Topics:

- Recurrent Neural Networks (RNNs)
- Long Short-Term Memory

CS 4644-DL / 7643-A ZSOLT KIRA

- Assignment 2 Due June. 22nd
 - Implement convolutional neural networks
 - Resources (in addition to lectures):
 - DL book: Convolutional Networks
 - CNN notes https://www.cc.gatech.edu/classes/AY2022/cs7643 spring/assets/L10 cnns notes.pdf
 - Backprop notes https://www.cc.gatech.edu/classes/AY2023/cs7643 spring/assets/L10 cnns backprop notes.pdf
 - HW2 Tutorial (@176)
 - Slower OMSCS lectures on dropbox: Module 2 Lessons 5-6 (M2L5/M2L6) (https://www.dropbox.com/sh/iviro188gq0b4vs/AADdHxX_Uy1TkpF_yvIzX0nPa?dl=0)

• Meta Office Hours – First one on language modeling today 3pm ET

- **GPU resources**: Google Colab, PACE-ICE
 - Google Cloud posted soon (for projects)

Module 3 Introduction





The Space of Architectures

Georgia Tech



Recurrent Neural Networks & Transformers







(C) Dhruv Batra



Image Credit: Andrei Karpathy

Why model sequences?







Figure Credit: Carlos Guestrin

Sequences are everywhere...



y = please return the car .



(C) Dhruv Batra Image Credit: Alex Graves and Kevin Gimpel

• It's a spectrum...

one to one

Input: No sequence

Output: No sequence

Example: "standard" classification / regression problems





• It's a spectrum...



Input: No sequence Output: No sequence Example: "standard" classification / regression problems

Input: No sequence Output: Sequence Example: Im2Caption





• It's a spectrum...



Output: No sequence Example: "standard" classification / regression problems Input: No sequence Output: Sequence

Example: Im2Caption

Input: Sequence

Output: No sequence

Example: sentence classification, multiple-choice question answering

(C) Dhruv Batra Image Credit: Andrej Karpathy



• It's a spectrum...







What's wrong with MLPs?

- Problem 1: Can't model sequences
 - Fixed-sized Inputs & Outputs
 - No temporal structure





(C) Dhruv Batra

Image Credit: Alex Graves, book

What's wrong with MLPs?

- Problem 1: Can't model sequences
 - Fixed-sized Inputs & Outputs
 - No temporal structure

 Problem 2: Pure feed-forward processing – No "memory", no feedback





(C) Dhruv Batra

Image Credit: Alex Graves, book

3 Key Ideas

- The notion of memory (state)
 - We want to propagate information across the sequence
 - We will do this with *state*, represented by a vector (embedding/representation)
 - Key idea will be mixing new inputs with this state, to yield a new state
 - All represented as vector operations
 - Just as a CNN represents an image with the final hidden vector/embedding before the final classifier



3 Key Ideas

• The notion of memory (state)

- Parameter Sharing
 - in computation graphs = adding gradients





Computational Graph



Gradients add at branches





3 Key Ideas

• The notion of memory (state)

- Parameter Sharing
 - in computation graphs = adding gradients
- "Unrolling"
 - in computation graphs with parameter sharing



New Words

- Recurrent Neural Networks (RNNs)
- Recursive Neural Networks
 - General family; think graphs instead of chains
- Types:
 - "Vanilla" RNNs (Elman Networks)
 - Long Short Term Memory (LSTMs)
 - Gated Recurrent Units (GRUs)
 - ...
- Algorithms
 - BackProp Through Time (BPTT)
 - BackProp Through Structure (BPTS)



Recurrent Neural Network

- Idea: Input is a **sequence** and we will process it sequentially though a neural network module with *state*
- For each timestep (element of sequence):





Recurrent Neural Network





(Vanilla) Recurrent Neural Network

The state consists of a single "hidden" vector h:







(Vanilla) Recurrent Neural Network

The state consists of a single *"hidden"* vector **h**:

y

RNN h

Х

>
$$y_{t} = W_{hy}h_{t} + b_{y}$$
>
$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n



Recurrent Neural Network





Recurrent Neural Network

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

$$h_t = f_W(h_{t-1}, x_t)$$

Notice: the same function and the same set of parameters are used at every time step.

















Re-use the same weight matrix at every time-step





RNN: Computational Graph: Many to Many







RNN: Computational Graph: Many to Many











RNN: Computational Graph: Many to One





RNN: Computational Graph: One to Many





Sequence to Sequence: Many-to-one + one-to-many

Many to one: Encode input sequence in a single vector




Sequence to Sequence: Many-to-one + one-to-many





How can we train this on language?

