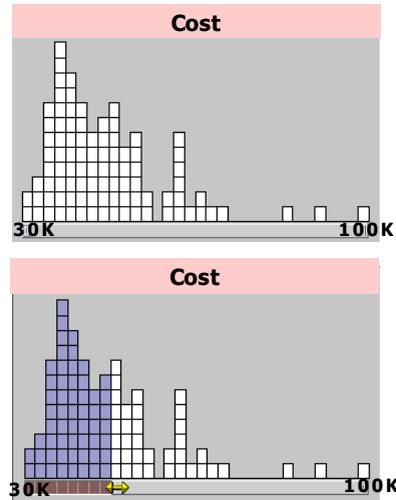
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# Features



- Attribute histogram
- All objects on all attribute scales
- Interaction with attributes limits



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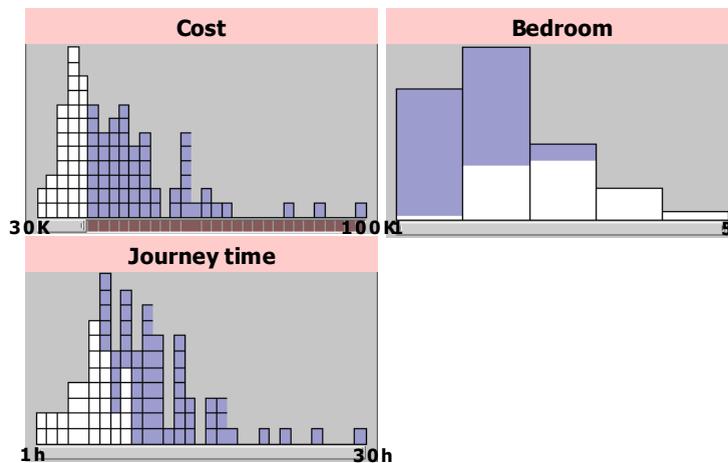
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# Features



- Inter-relations between attributes – brushing



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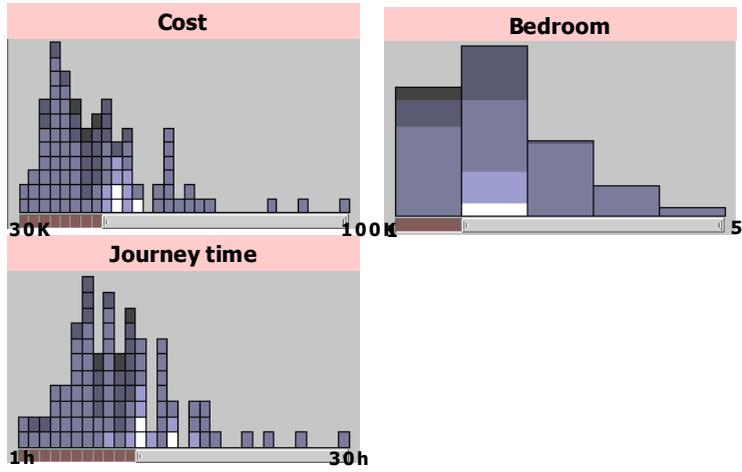
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# Features



- Color-encoded sensitivity



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# Attribute Explorer



Video

<http://www.open-video.org/details.php?videoid=8162>

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# Parallel Coordinates



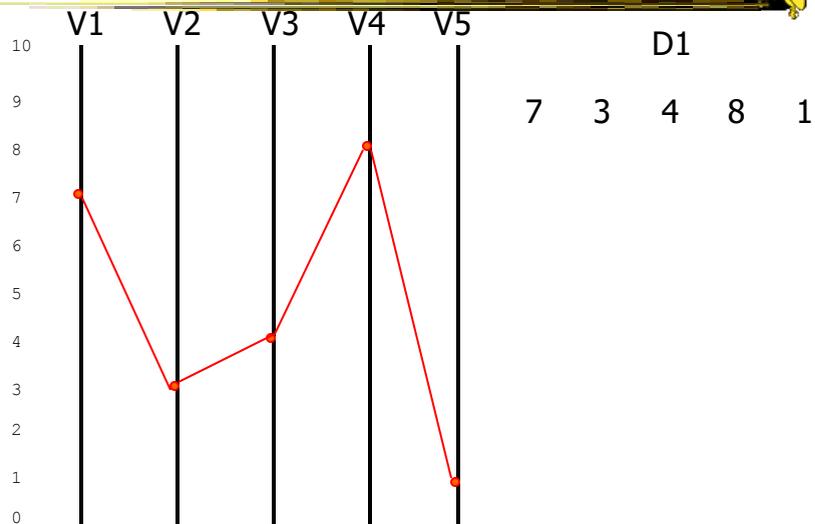
	V1	V2	V3	V4	V5
D1	7	3	4	8	1
D2	2	7	6	3	4
D3	9	8	1	4	2

