Topics:

- Machine learning intro, applications (CV, NLP, etc.)
- Parametric models and their components

CS 4644 / 7643-A

ZSOLT KIRA

- **PS0 due 14th Sunday night, but do it TODAY!**
  - Please do it, and give others a chance at waitlist if your background is not sufficient (beef it up and take it next time)
  - Do it even if you're on the waitlist!

- **Piazza**:
  - Enroll now! https://piazza.com/gatech/spring2023/cs46447643/home (Code: DLSPR23 or through canvas)
  - Search for teammates: **@5** (https://piazza.com/class/lr1kcuwnhwo743/post/5)
  - Note: Do NOT post anything containing solutions publicly!
  - Make it active!

- **Office hours** start next week

Administrivia

Georgia Tech

- **Collaboration**
  - Only on HWs and project (not allowed in HW0/PS0).
  - You may discuss the questions
  - Each student writes their own answers
  - Write on your homework anyone with whom you collaborate
  - Each student must write their own code for the programming part
  - Do NOT search for code implementing what we ask; search for concepts

- **Zero tolerance on plagiarism**
  - Neither ethical nor in your best interest
  - Always credit your sources
  - Don’t cheat. We will find out.

Collaboration Policy

- **Grace period**
  - 2 days grace period for each assignment (**EXCEPT PS0**)
    - Intended for checking submission NOT to replace due date
    - No need to ask for grace, no penalty for turning it in within grace period
    - Can NOT use for PS0

- **After grace period, you get a 0 (no excuses except medical)**
  - Send all medical requests to dean of students (https://studentlife.gatech.edu/)
  - Form: https://gatech-advocate.symplicity.com/care_report/index.php/pid224342

- **DO NOT SEND US ANY MEDICAL INFORMATION!** We do not need any details, just a confirmation from dean of students

Grace Period

Georgia Tech

CS231n Convolutional Neural Networks for Visual Recognition

Python Numpy Tutorial

This tutorial was contributed by Justin Johnson.

We will use the Python programming language for all assignments in this course. Python is a great general-purpose programming language on its own, but with the help of a few popular libraries (numpy, scipy, matplotlib) it becomes a powerful environment for scientific computing.

We expect that many of you will have some experience with Python and numpy; for the rest of you, this section will serve as a quick crash course both on the Python programming language and on the use of Python for scientific computing.

http://cs231n.github.io/python-numpy-tutorial/

Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Machine Learning Overview

Georgia Tech

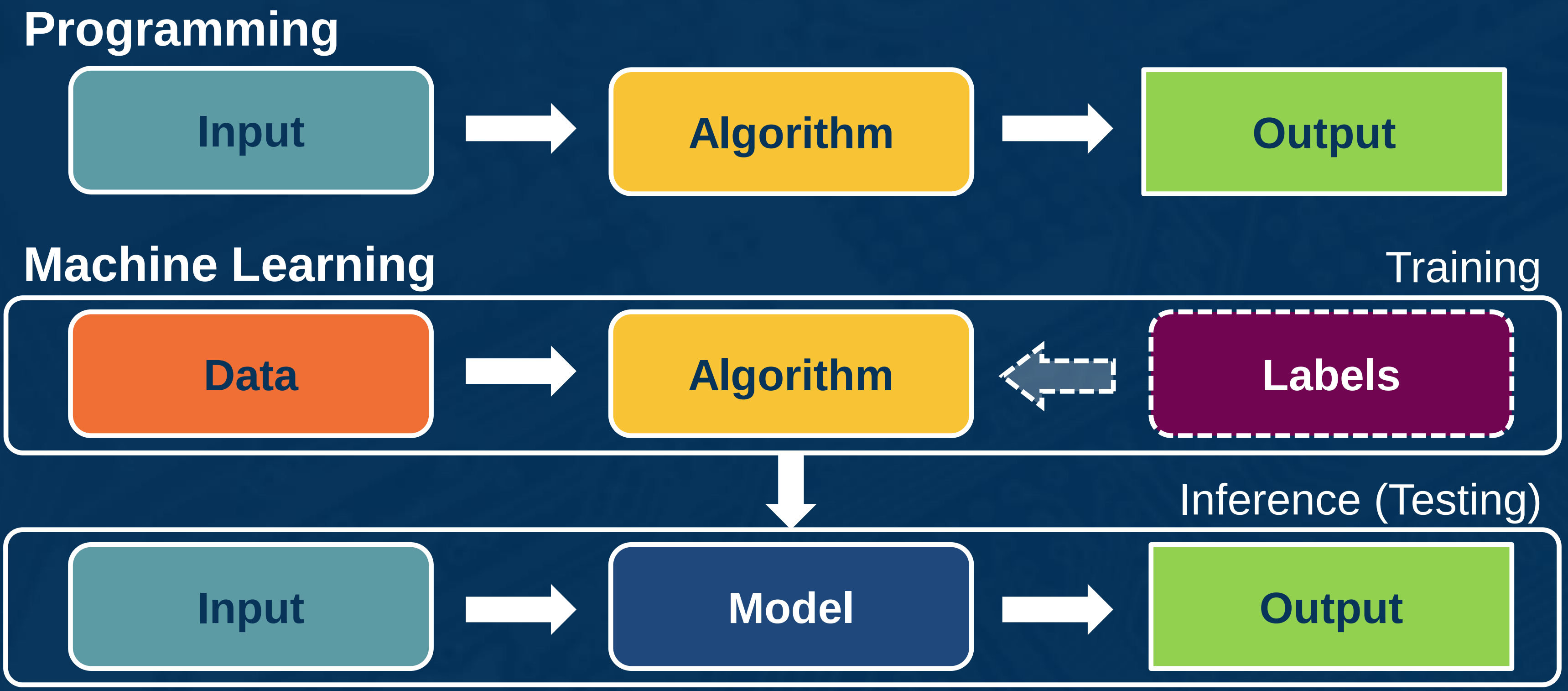
What is Machine Learning (ML)?

"A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E."

Tom Mitchell (Machine Learning, 1997)

Georgia Tech

How is it Different than Programming?

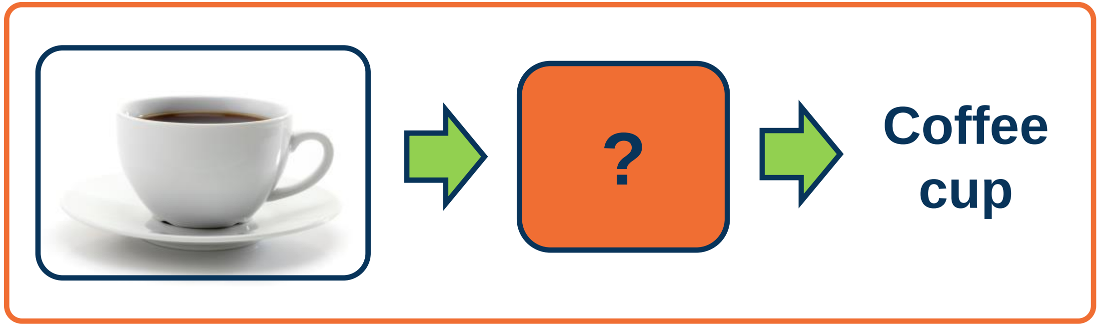


Machine learning thrives when it is **difficult to design an algorithm** to perform the task

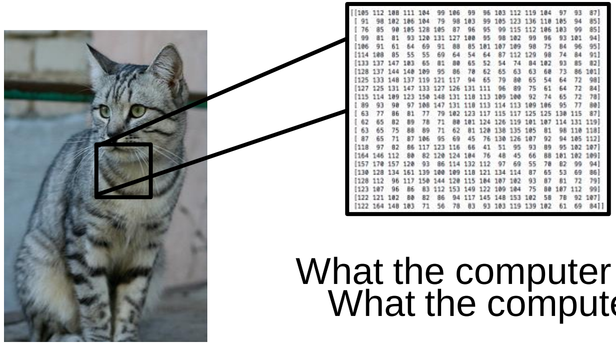
Applications:

```
algorithm quicksort(A, lo, hi) is
    if lo < hi then
        p := partition(A, lo, hi)
        quicksort(A, lo, p - 1)
        quicksort(A, p + 1, hi)

algorithm partition(A, lo, hi) is
    pivot := A[hi]
    i := lo
    for j := lo to hi do
        if A[j] < pivot then
            swap A[i] with A[j]
            i := i + 1
    swap A[i] with A[hi]
    return i
```



Why Image Classification is Hard



This image by Nikita is licensed under CC-BY 2.0

What the computer sees
What the computer sees

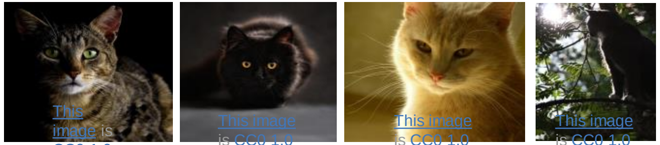
An image is just a big grid of numbers between [0, 255]:

e.g. 800 x 600 x 3
(3 channels RGB)

Viewpoint Changes

All pixels change when the camera moves!