- We have a generic sequence-in, sequence-out model
- How do we train this on language?
- Supervised Learning:
 - Sentiment analysis (sentence -> negative/neutral/positive) labeled by humans
 - Translation -> English and equivalent other language
- Self-supervised: Predict the next letter or word!
 - This is extremely powerful!!
 - In order to predict what's next, it needs to really understand not just language statistics but world knowledge!
 - Of course, we need scale for this level of loss reduction / understanding



- **Training:** A large corpus of text from the web
 - Note: No annotation required! It's just "the text"
- Inference: Just generate me new text
 - Can condition on some initial input (prompt)

```
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
#define REG PG
                vesa_slot_addr_pack
#define PFM NOCOMP AFSR(0, load)
#define STACK DDR(type)
                            (func)
#define SWAP ALLOCATE(nr)
                              (e)
#define emulate sigs() arch get unaligned child()
#define access_rw(TST) asm volatile("movd %%esp, %0, %3" : : "r" (0)); \
 if ( type & DO READ)
static void stat PC_SEC __read mostly offsetof(struct seq argsqueue, \
         pC>[1]);
static void
os prefix(unsigned long sys)
#ifdef CONFIG PREEMPT
 PUT PARAM RAID(2, sel) = get state state();
 set_pid_sum((unsigned long)state, current_state_str(),
           (unsigned long)-1->lr full; low;
```



Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**





Example: Character-level Language Model

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$$

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**





Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**





Training Time: MLE / "Teacher Forcing"

Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**





Example: Character-level Language Model Sampling

Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model





Example: Character-level Language Model Sampling

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Example: Character-level Language Model Sampling

Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model



Can also feed in predictions during training (student forcing)









time

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           (unsigned long)-1->lr full; low;
```





Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016



Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016

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"You mean to imply that I have nothing to eat out of.... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."

quote detection cell

Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016 Figures copyright Karpathy, Johnson, and Fei-Fei, 2015; reproduced with permission

Cell sensitive to position in line:

The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae-pressed forward into boats and into the ice-covered water and did not,

line length tracking cell

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Cell that turns on inside comments and quotes:







code depth cell

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$



Backpropagation from h_t to h_{t-1} multiplies by W (actually W_{hh})



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\begin{pmatrix}W_{hh} & W_{hx}\end{pmatrix}\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h_0 involves many factors of W (and repeated tanh)



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1}+W_{xh}x_t)W_{hh}$$



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", IOML 2013





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Computing gradient of h_0 involves many factors of W (and repeated tanh)

With no non-linearity:

Largest singular value > 1: Exploding gradients

Largest singular value < 1: Vanishing gradients



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013





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Long Short Term Memory (LSTM)

$$h_t = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)$$

Vanilla RNN

$$\begin{pmatrix}
i \\
f \\
o \\
g
\end{pmatrix} = \begin{pmatrix}
\sigma \\
\sigma \\
\sigma \\
tanh
\end{pmatrix} W \begin{pmatrix}
h_{t-1} \\
x_t
\end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

LSTM

Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997





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Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

LSTMs Intuition: Memory

• Cell State / Memory





LSTMs Intuition: Forget Gate

• Should we continue to remember this "bit" of information or not? $f_{t} = \sigma \left(W_{f} \cdot [h_{t-1}, x_{t}] + b_{f} \right)$

 x_t



LSTMs Intuition: Input Gate

- Should we update this "bit" of information or not?
 - If so, with what?



$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$



LSTMs Intuition: Memory Update

• Forget that + memorize this



 $C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$



LSTMs Intuition: Output Gate

• Should we output this "bit" of information to "deeper" layers?



$$o_t = \sigma \left(W_o \left[h_{t-1}, x_t \right] + b_o \right)$$
$$h_t = o_t * \tanh \left(C_t \right)$$



LSTMs Intuition: Additive Updates



Backpropagation from c_t to c_{t-1} only elementwise multiplication by f, no matrix multiply by W



LSTMs Intuition: Additive Updates





LSTMs Intuition: Additive Updates







Other RNN Variants

[An Empirical Exploration of Recurrent Network Architectures, Jozefowicz et al., 2015]

MUT1:

 $\begin{array}{lll} z &=& \mathrm{sigm}(W_{\mathrm{xz}}x_t+b_{\mathrm{z}})\\ r &=& \mathrm{sigm}(W_{\mathrm{xr}}x_t+W_{\mathrm{hr}}h_t+b_{\mathrm{r}})\\ h_{t+1} &=& \mathrm{tanh}(W_{\mathrm{hh}}(r\odot h_t)+\mathrm{tanh}(x_t)+b_{\mathrm{h}})\odot z\\ &+& h_t\odot(1-z) \end{array}$

MUT2:

$$z = \operatorname{sigm}(W_{xz}x_t + W_{hz}h_t + b_z)$$

$$r = \operatorname{sigm}(x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

MUT3:

$$z = \operatorname{sigm}(W_{\operatorname{xz}}x_t + W_{\operatorname{hz}}\tanh(h_t) + b_z)$$

$$r = \operatorname{sigm}(W_{\operatorname{xr}}x_t + W_{\operatorname{hr}}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{\operatorname{hh}}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$





Image Embedding (VGGNet)





Image Embedding (VGGNet)



Image Embedding (VGGNet)