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# Parallel Coordinates

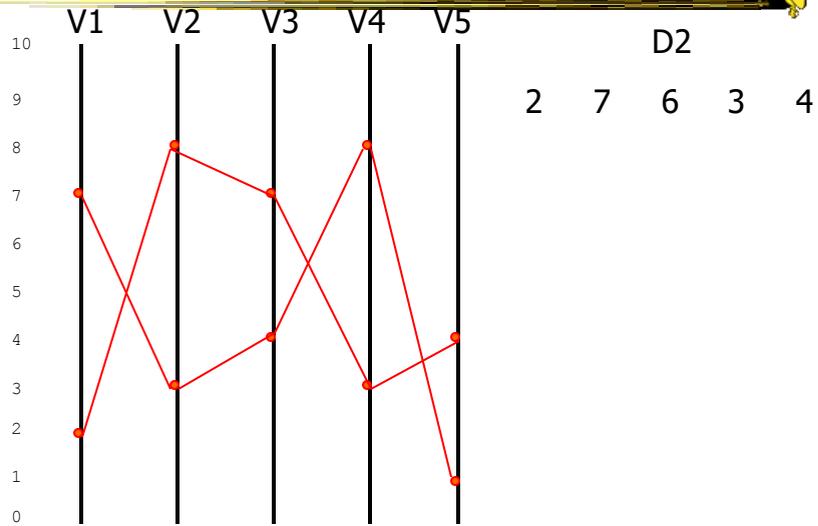


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# Parallel Coordinates

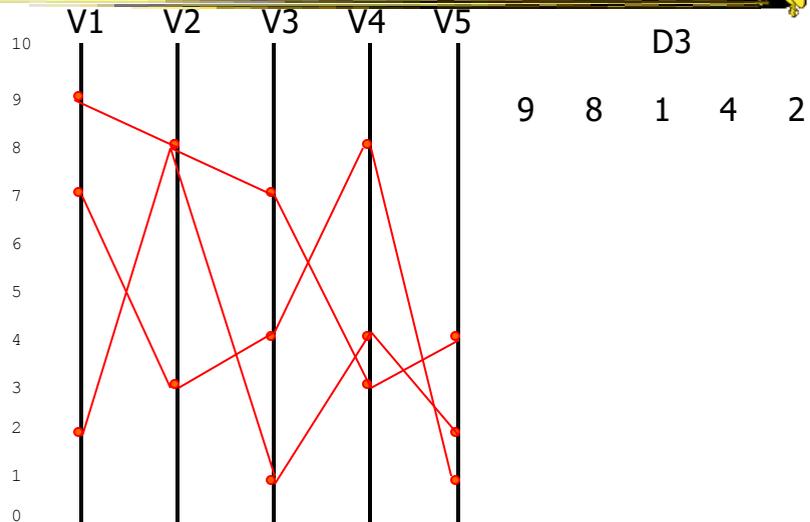


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# Parallel Coordinates

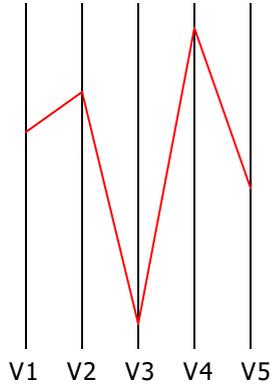


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# Parallel Coordinates



Encode variables along a horizontal row

Vertical line specifies different values that variable can take

Data point represented as a polyline

## Issue

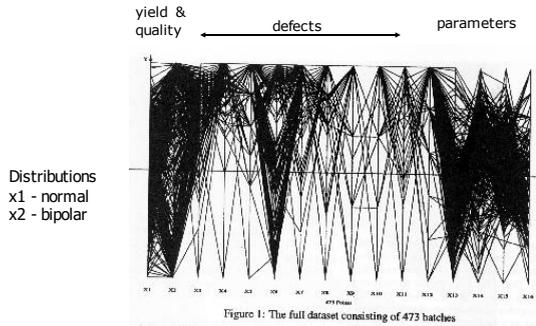


- Different variables can have values taking on quite different ranges
- Must normalize all down (e.g., 0->1)

# Application



- VLSI chip manufacture
- Want high quality chips (high speed) and a high yield batch (% of useful chips)
- Able to track defects
- Hypothesis: No defects gives desired chip types
- 473 batches of data



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# To Learn More

Great site  
that's all about  
parallel coords



Welcome to parallelcoordinates.de  
This website is dedicated to parallel coordinates, a visualization technique for multidimensional geometry. Learn about the theory and applications of parallel coordinates, or interactively explore parallel coordinates with your own data.

Blog  
The blog features various topics around aspects of parallel coordinates and multidimensional data visualization. Learn everything to prevent all kinds of problems that will be useful for teaching and to make more clear examples and pointers to the literature where applicable.