Illumination



This image is CC0 1.0 public domain

This image is CC0 1.0 public domain

This image is CC0 1.0 public domain

This image is CC0 1.0 public domain

Deformation

This image by Umberto Salvagnin is licensed under CC-BY 2.0

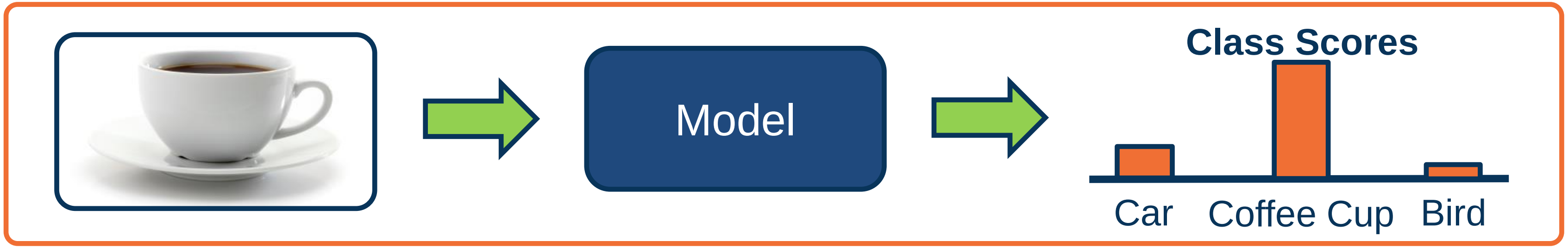
This image by Umberto Salvagnin is licensed under CC-BY 2.0

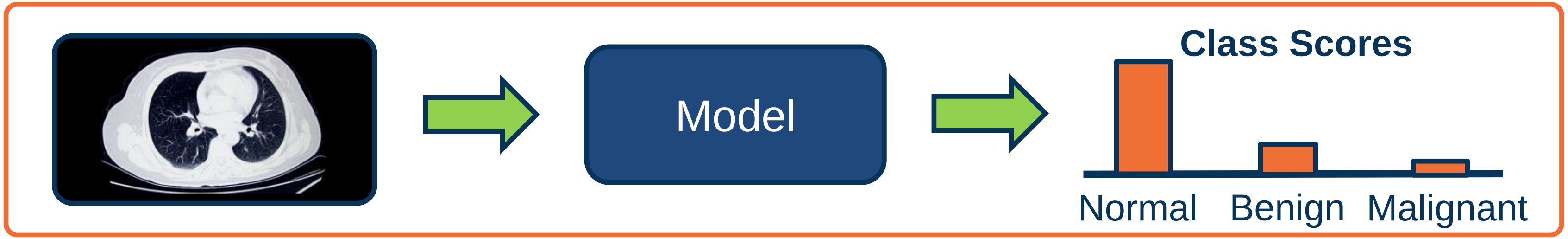
This image by sare bear is licensed under CC-BY 2.0

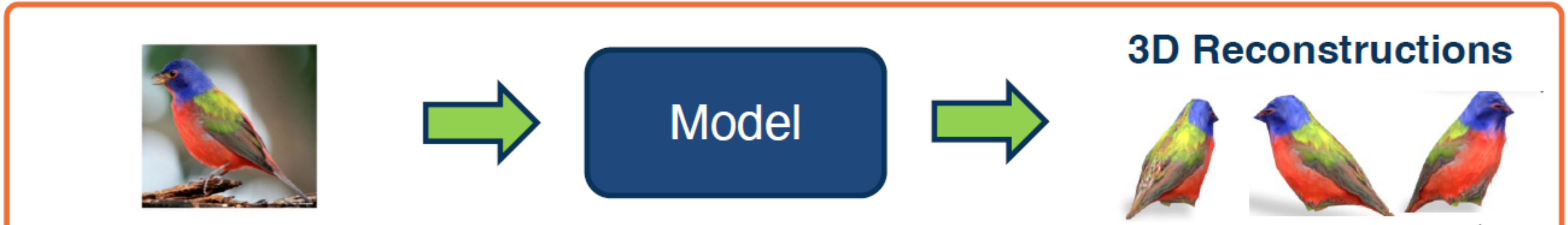
This image by Tom Thai is licensed under CC-BY 2.0

Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Application: Computer Vision





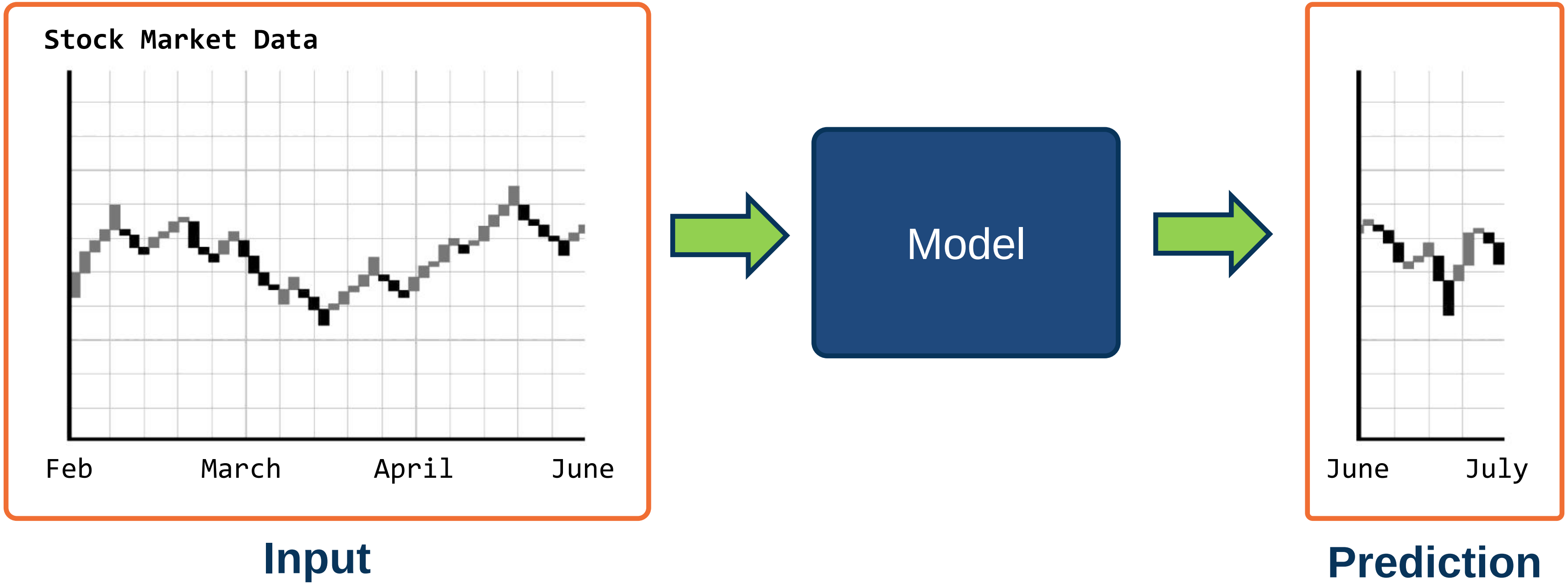


Kanazawa *et al.*, 2018

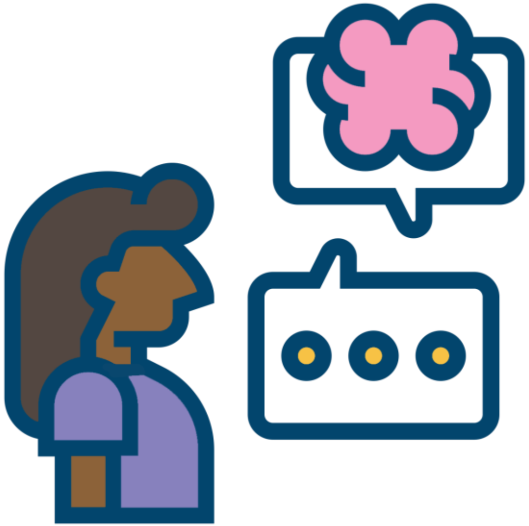
Example: Image Classification

Application: Time-Series Forecasting

Given a series of measurements, **output prediction for next time period**



Application: Natural Language Process (NLP)



Very large number of NLP sub-tasks:

- Syntax Parsing
- Translation
- Named entity recognition
- Summarization

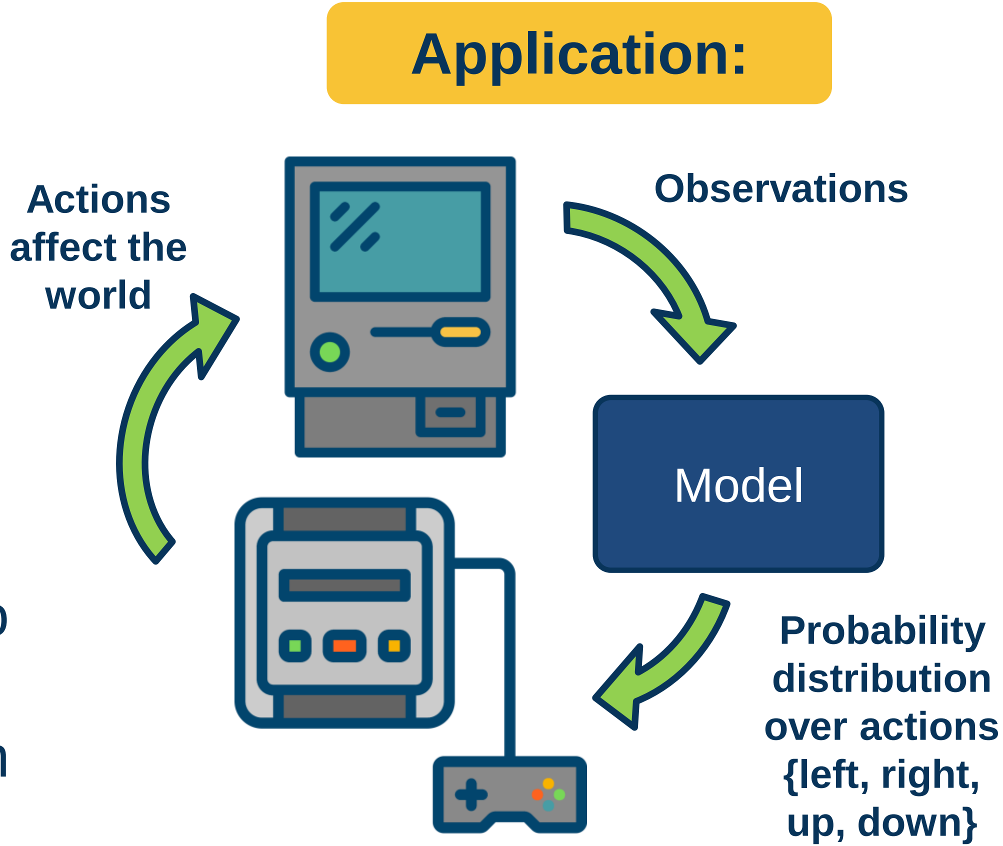
Sequence modeling: Variable length sequential inputs and/or outputs

Recent progress: Large-scale language models

Decision-making tasks

- Sequence of inputs/outputs
- Actions affect the environment

Examples: Chess / Go, Video Games, Recommendation Systems, Network Congestion Control, …



Robotics involves a **combination of AI/ML techniques**:

- **Sense:** Perception
- **Plan:** Planning
- **Act:** Controls/Decision-Making

Some things are **learned (perception)**, while others **programmed**

- Evolving landscape

Application:

Supervised Learning and Parametric Models

Georgia Tech

Supervised Learning

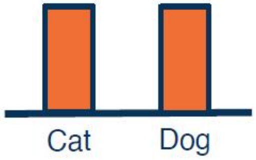
Unsupervised Learning

Reinforcement Learning

Supervised Learning

- Train Input: $\{X, Y\}$
- Learning output: $f : X \rightarrow Y$, e.g. a **distribution** $P(y|x)$

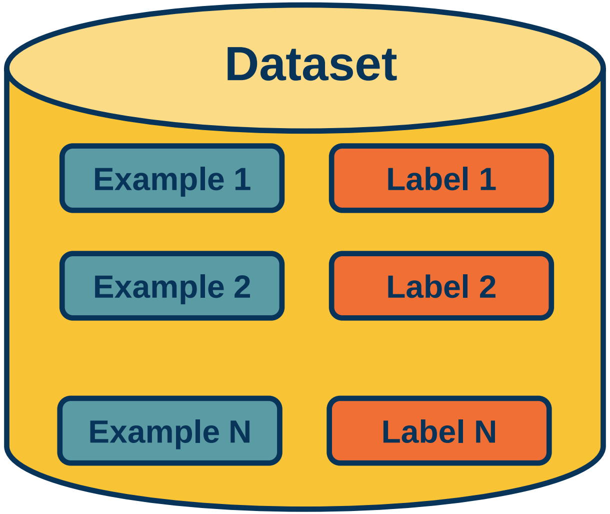
https://en.wikipedia.org/wiki/CatDog



Dataset

$X = \{x_1, x_2, \dots, x_N\}\ where\ x \in \mathbb{R}^d$ **Examples**

$Y = \{y_1, y_2, \dots, y_N\}\ where\ y \in \mathbb{R}^c$ **Labels**



Supervised Learning

- Train Input: $\{X, Y\}$
- Learning output: $f : X \rightarrow Y$, e.g. $P(y|x)$

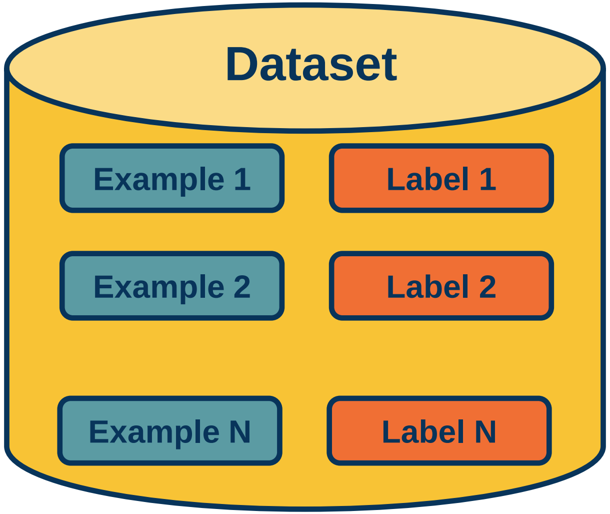
Terminology:

- Model / Hypothesis Class
  - $H: \{h: X \rightarrow Y\}$
  - Learning is search in hypothesis space
- Note **inputs $\boldsymbol{x_i}$ and $\boldsymbol{y_i}$** are each represented as **vectors**

Dataset

$X = \{x_1, x_2, \ldots, x_N\}$ *where* $x \in \mathbb{R}^d$ **Examples**

$Y = \{y_1, y_2, \ldots, y_N\}$ *where* $y \in \mathbb{R}^c$ **Labels**

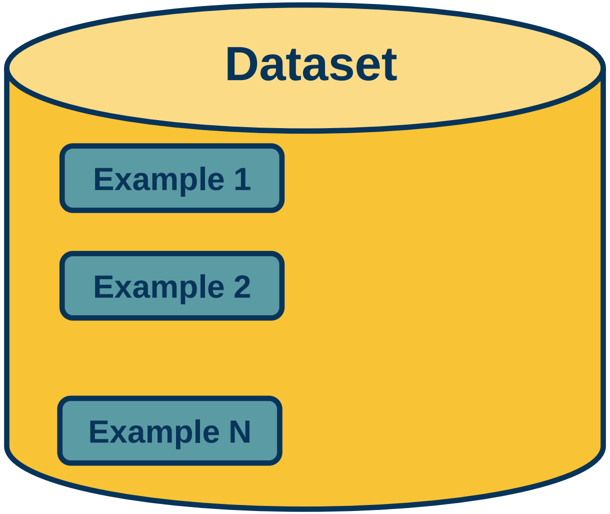


Dataset

$X = \{x_1, x_2, \ldots, x_N\}\ where\ x \in \mathbb{R}^d$ **Examples**

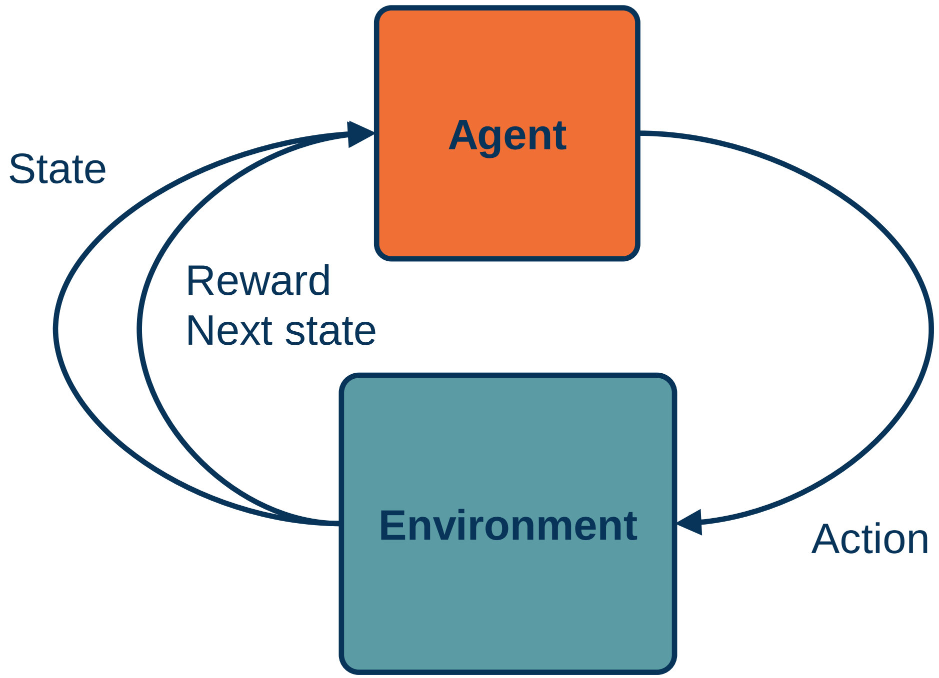
Unsupervised Learning

- Input: $\{X\}$
- Learning output: $P_{data}(x)$
- How likely is x under P_{data}?
- Can we sample from P_{data}?
- Example: Clustering, density estimation, generative modeling, etc.