PACO  
PACO is an interactive, web-based application that allows you to not only view the concepts covered in the blog and to use parallel coordinates with your own data. Be warned that this is work in progress, so it is prepared for bugs and track back frequently for improved versions.

parallelcoordinates.de

http://www.parallelcoordinates.de

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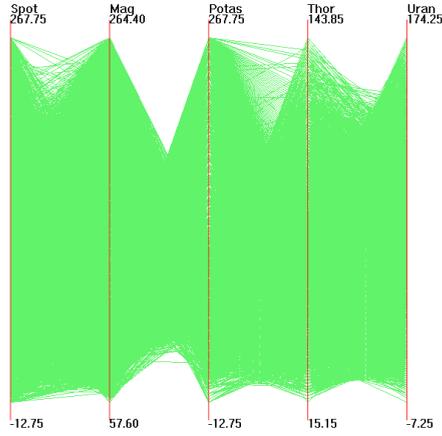
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# Challenges



Too much data



Out5d dataset (5 dimensions, 16384 data items)

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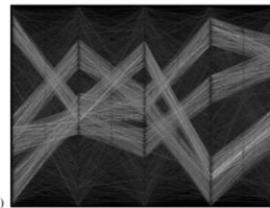
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(courtesy of J. Yang)

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# Reducing Density

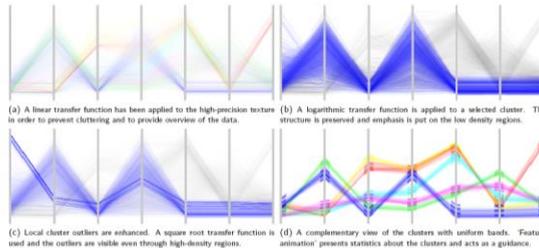
Jerding and Stasko, '95, '98  
Wegman & Luo, '96



Artero et al, '04

Figure 1 – Parallel Coordinates visualization of the *Sirt1* data set (7,500 five-attribute records).

(a)



Johansson et al, '05

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# Dimensional Reordering



Can you reduce clutter and highlight other interesting features in data by changing order of dimensions?

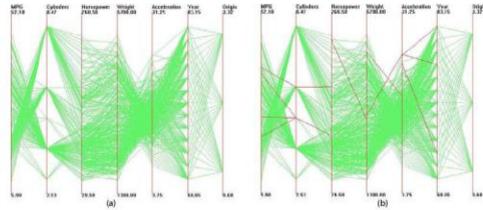


Figure 1: Parallel coordinates visualization of Cars dataset. Outliers are highlighted with red in (b).

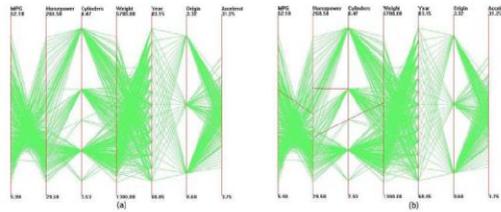


Figure 2: Parallel coordinates visualization of Cars dataset after clutter-based dimension reordering. Outliers are highlighted with red in (b).

Peng et al  
InfoVis '04

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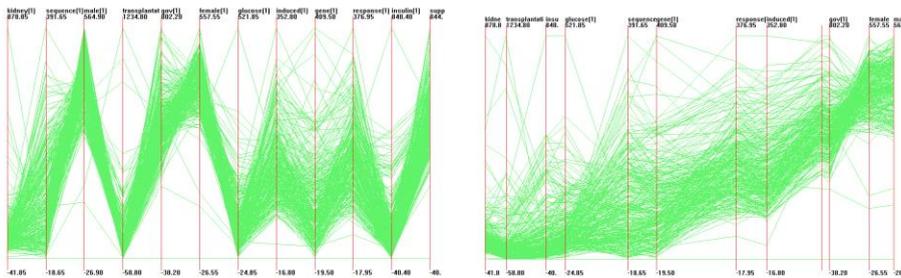
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# Dimensional Reordering



Which dimensions are most like each other?



Same dimensions ordered according to similarity

Yang et al  
InfoVis '03

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# Different Kinds of Data



- How about categorical data?
  - Can parallel coordinates handle that well?