Reinforcement Learning

- Supervision in form of **reward**
- No supervision on what action to take



Adapted from: http://cs231n.stanford.edu/slides/2020/lecture_17.pdf

Supervised Learning

- Train Input: $\{X, Y\}$
- Learning output: $f : X \rightarrow Y$, e.g. $P(y|x)$

Unsupervised Learning

- Input: $\{X\}$
- Learning output: $P(x)$
- Example: Clustering, density estimation, etc.

Reinforcement Learning

- Supervision in form of **reward**
- No supervision on what action to take

Very often combined, sometimes within the same model!

Parametric Model

Explicitly model the function $f : X \rightarrow Y$ in the form of a parametrized function $f(x, W) = y$, **examples**:

- Logistic regression/classification
- Neural networks

Capacity (size of hypothesis class) **does not** grow with size of training data!

Learning is **search**

Parametric – Linear Classifier

$$f(x, W) = Wx + b$$

Training Stage:

Training Data $\{ (x_i,y_i) \} \rightarrow h$ (Learning)

Testing Stage

Test Data $x \rightarrow h(x)$ (Apply function, Evaluate error)

Procedural View of ML

Georgia Tech

Probabilities to rescue:

X and Y are *random variables*

$D = (x_1,y_1), (x_2,y_2), \ldots, (x_N,y_N) \quad \sim P(X,Y)$

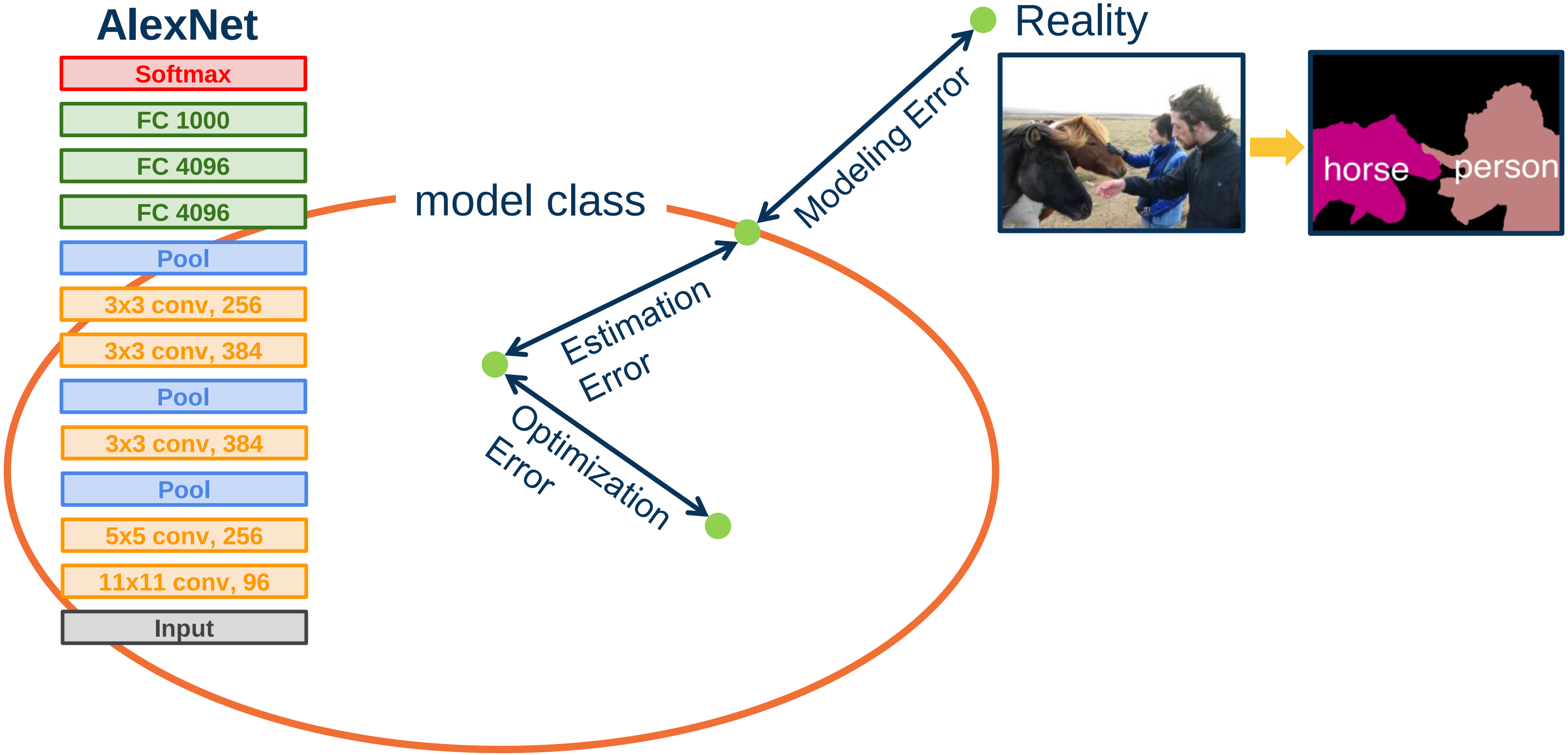
IID: Independent Identically Distributed

Both training & testing data sampled IID from P(X,Y)

Learn on training set

Have some hope of *generalizing* to test set

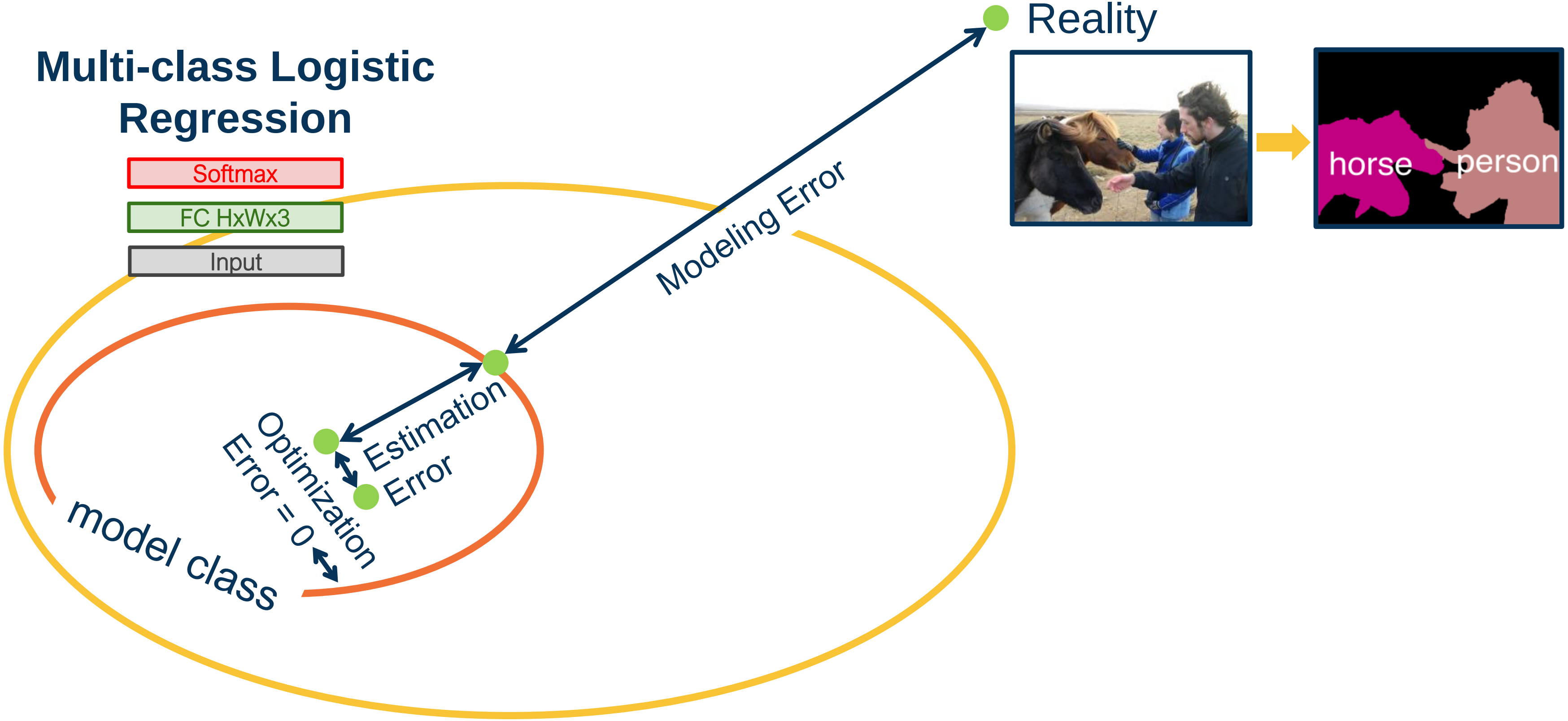
Statistical View of ML



From: slides by Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

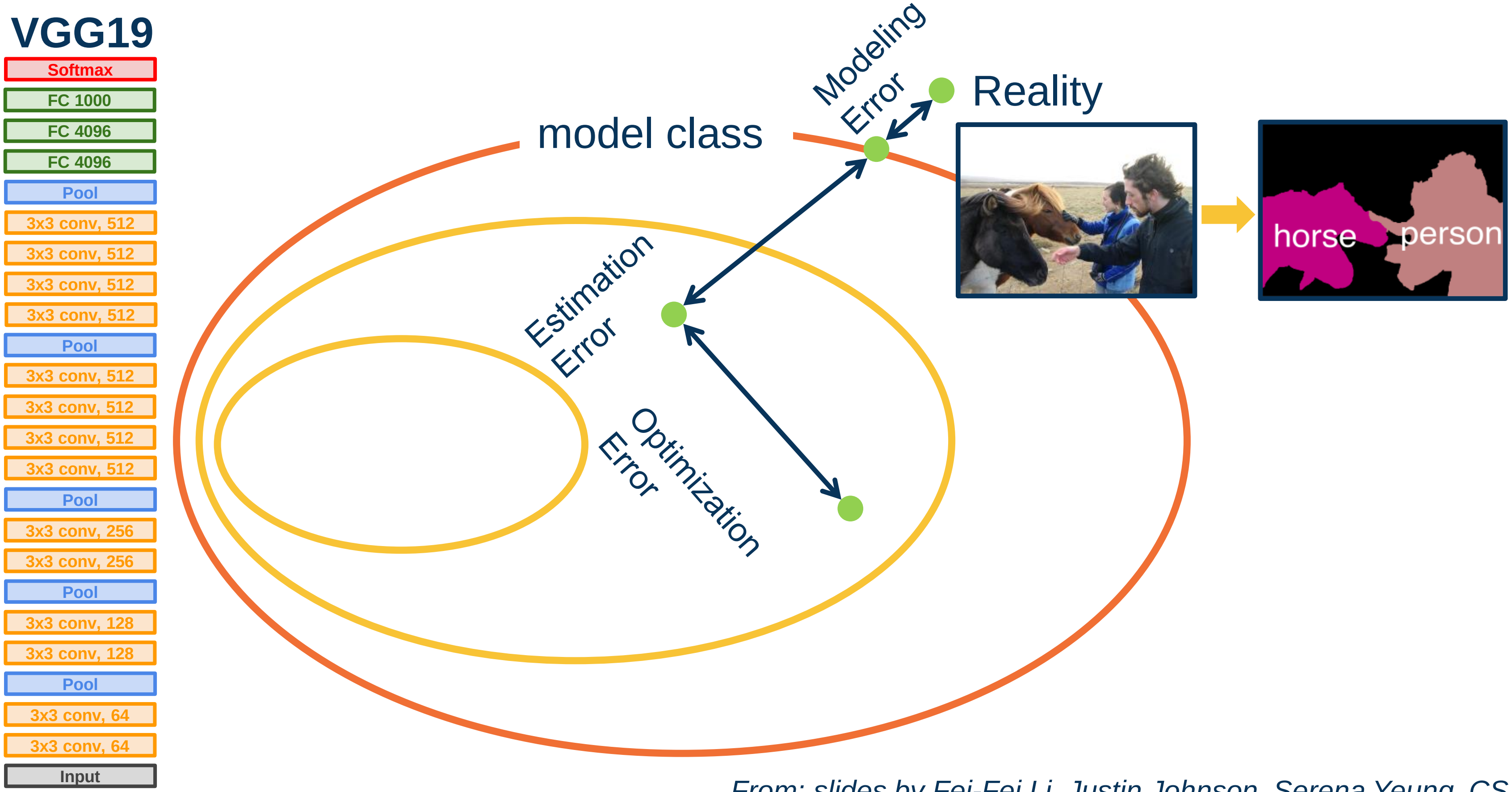
Generalization

Multi-class Logistic Regression



From: slides by Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Generalization



From: slides by Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

20 years of research in Learning Theory oversimplified:

If you have:

Enough training data D

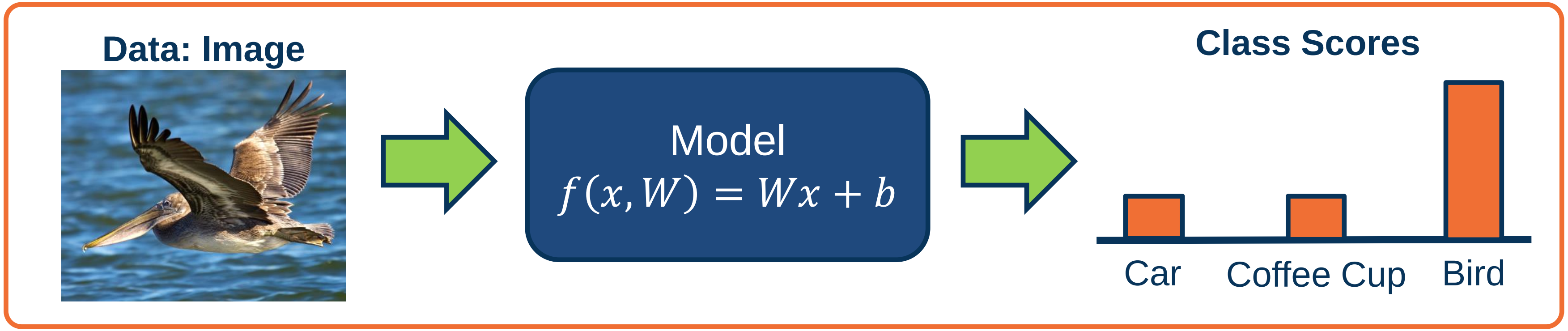
and H is not too complex

then *probably* we can generalize to unseen test data

Caveats: A number of recent empirical results question our intuitions built from this clean separation.

Zhang et al., Understanding deep learning requires rethinking generalization

Guarantees



Input $\{X, Y\}$ where:

- X is an image
- Y is a **ground truth label** annotated by an expert (human)
- $f(x, W) = Wx + b$ is our model, chosen to be a linear function in this case
- W and b are the parameters (**weights**) of our model that must be learned

Example: Image Classification

Input image is **high-dimensional**

- For example n=512 so 512x512 image = **262,144** pixels
- Learning a classifier with high-dimensional inputs is hard

Before deep learning, it was typical to perform **feature engineering**

- Hand-design algorithms for converting raw input into a lower-dimensional set of features

Input Image

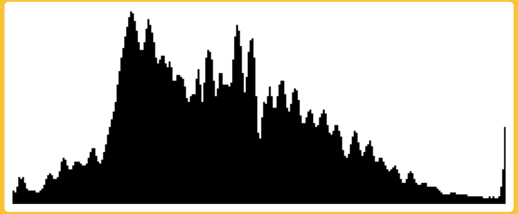
$$x = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1n} \\ x_{21} & x_{22} & \cdots & x_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nn} \end{bmatrix}$$

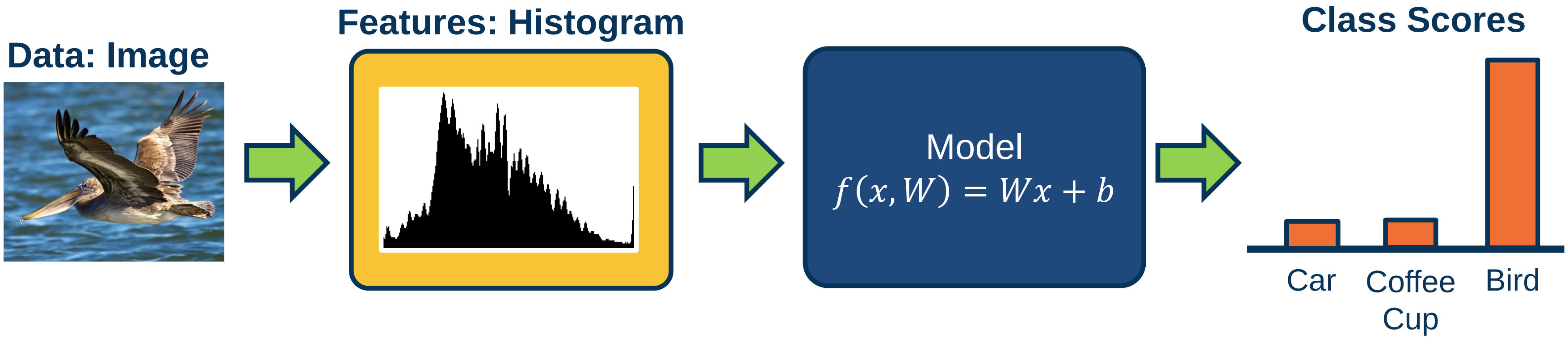
Example: Color histogram

- Vector of numbers representing number of pixels fitting within each bin
- We will later see that learning the feature representation itself is much more effective