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# Parallel Sets



- Visualization method adopting parallel coordinates layout but uses frequency-based representation
- Visual metaphor
  - Layout similar to parallel coordinates
  - Continuous axes replaced with boxes
- Interaction
  - User-driven: User can create new classifications

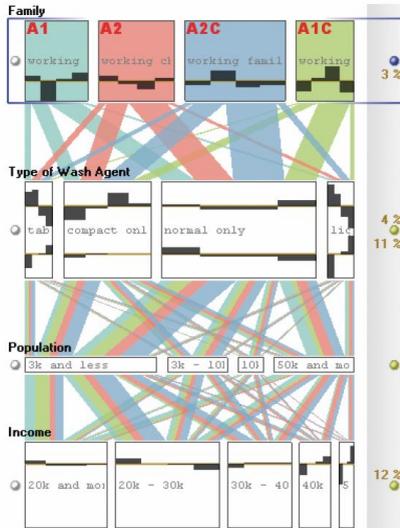
Kosara, Bendix, & Hauser  
*TVCG'05*

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# Representation



Color used for different categories

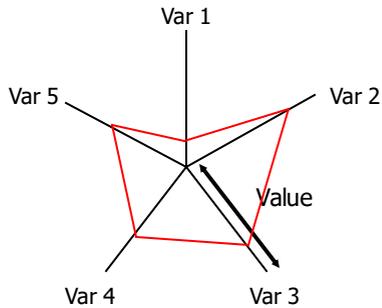
Those values flow into the other variables

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# Star Plots (Radar Chart)



Space out the n variables at equal angles around a circle

Each "spoke" encodes a variable's value

Alternative Rep.

Data point is now a "shape"

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# Example

Time  
April 16, 2012

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# Star Coordinates



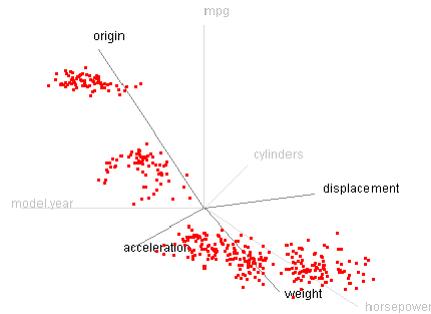
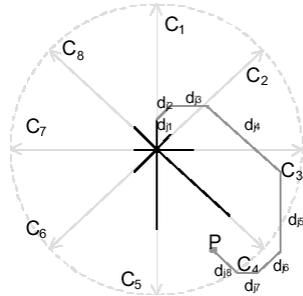
- Same ideas as star plot
- Rather than represent point as polyline, just accumulate values along a vector parallel to particular axis
- Data case then becomes a point

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# Star Coordinates



E. Kandogan  
Late-Breaking Hot Topics, InfoVis '00

Demo

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# Star Coordinates



- Data cases with similar values will lead to clusters of points
- (What's the problem though?)
- Multi-dimensional scaling or projection down to 2D

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# Generalizing the Principles



- General & flexible framework for axis-based visualizations
  - Scatterplots, par coords, etc.
- User can position, orient, and stretch axes
- Axes can be linked

Claessen & van Wijk  
*TVCG*(InfoVis) '11

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## FLINA View

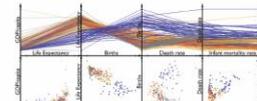
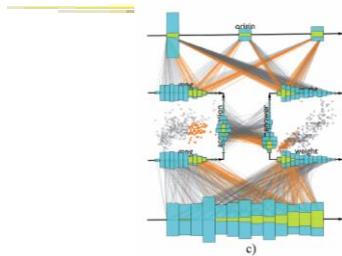


Fig. 6. Demographic data for different countries. Asia: brown; Africa: blue; North America: red; South America: green; Oceania: orange; Europe: gray.

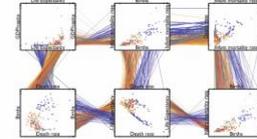
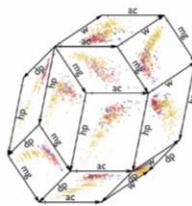
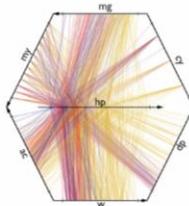


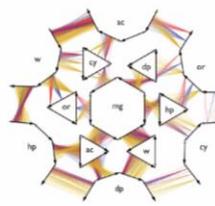
Fig. 7. Alternative lay-out for demographic data



(d) Hyperbox



(e) Time Wheel



(f) Many-to-many PCP

Video

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# Learning Objectives



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  - Iconic representations (Chernoff faces), Table Lens, InfoZoom, Mosaic plot, Attribute Explorer, Parallel Sets, Star plots, Star coordinates
- Explain the visual encoding and design issues of Parallel Coordinates, as well as their utility and limitations
- Understand how the different types of variables in a multivariate data set influence the visualization technique that should be chosen to represent the data
- Be able to apply any of these techniques to a data set that is an appropriate match for them

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# Readings



- Inselberg, InfoVis '97 paper
- Browse Heinrich  
<http://www.parallelcoordinates.de>  
website (try out demo)

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## Reminder



- Processing tutorial session
  - Thursday 11-12 in GVU Café
- HW 3 due a week from today

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## Upcoming



- Multivariate Visual Representations 2
- InfoVis Systems & Toolkits

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