Data: Image

Features: Histogram





Input $\{X, Y\}$ where:

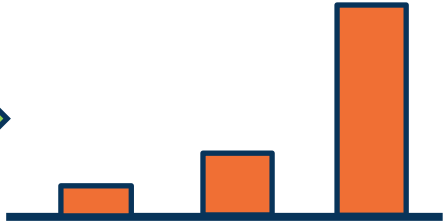
- X is an **image histogram**
- Y is a **ground truth label represented a probability distribution**
- $f(x, W) = Wx + b$ is our model, chosen to be a linear function in this case
- W and b are the **weights** of our model that must be learned

Example: Image Classification

Data: Text

Model
$f(x, W) = W_x + b$

Class Scores



Input $\{X, Y\}$ where:

- X is a sentence
- Y is a **ground truth label** annotated by an expert (human)
- $f(x, W) = Wx + b$ is our model, chosen to be a linear function in this case
- W and b are the **weights** of our model that must be learned

Word Histogram

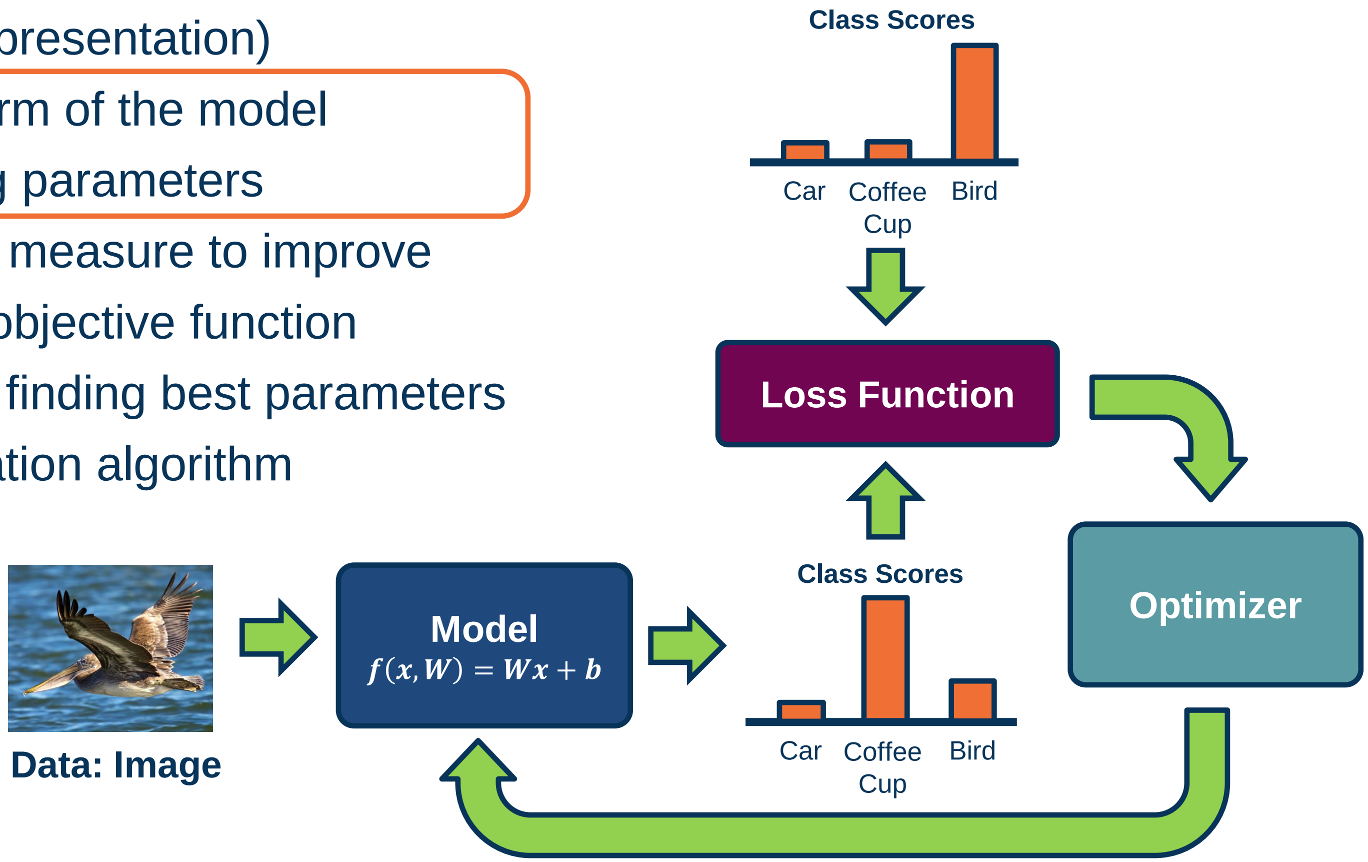
Word	Count
this	1
that	0
is	2
...	
extremely	1
hello	0
onomatopoeia	0
…	

Example: Image Classification

Components of a Parametric Learning Algorithm

Georgia Tech

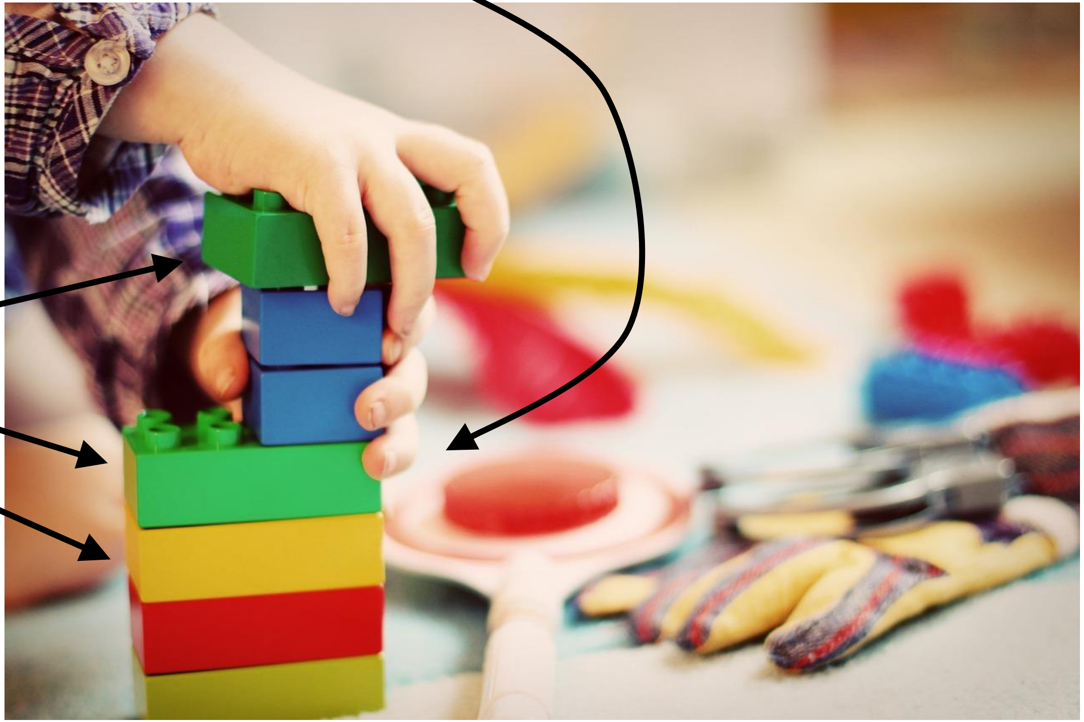
- Input (and representation)
- Functional form of the model
  - Including parameters
- Performance measure to improve
  - Loss or objective function
- Algorithm for finding best parameters
  - Optimization algorithm



Components of a Parametric Model

Neural Network

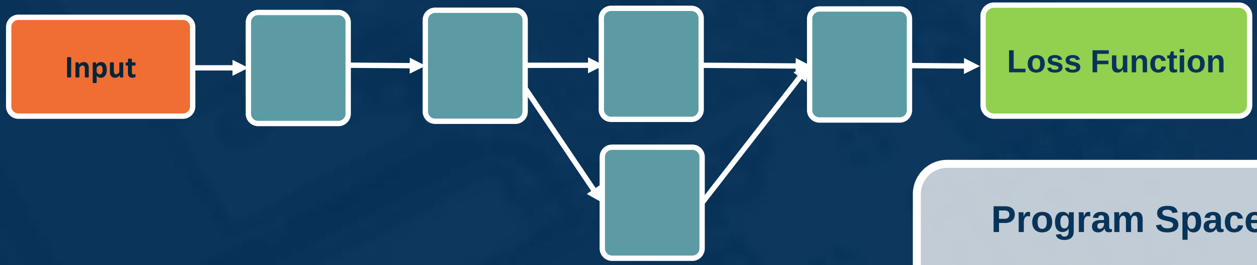
Linear classifiers

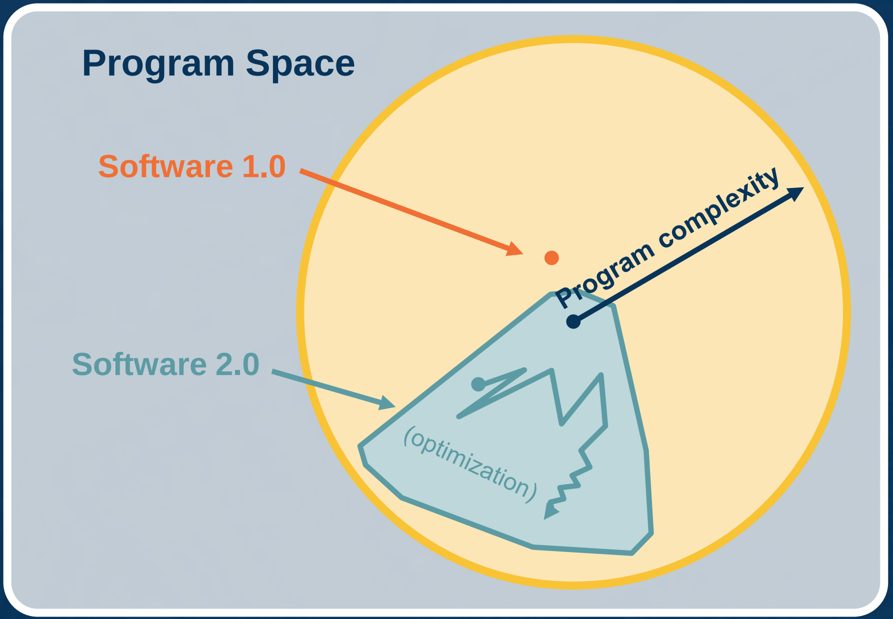


This image is CC0 1.0 public domain

Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

The Power of Deep Learning





Adapted from figure by Andrej Karpathy

What is the **simplest function** you can think of?

Our model is:

$$f(x, w) = w \cdot x + b$$

Classifier Result

Weights

Input

Bias (scalar)

(Note if $\boldsymbol{w}$ and $\mathbf{x}$ are column vectors we often show this as $\boldsymbol{w}^T \boldsymbol{x}$)

Linear Classification and Regression

Simple linear classifier:

- Calculate score:
  $$f(x, w) = w \cdot x + b$$
- Binary classification rule (w is a vector):

$$y = \begin{cases} 1 & \text{if } f(x, w) >= 0 \\ 0 & \text{otherwise} \end{cases}$$

- For multi-class classifier take class with highest (max) score
  $$f(x, W) = Wx + b$$

Input Dimensionality

Data: Image

Model

$$f(x, W) = Wx + b$$

Class Scores

$$x = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1n} \\ x_{21} & x_{22} & \cdots & x_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nn} \end{bmatrix}$$

Flatten

$$x = \begin{bmatrix} x_{11} \\ x_{12} \\ \vdots \\ x_{21} \\ x_{22} \\ \vdots \\ x_{n1} \\ \vdots \\ x_{nn} \end{bmatrix}$$

To simplify notation we will refer to inputs as $x_1 \cdots x_m$ where $m = n \times n$

Model

$$f(x, W) = Wx + b$$

Classifier for class 1 →
Classifier for class 2 →
Classifier for class 3 →

$$\underbrace{\begin{bmatrix} w_{11} & w_{12} & \cdots & w_{1m} \\ w_{21} & w_{22} & \cdots & w_{2m} \\ w_{31} & w_{32} & \cdots & w_{3m} \end{bmatrix}}_{\boldsymbol{W}} \underbrace{\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \end{bmatrix}}_{\boldsymbol{x}} + \underbrace{\begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}}_{\boldsymbol{b}}$$

(Note that in practice, implementations can use xW instead, assuming a different shape for W. That is just a different convention and is equivalent.)

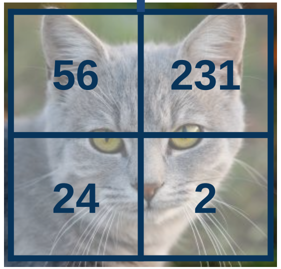
- We can move the bias term into the weight matrix, and a "1" at the end of the input
- Results in **one matrix-vector multiplication**!

Model
$$f(x, W) = Wx + b$$

$$\underbrace{\begin{bmatrix} w_{11} & w_{12} & \cdots & w_{1m} & b_1 \\ w_{21} & w_{22} & \cdots & w_{2m} & b_2 \\ w_{31} & w_{32} & \cdots & w_{3m} & b_3 \end{bmatrix}}_{\boldsymbol{W}} \underbrace{\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \\ 1 \end{bmatrix}}_{\boldsymbol{x}}$$

Example with an image with **4 pixels**, and **3 classes** (cat/dog/ship)

Stretch pixels into column



Input image

$$\underbrace{\begin{bmatrix} 0.2 & -0.5 & 0.1 & 2.0 \\ 1.5 & 1.3 & 2.1 & 0.0 \\ 0 & 0.25 & 0.2 & -0.3 \end{bmatrix}}_{W} \begin{bmatrix} 56 \\ 231 \\ 24 \\ 2 \end{bmatrix} + \underbrace{\begin{bmatrix} 1.1 \\ 3.2 \\ -1.2 \end{bmatrix}}_{b} = \begin{array}{l} \begin{bmatrix} -96.8 \\ 437.9 \\ 61.95 \end{bmatrix} \end{array} \begin{array}{l} \text{Cat score} \\ \text{Dog score} \\ \text{Ship score} \end{array}$$

Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

airplane
automobile
bird
cat
deer
dog
frog
horse
ship
truck

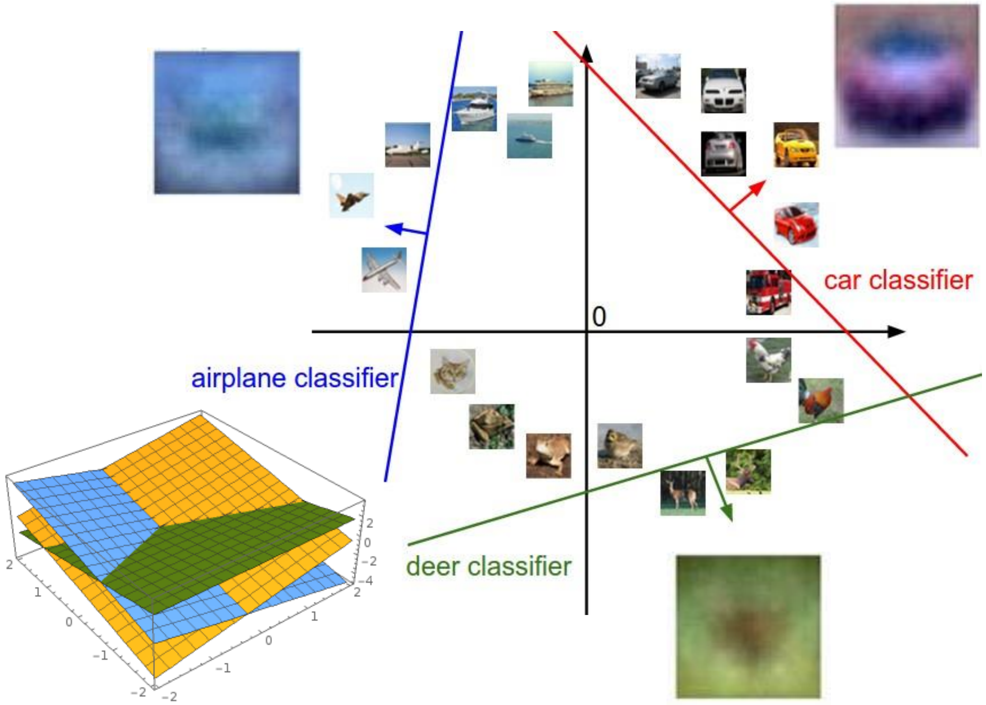
Visual Viewpoint

We can convert the weight vector back into the shape of the image and visualize

plane car bird cat deer dog frog horse ship truck

Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

Geometric Viewpoint



Plot created using Wolfram Cloud

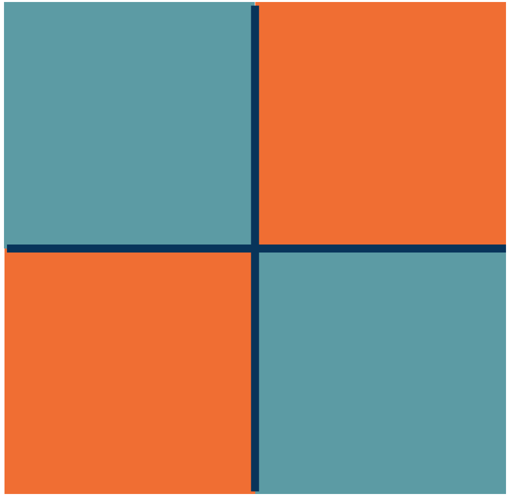
$$f(x, W) = Wx + b$$

Array of **32x32x3** numbers
(3072 numbers total)

Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

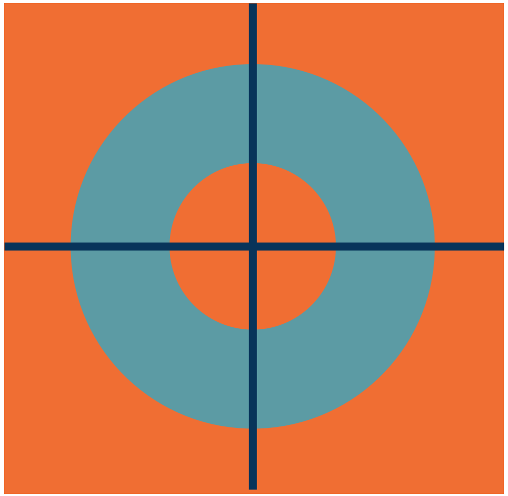
Class 1:
number of pixels > 0 odd

Class 2:
number of pixels > 0 even



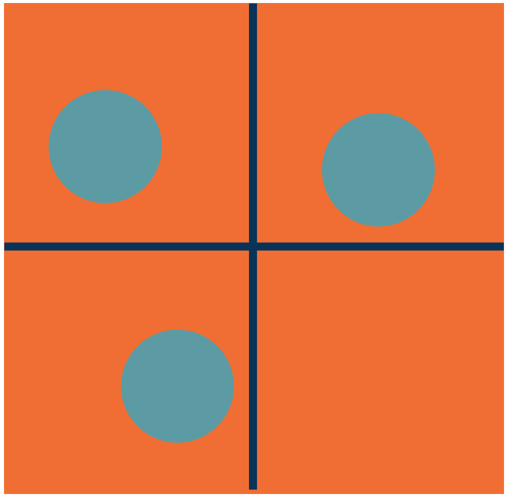
Class 1:
1 < = L2 norm < = 2

Class 2:
Everything else



Class 1:
Three modes

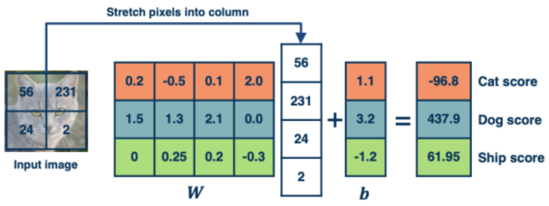
Class 2:
Everything else



Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

Algebraic Viewpoint

$$f(x, W) = Wx$$

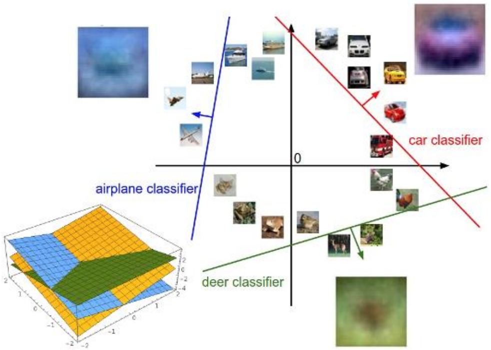


Visual Viewpoint

One template per class

Geometric Viewpoint

Hyperplanes cutting up space



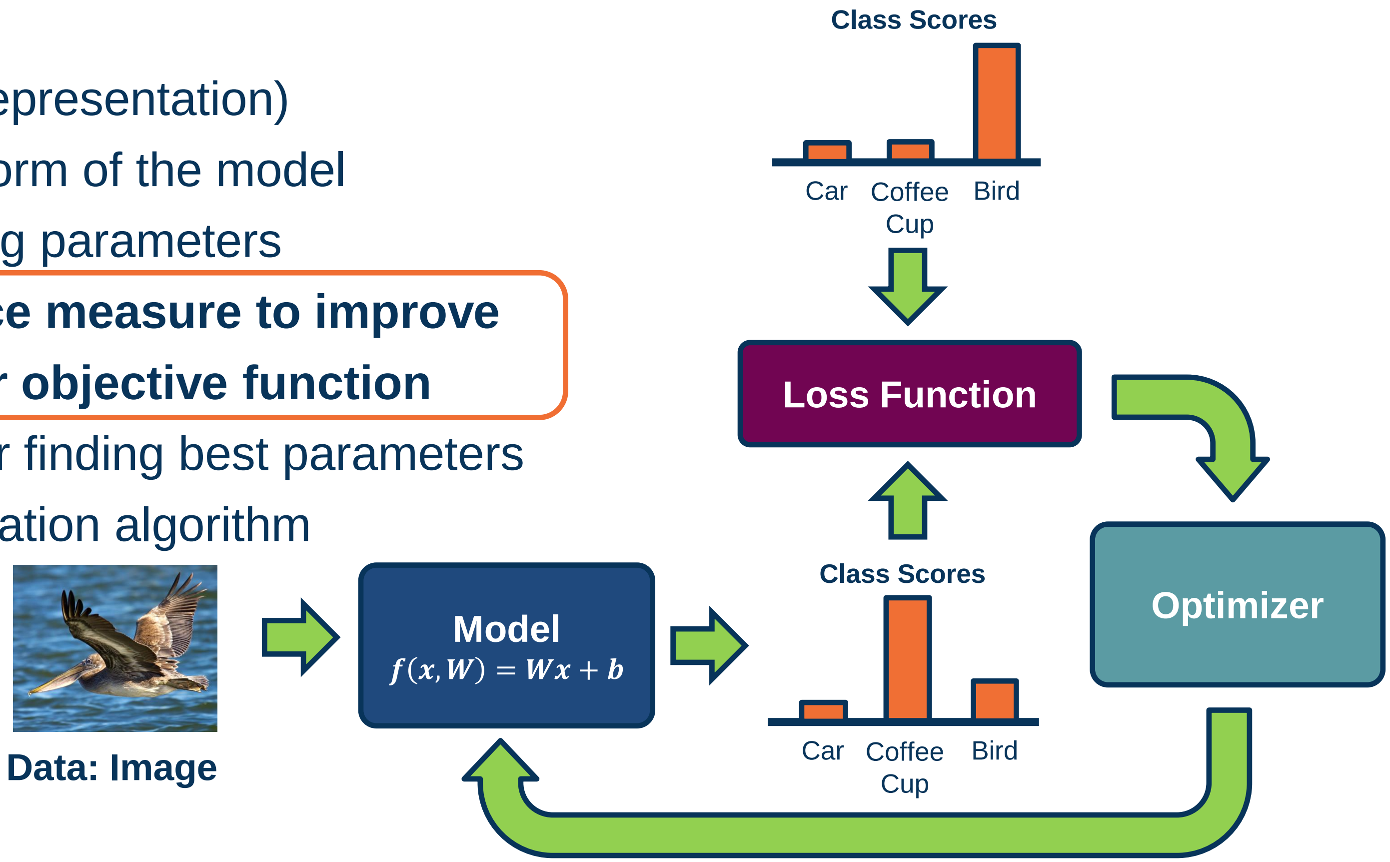
Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

- We will learn complex, parameterized functions
  - Start w/ simple building blocks such as linear classifiers
- Key is to learn parameters, but learning is hard
  - Sources of generalization error
  - Add bias/assumptions via architecture, loss, optimizer
- Components of parametric classifiers:
  - Input/Output, Model (function), Loss function, Optimizer
  - Example: Image/Label, Linear Classifier, Hinge Loss, ?

Summary

Next Time:

- Input (and representation)
- Functional form of the model
  - Including parameters
- **Performance measure to improve**
  - **Loss or objective function**
- Algorithm for finding best parameters
  - Optimization algorithm



Components of a Parametric Model

Several issues with scores:

- Not very interpretable (no bounded value)

We often want **probabilities**

- More interpretable
- Can relate to probabilistic view of machine learning

We use the **softmax** function to convert scores to probabilities

$$s = f(x, W)$$ **Scores**

$$P(Y = k | X = x) = \frac{e^{s_k}}{\sum_j e^{s_j}}$$ **Softmax Function**

Performance Measure

We need a performance measure to **optimize**

- Penalizes model for being wrong
- Allows us to modify the model to reduce this penalty
- Known as an **objective** or **loss** function

In machine learning we use **empirical risk minimization**

- Reduce the loss over the **training** dataset
- We **average** the loss over the training data

Given a dataset of examples:

$$\{(x_i, y_i)\}_{i=1}^{N}$$

Where x_i is image and

y_i is (integer) label

Loss over the dataset is a sum of loss over examples:

$$L = \frac{1}{N} \sum L(f(x_i, W), y_i)$$